

# Exotic Metals from Geometrical Frustration

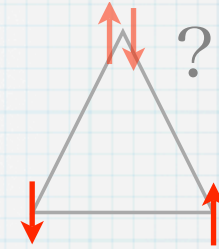
---

**Minoru NOHARA**

**Department of Physics, Okayama University**

# Topics

## (1) Pseudogap Metal in $\text{LiVS}_2$



**N. Katayama and H. Takagi**

University of Tokyo

**M.Uchida, D.Hashizume, S.Niitaka, and J. Matsuno**

RIKEN

**D.Matsumura, Y.Nishihata, and J.Mizuki**

JAEA

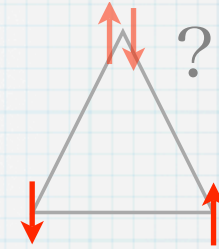
## (2) High-Entropy Metal in $\text{CuRhO}_2$

**H.Kuriyama, K.Takubo, T.Mizokawa, K.Kimura,  
and H.Takagi**

University of Tokyo

# Topics

## (1) Pseudogap Metal in $\text{LiVS}_2$



**N. Katayama and H. Takagi**

University of Tokyo

**M.Uchida, D.Hashizume, S.Niitaka, and J. Matsuno**

RIKEN

**D.Matsumura, Y.Nishihata, and J.Mizuki**

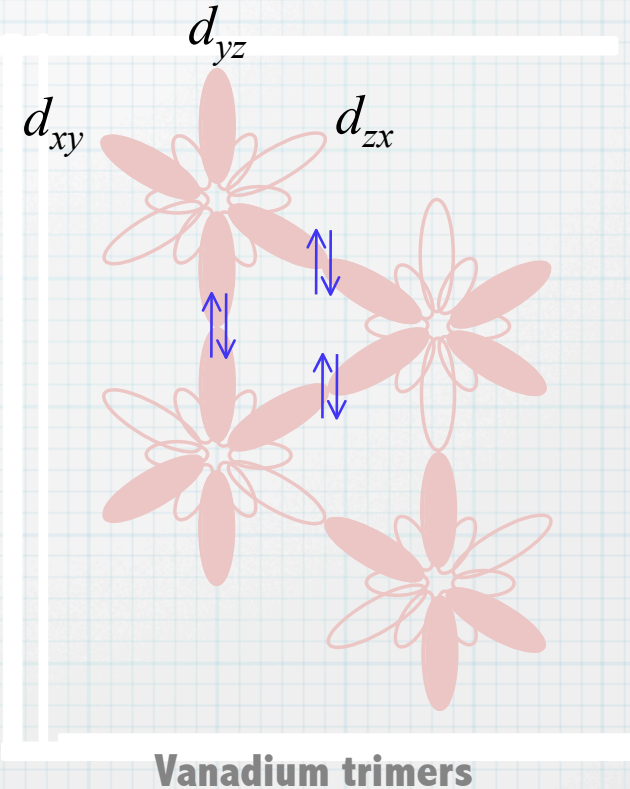
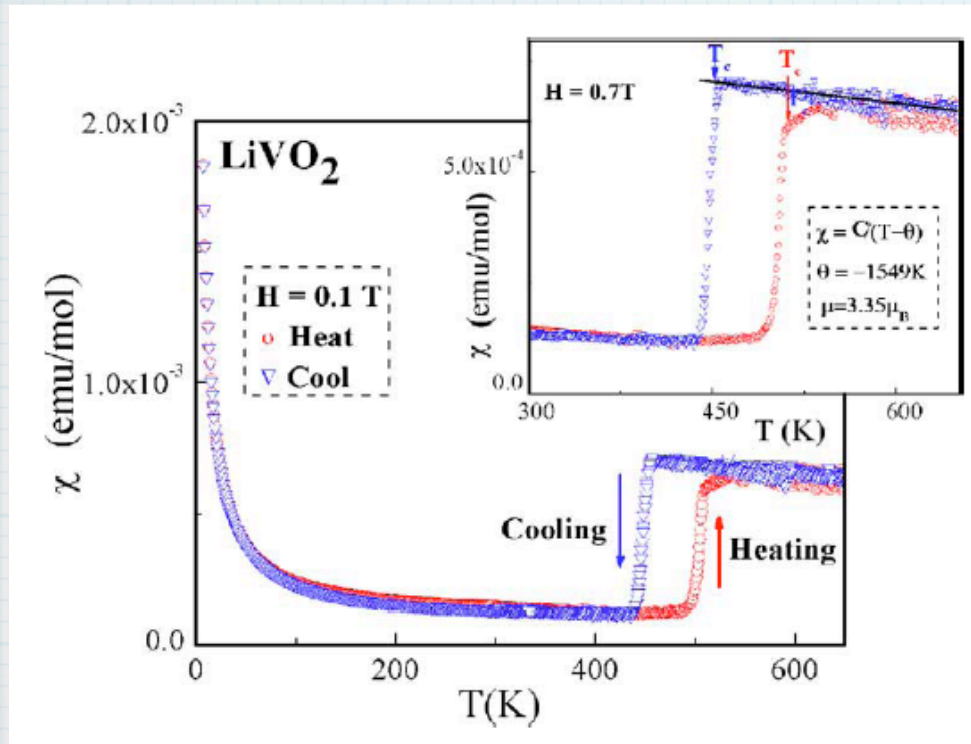
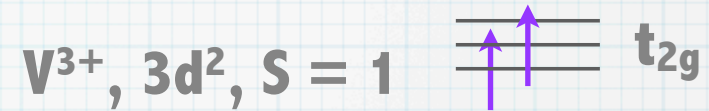
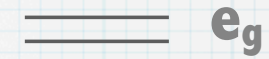
JAEA

## (2) High-Entropy Metal in $\text{CuRhO}_2$

**H.Kuriyama, K.Takubo, T.Mizokawa, K.Kimura,  
and H.Takagi**

University of Tokyo

# Valence Bond Solid in $\text{LiVO}_2$



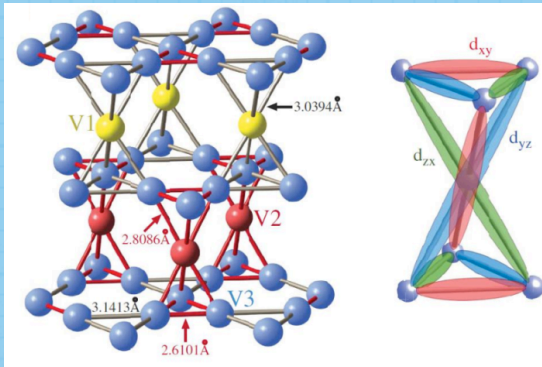
W. Tian *et al.*, Mater. Res. Bull. **39** (2004) 1319 .

**Weiss  $T = -1500 \text{ K}$  (AF), indicating strong frustration.**

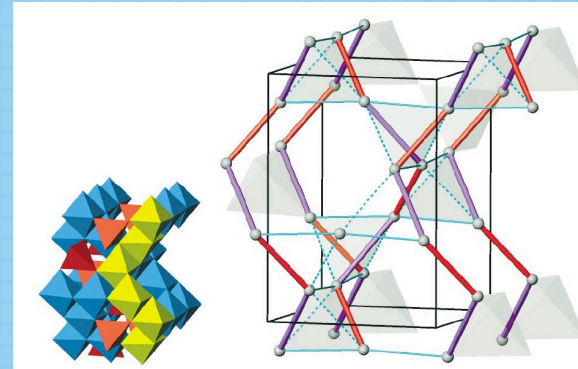
**1st order transition from CW insulator to non-magnetic insulator at  $\sim 500 \text{ K}$ .**

# Valence Bond Solids are ubiquitous

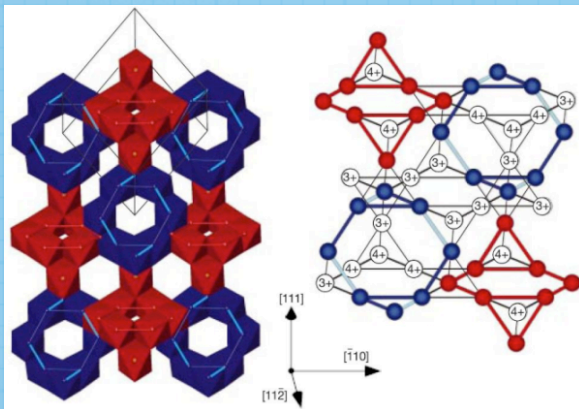
## Pyrochlore Lattice



heptmer in  $\text{AlV}_2\text{O}_4$

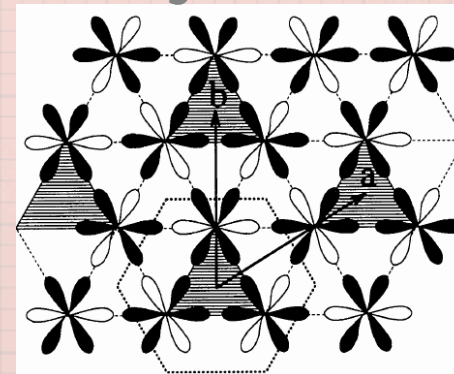


Helical dimer in  $\text{MgTi}_2\text{O}_4$



Octmer in  $\text{CuIr}_2\text{S}_4$

## Triangular Lattice

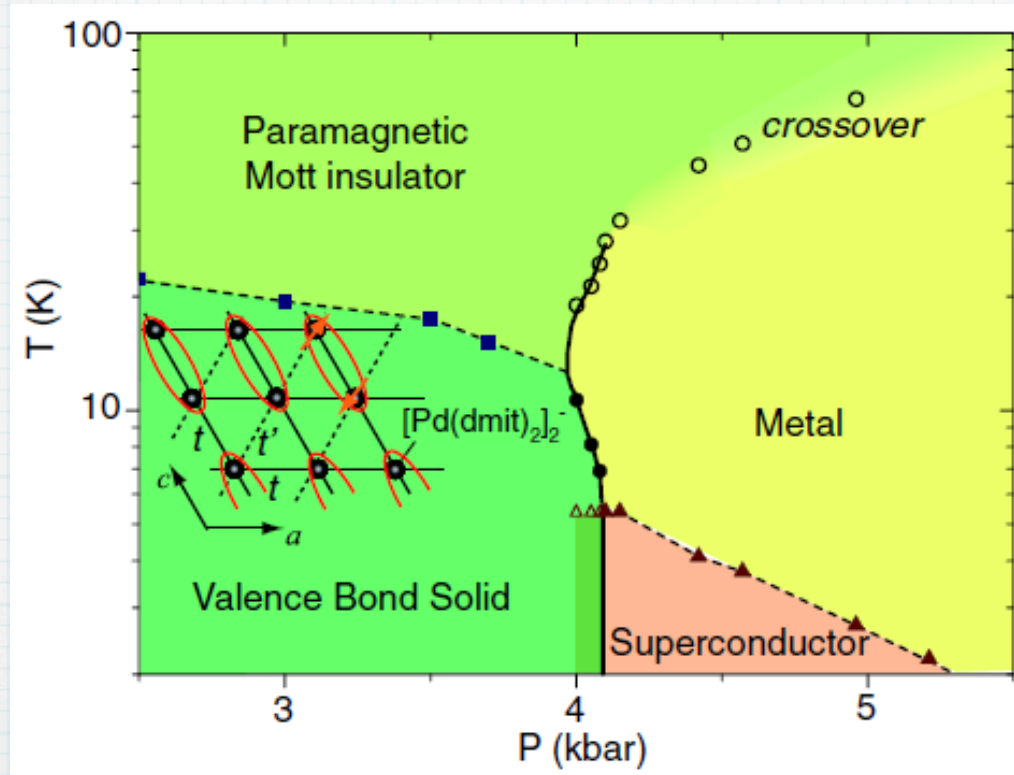


Trimer in  $\text{LiVO}_2$

$$\frac{1}{\sqrt{2}} (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)$$



# What kind of metal do we expect if VBS melts ?



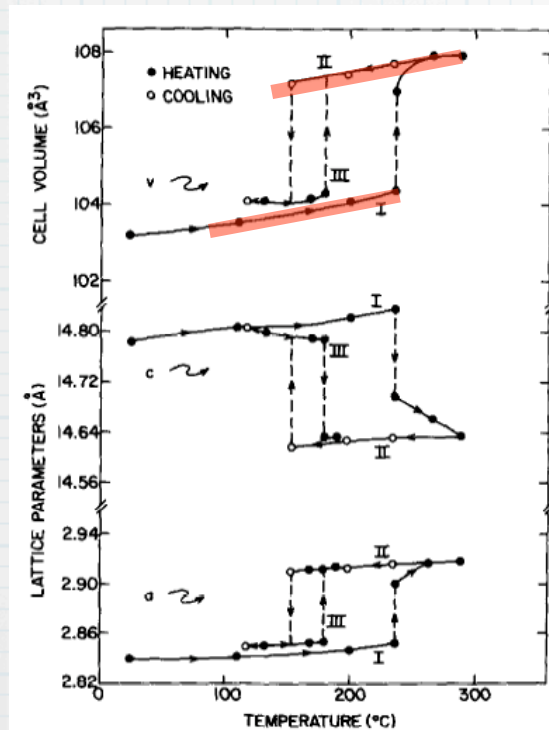
Shimizu *et al.*, PRL **99**, 256403 (2007).

**In organic systems, BVS melts under pressure and superconductivity emerges.**

**Spin singlet in real space turns into spin singlet in k-space.**

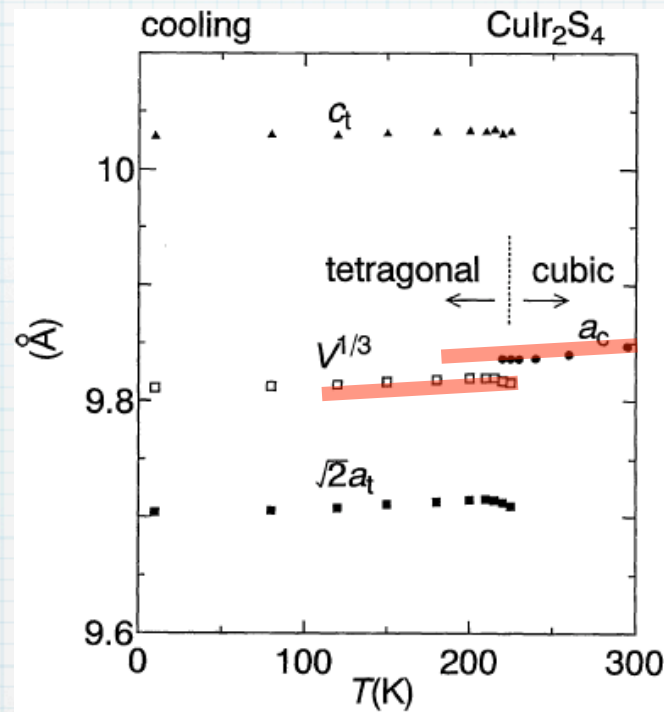
# Inorganic Systems: VBS is stabilized by Pressure

Trimer in  $\text{Li}_{0.8}\text{VO}_2$

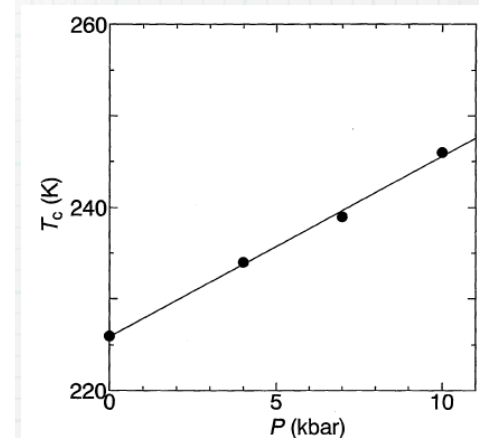


Cardoso *et al.*, J. Solid State Chem.  
**72**, 234 (1988).

Octamer in  $\text{CuIr}_2\text{S}_4$



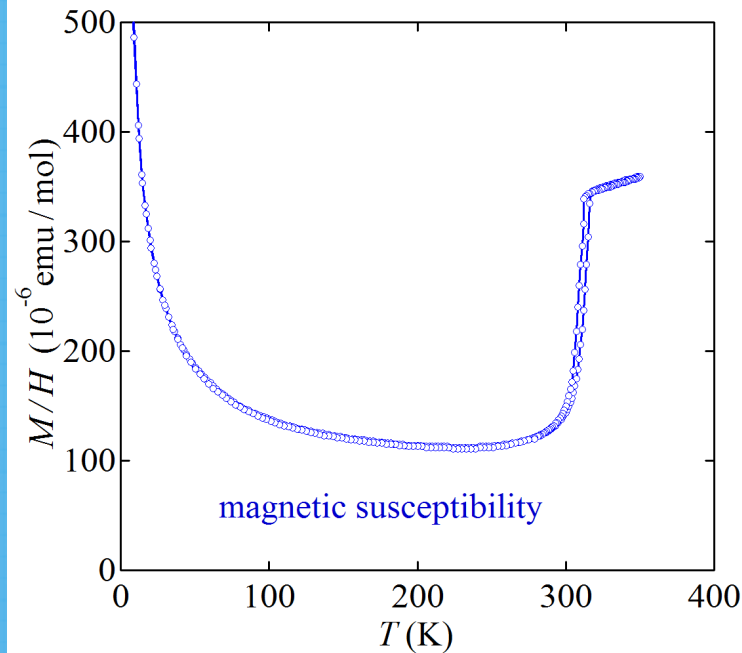
Furubayashi *et al.*, JPSJ **63**, 3333 (1994).



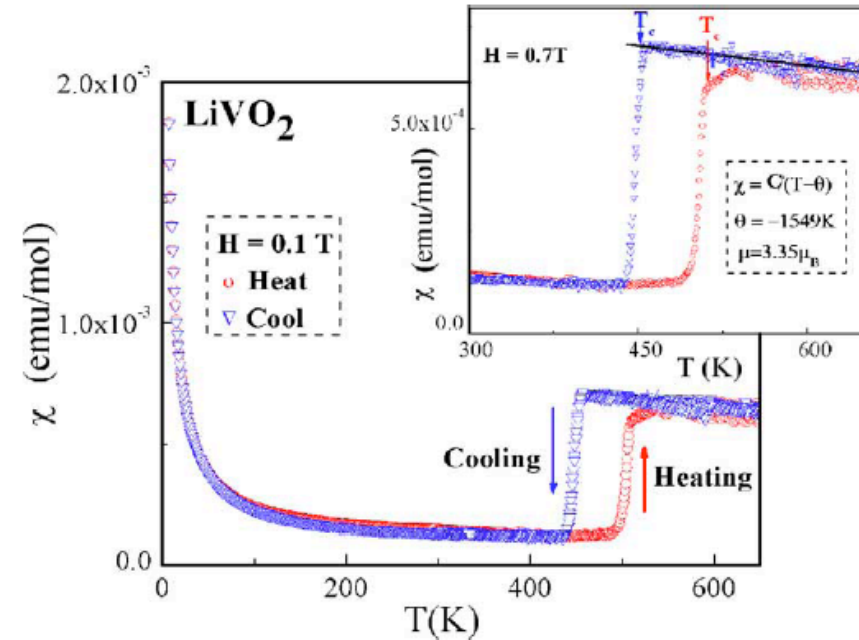
**Cell volume decreases at the VBS transition.**

# Negative pressure by chemical substitution

LiVS<sub>2</sub>



LiVO<sub>2</sub>



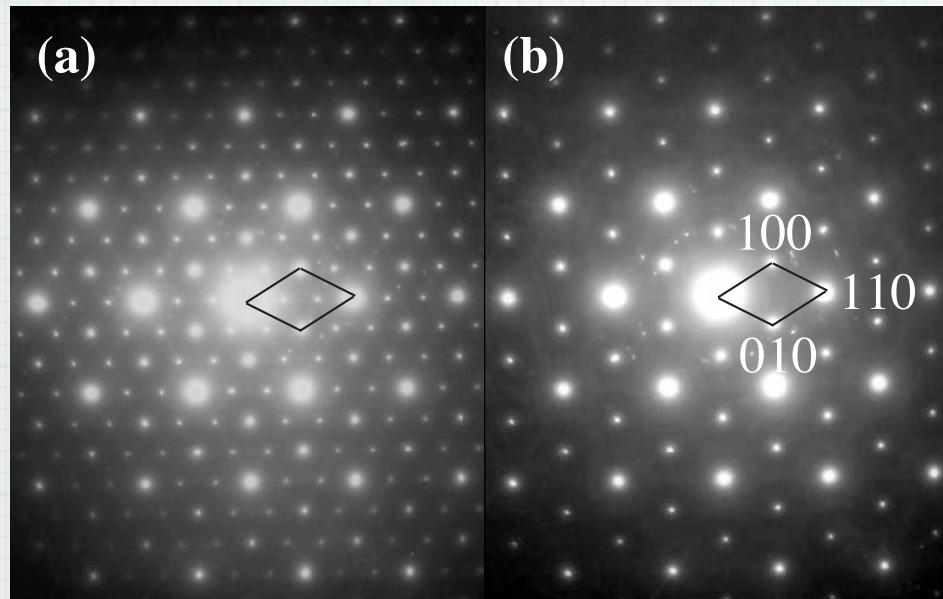
W. Tian *et al.*, Mater. Res. Bull. **39** (2004) 1319 .

**Transition Temperature is reduced by replacing O to S.**



# Trimer at low temperatures in $\text{LiVS}_2$

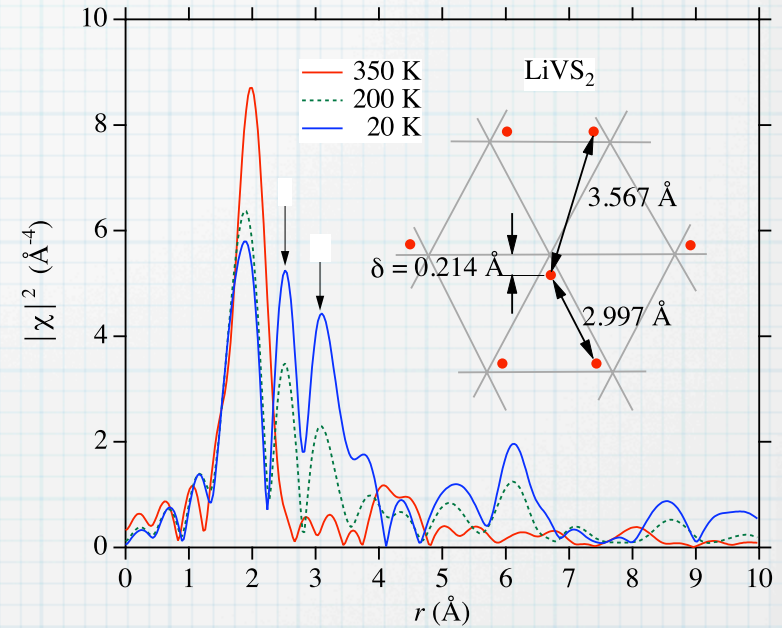
Electron Diffraction



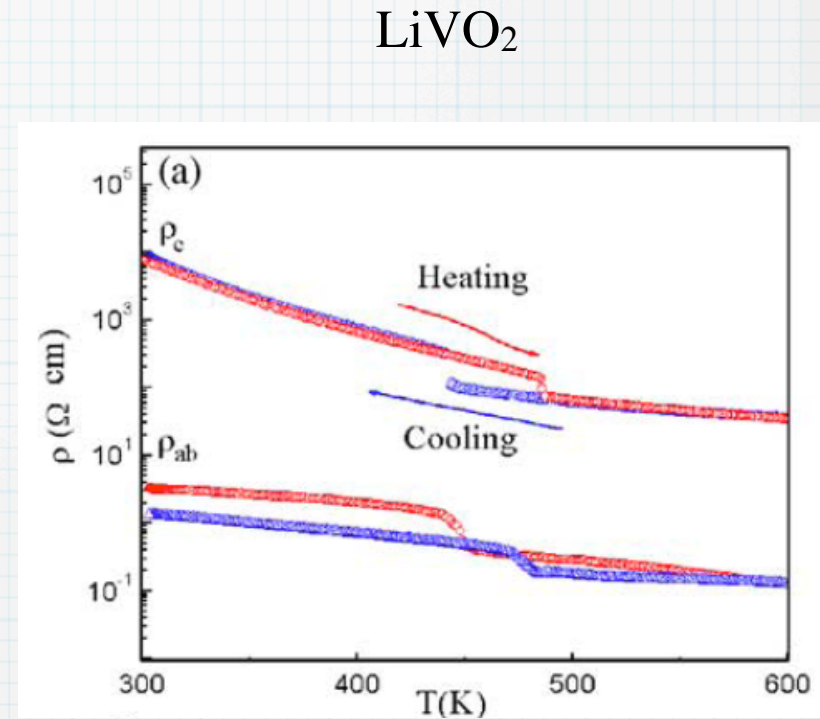
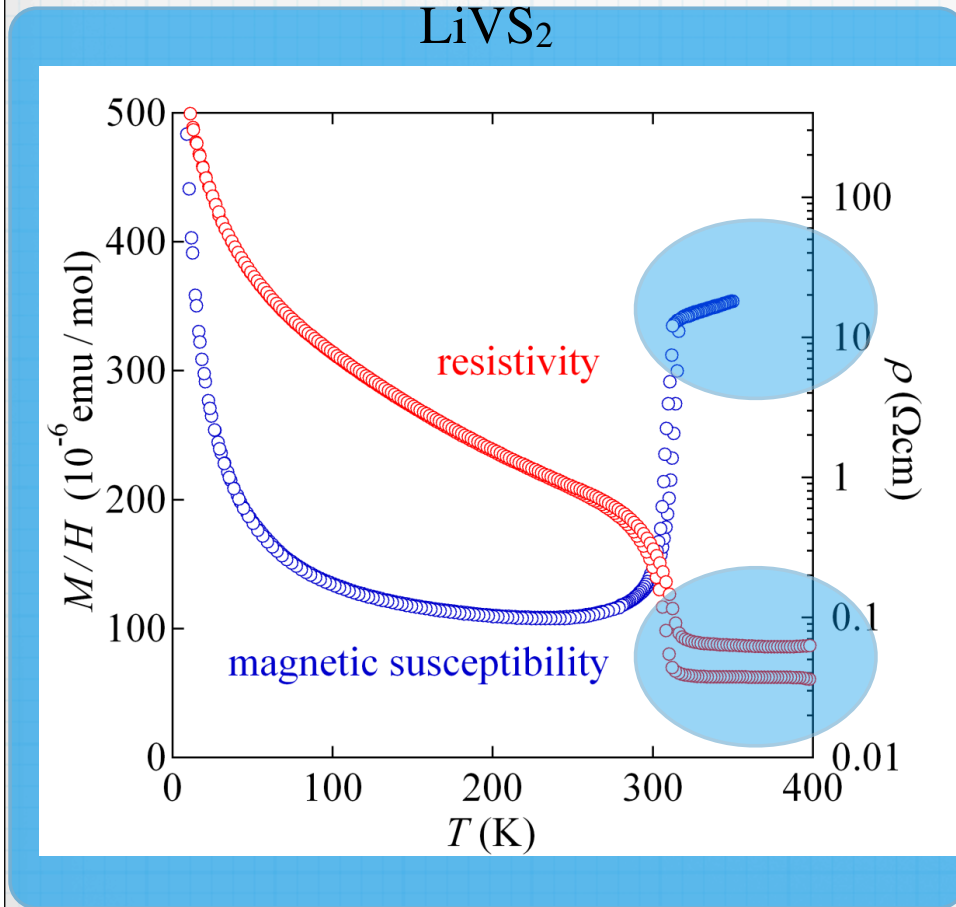
295 K ( $< T_c$ )  
{1/3, 1/3, 0}  
superlattice

350 K

EXAFS, BL14B1, SPring-8



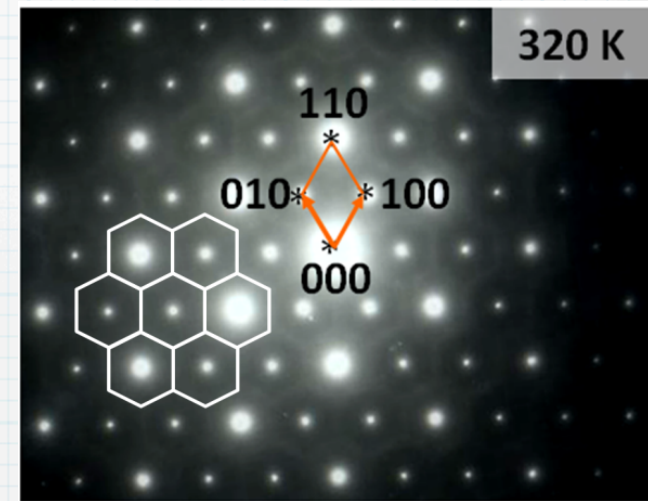
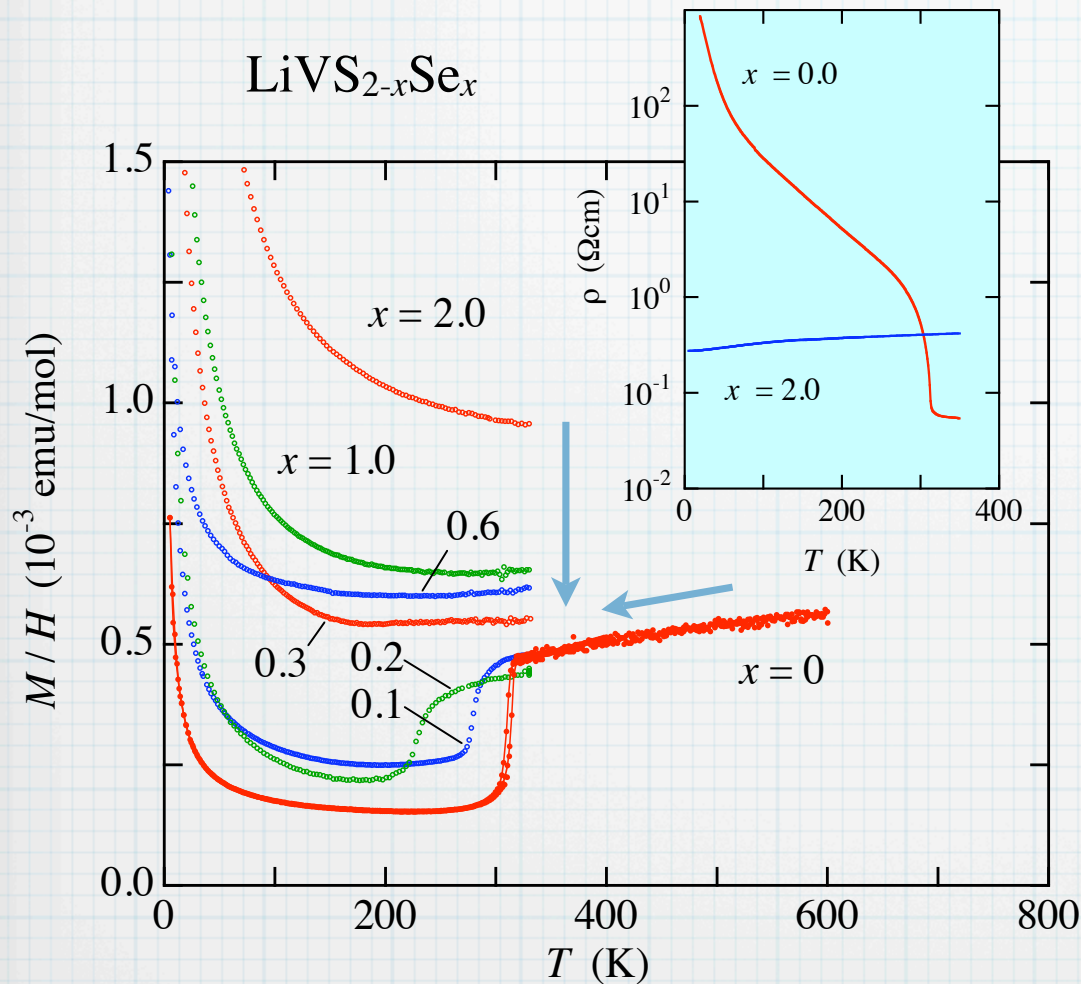
# Metal-Insulator Transition in $\text{LiVS}_2$



W. Tian *et al.*, Mater. Res. Bull. **39** (2004) 1319.

**VBS is robust irrespective of high temperature phases,  
metallic in  $\text{LiVS}_2$  and semiconducting in  $\text{LiVO}_2$ .**

# Pseudogap behavior in the metallic phase

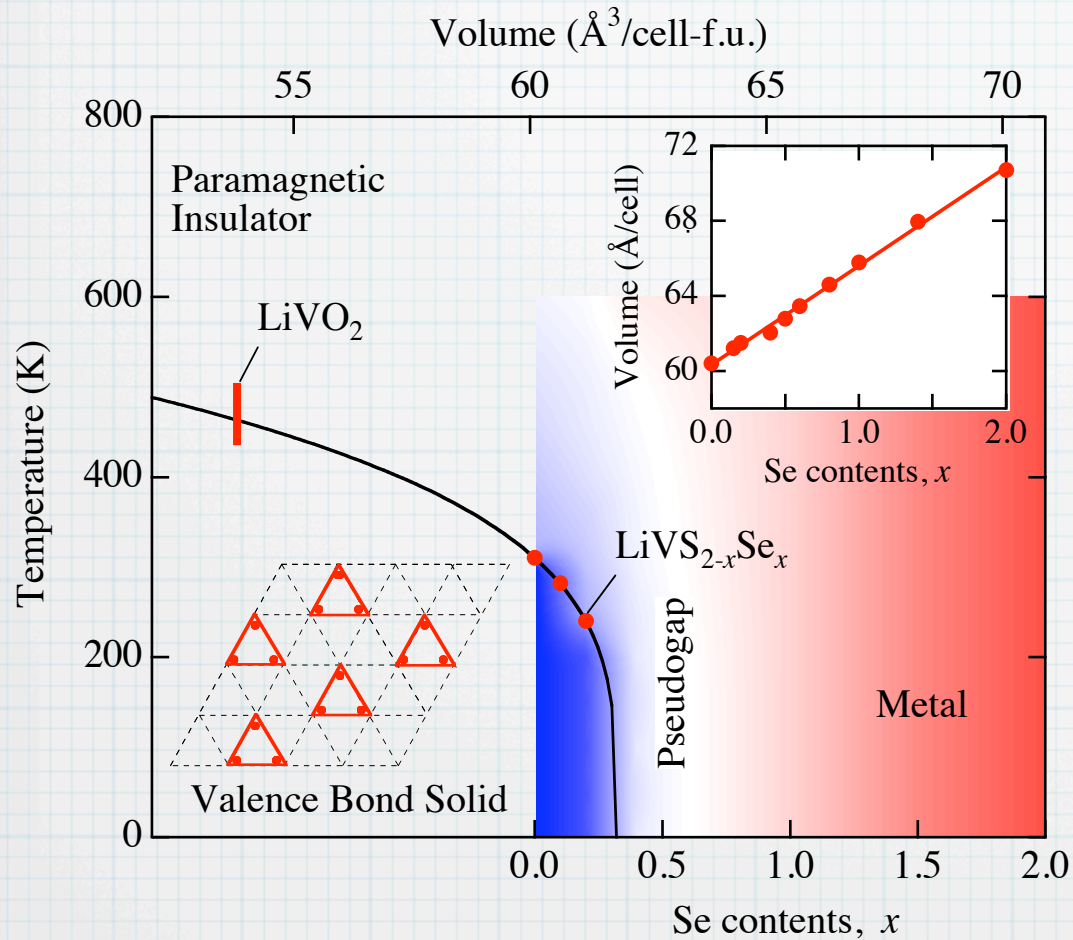


Diffuse scattering due to local trimer formation.

VBS state is suppressed by Se doping.

Gradual decrease in susceptibility by approaching VBS phase, indicative local singlet.

# Conclusion



**VBS can be melted by negative pressure.**

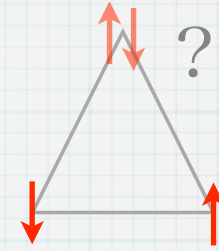
**VBS is robust from insulating to metallic side.**

**No superconductivity when VBS melts.**

**Short range correlation, or pseudogap, at the vicinity of phase boundary.**

# Topics

## (1) Pseudogap Metal in $\text{LiVS}_2$



N. Katayama and H. Takagi

University of Tokyo

M.Uchida, D.Hashizume, S.Niitaka, and J. Matsuno

RIKEN

D.Matsumura, Y.Nishihata, and J.Mizuki

JAEA

## (2) High-Entropy Metal in $\text{CuRhO}_2$

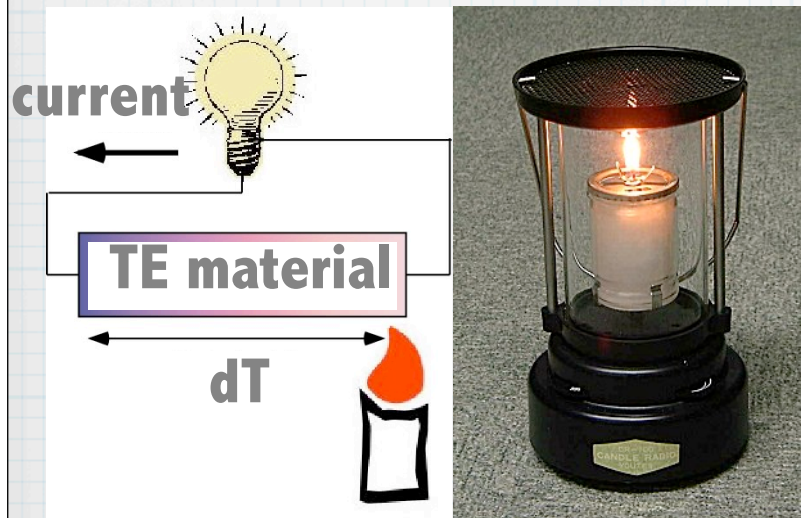
H.Kuriyama, K.Takubo, T.Mizokawa, K.Kimura,  
and H.Takagi

University of Tokyo



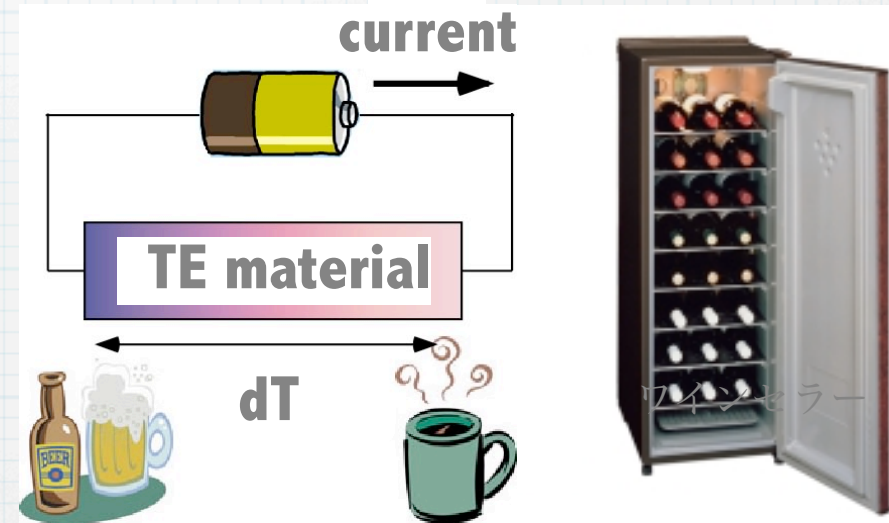
# Frustration can be a new route to thermoelectric materials

## Power Generation



Candle Radio

## Peltier Cooling



Refrigerator

# Requirements for thermoelectric materials

## 1. Large "Power Factor" (PF)

$$PF = S^2 \sigma$$

Large Seebeck

$$S = \Delta V / \Delta T$$

High electrical conductivity

$\sigma$

## 2. Large "Dimensionless Figure of Merit" (ZT)

$$ZT = \left( \frac{S^2 \sigma}{\kappa} \right) T$$

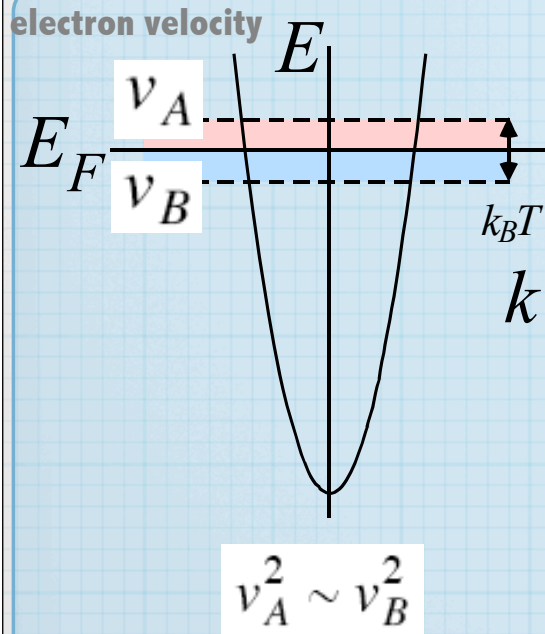
Large PF

$PF$

Low thermal conductivity

$\kappa$

# Hard to realize both “large Seebeck” and “high



**Large Fermi surface**

$$\sigma \propto v_A^2 + v_B^2 \quad \text{Large}$$

$$\text{Small } PF = S^2 \sigma$$

**Symmetric band to  $E_F$**

$$S \propto \frac{v_A^2 - v_B^2}{v_A^2 + v_B^2} \sim 0$$

**Boltzmann's  
transport**

$$\sigma = e^2 K_0$$

$$S = \frac{1}{eT} \frac{K_1}{K_0}$$

$$K_n = \sum_k \tau(k) v(k) v(k) \left[ -\frac{\partial f}{\partial E} \right] (E_k - \mu)^n$$

$$K_0 \sim (v_A^2 + v_B^2)$$

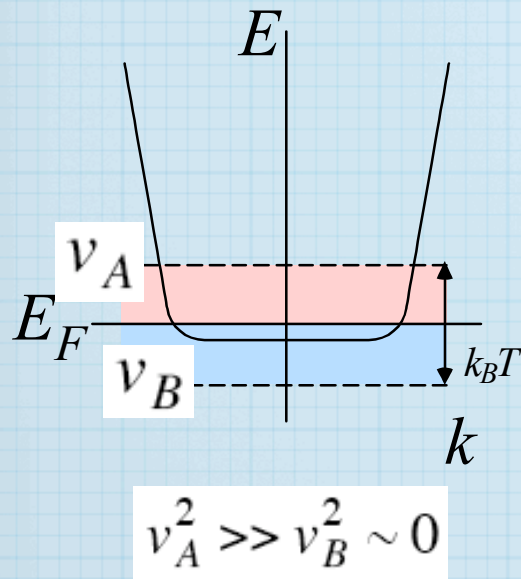
$$K_1 \sim k_B T (v_A^2 - v_B^2)$$

# “Pudding Mold” Band Drives Large Thermopower in $\text{Na}_x\text{CoO}_2$

triangular lattice

Kazuhiko KUROKI and Ryotaro ARITA<sup>1</sup>

Journal of the Physical Society of Japan  
Vol. 76, No. 8, August, 2007, 083707



Large Fermi surface

$$\sigma \propto v_A^2 + v_B^2 \quad \text{large}$$

Highly asymmetric band

$$PF = S^2 \sigma$$

large

$$S \propto \frac{v_A^2 - v_B^2}{v_A^2 + v_B^2} \quad \text{large}$$

Boltzmann's  
transport

$$\sigma = e^2 K_0$$

$$S = \frac{1}{eT} \frac{K_1}{K_0}$$

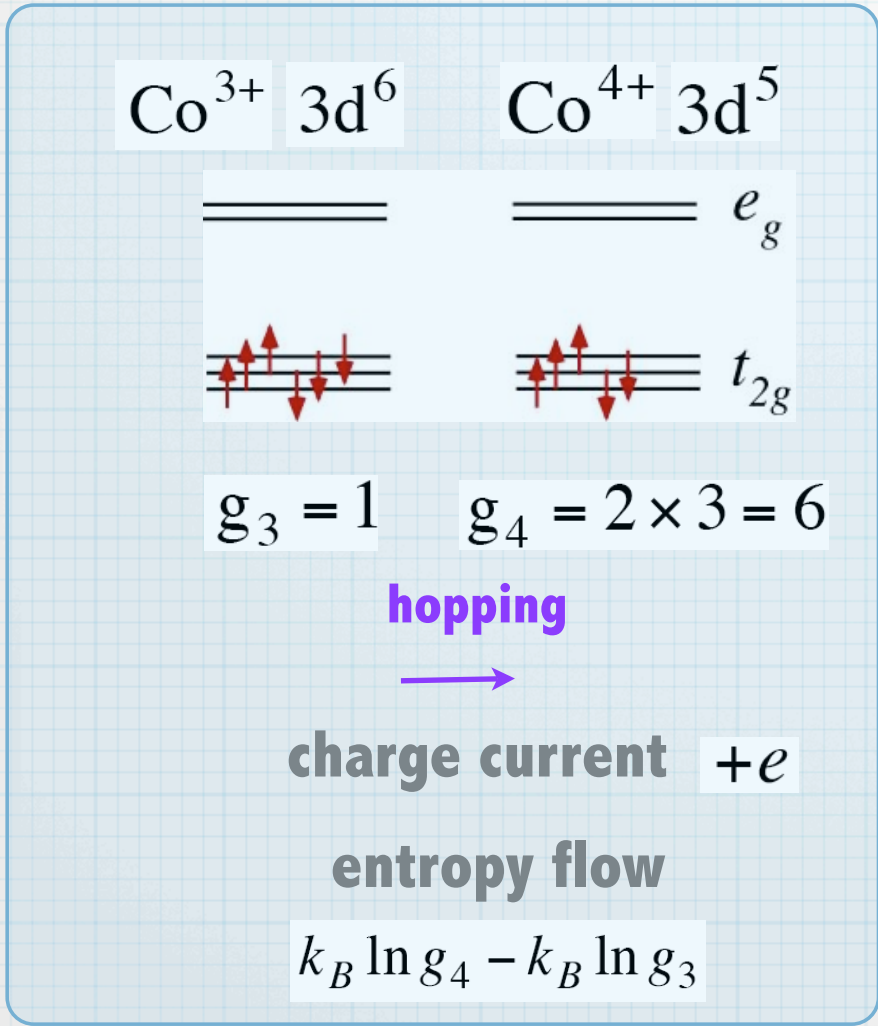
$$K_n = \sum_k \tau(k) v(k) v(k) \left[ -\frac{\partial f}{\partial E} \right] (E_k - \mu)^n$$

$$K_0 \sim (v_A^2 + v_B^2)$$

$$K_1 \sim k_B T (v_A^2 - v_B^2)$$

**Effects of Spin and Orbital Degeneracy on the Thermopower of Strongly Correlated Systems**

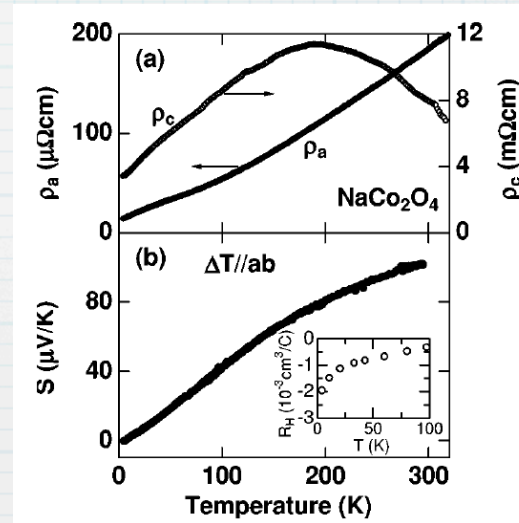
W. Koshibae and S. Maekawa



**Extended Heikes eq.**

$$S = \frac{k_B}{e} (\ln g_4 - \ln g_3) = 154 \mu\text{V/K}$$

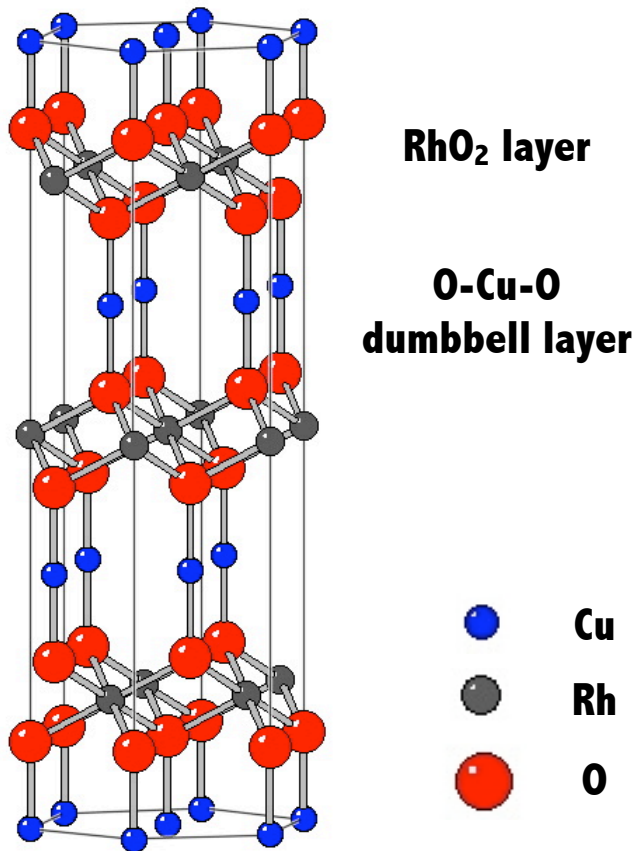
**High-T limit / hopping conduction**





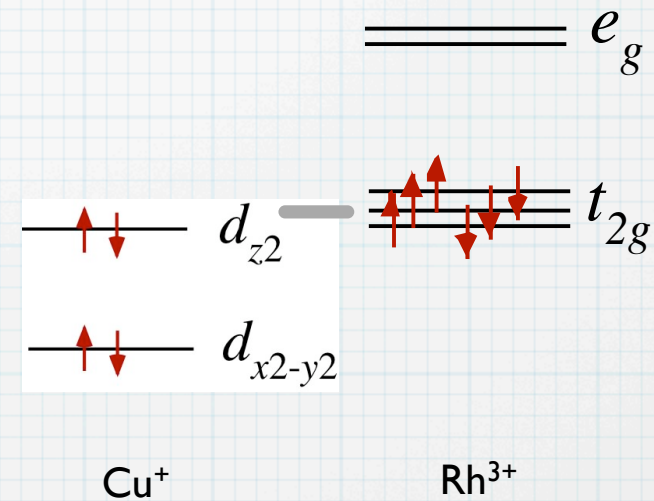
# Layered Rh oxides with $d^6$ low-spin state

## Delafossite $\text{CuRhO}_2$

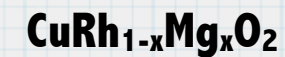


## Band insulator

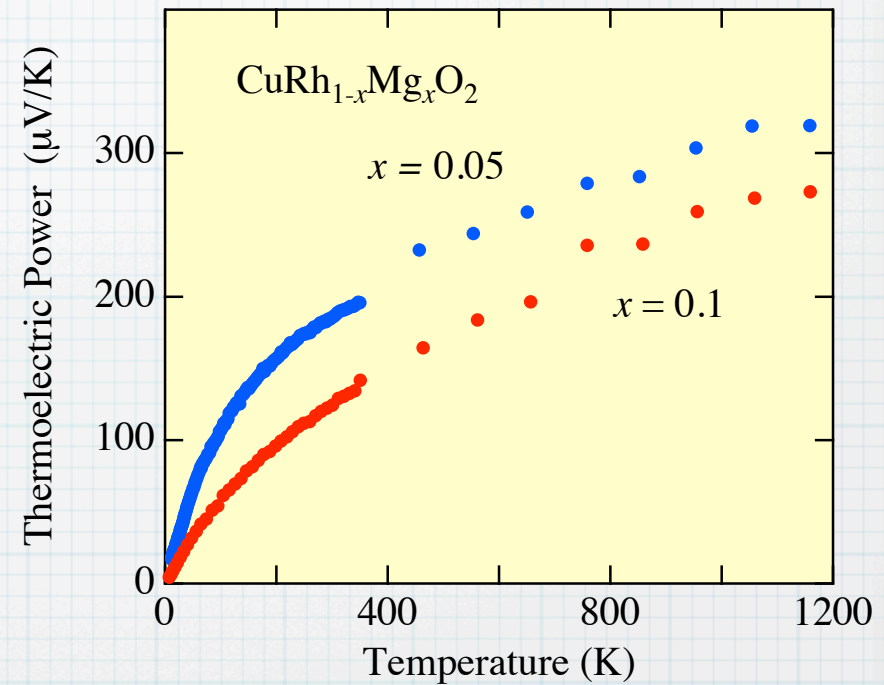
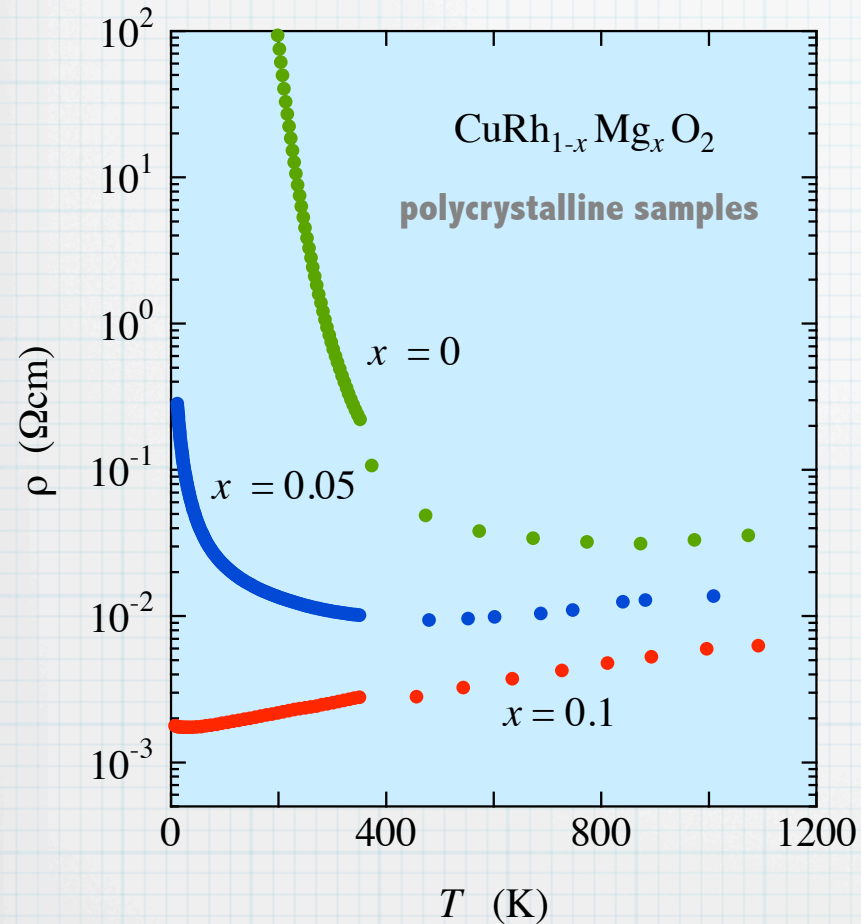
\*  $d^6$  low-spin state



Hole doping by substituting  $\text{Mg}^{2+}$  for  $\text{Rh}^{3+}$



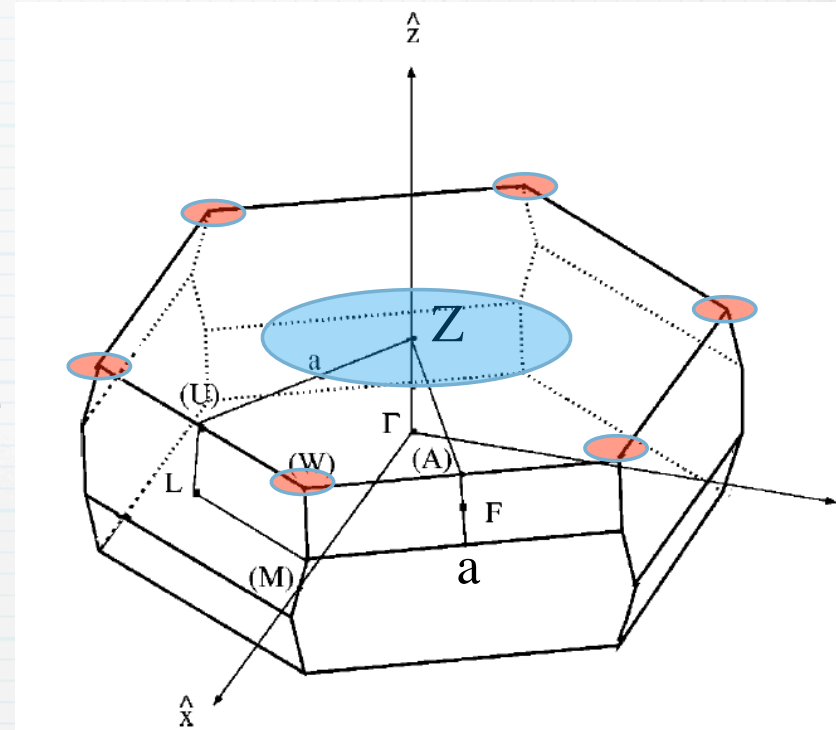
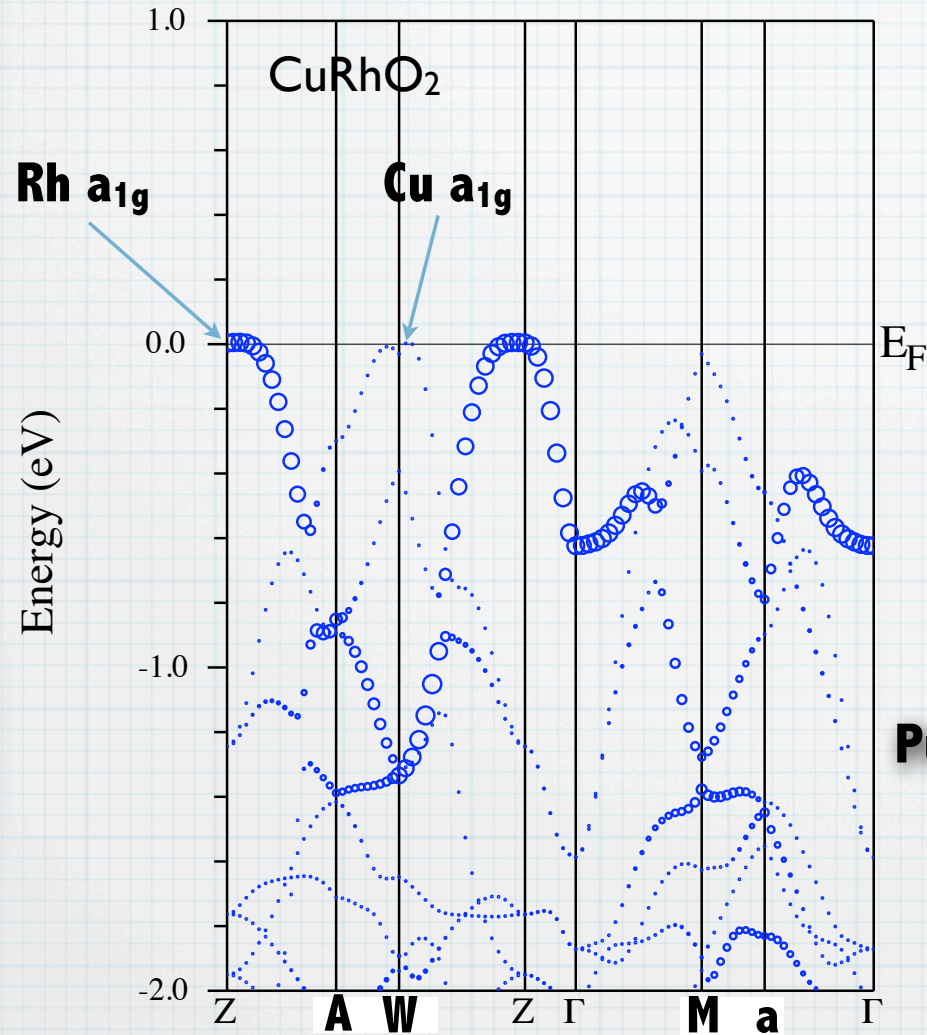
# Large Seebeck and Metallic Conductivity Realized



**Large Mg solubility of  $x = 0.1$ .**

**Large mobility of  $\sim 1 \text{ cm}^2/\text{Vs}$ .**

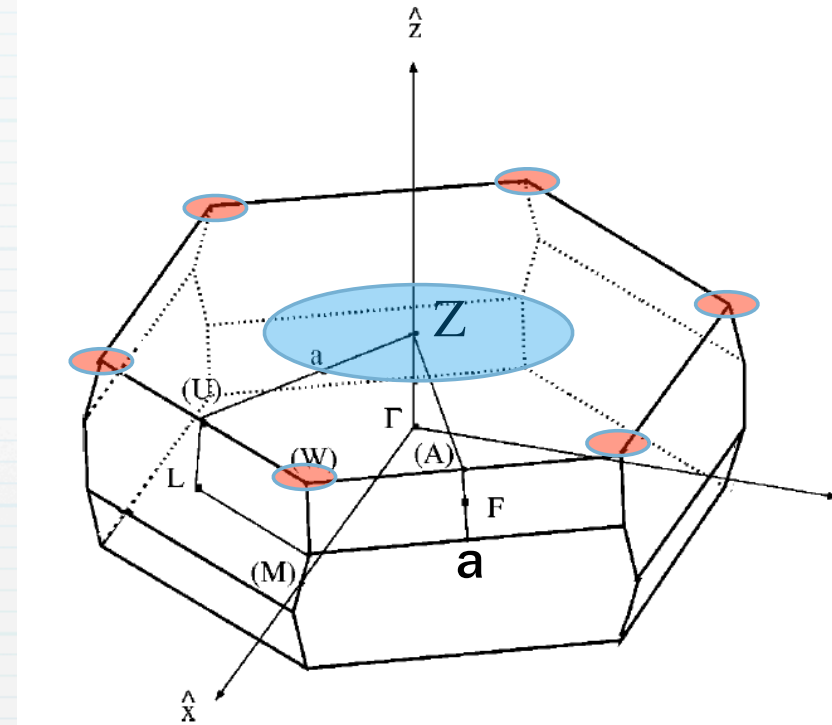
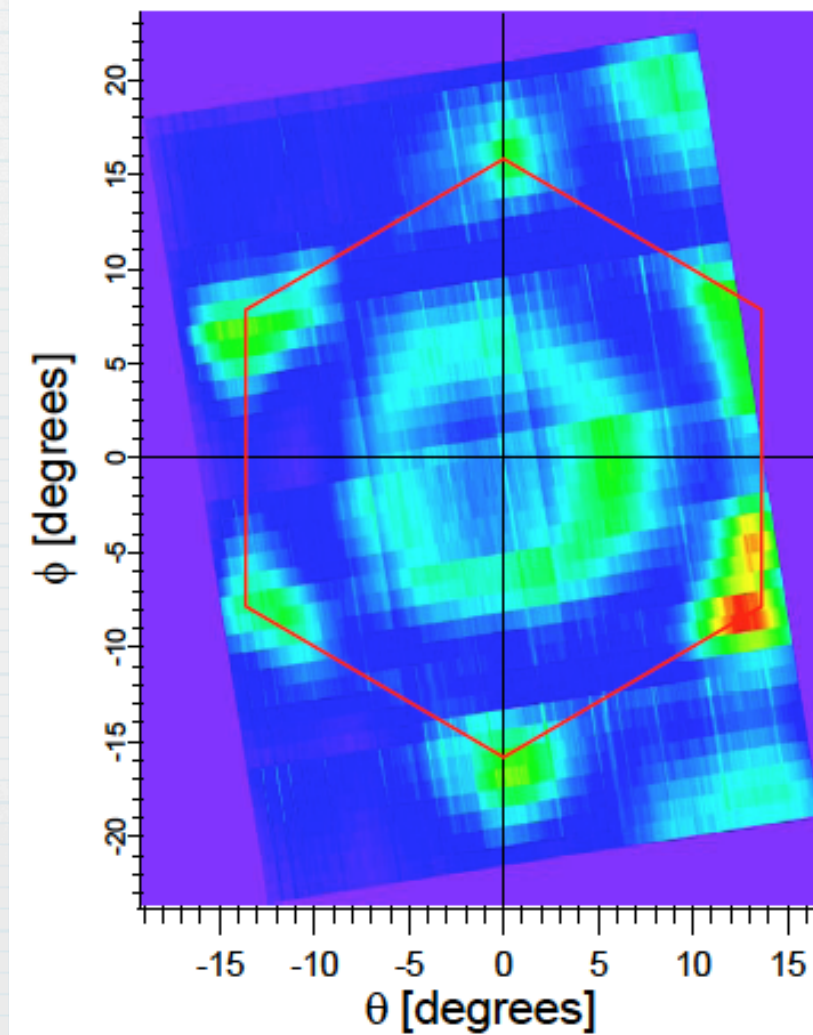
# “Pudding Mold Band” is present at Z point



**Pudding Mold Band of Rh a<sub>1g</sub> centered at Z**

Pocket of Cu a<sub>1g</sub> centered at W

# “Pudding Mold Band” is present at Z point

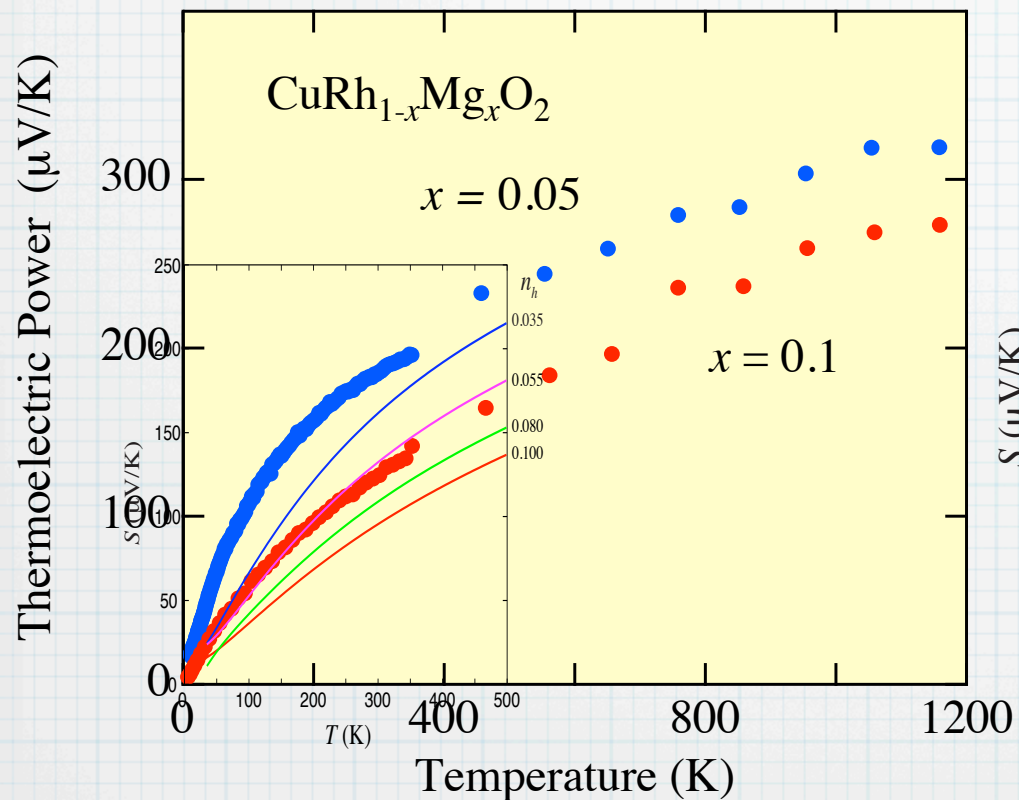


$h\nu = 100 \text{ eV}$   
 $T = 18 \text{ K}$

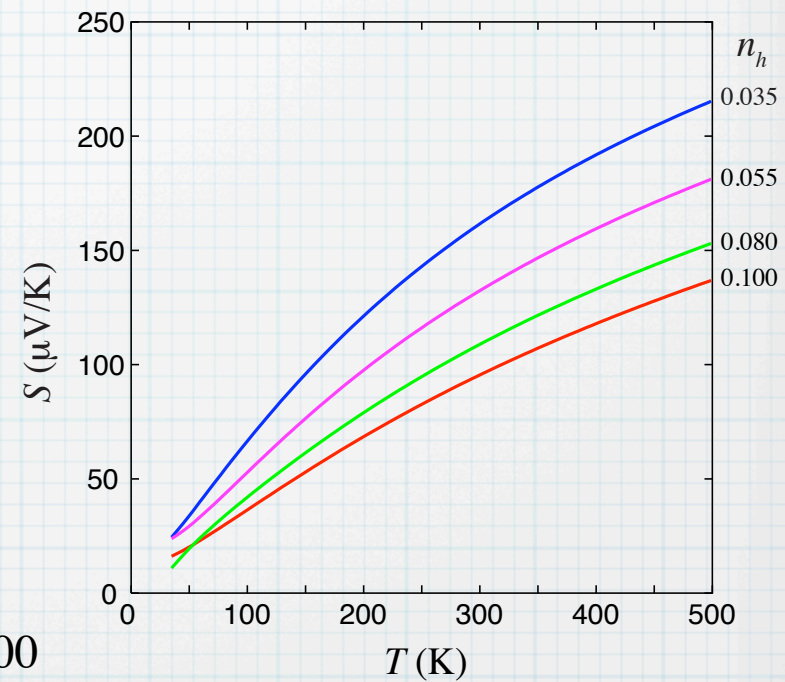
SRC-Wisconsin  
collaboration with N. Bontemps  
(Paris)

# “Pudding Mold Band” scenario looks OK

Observation



calculation

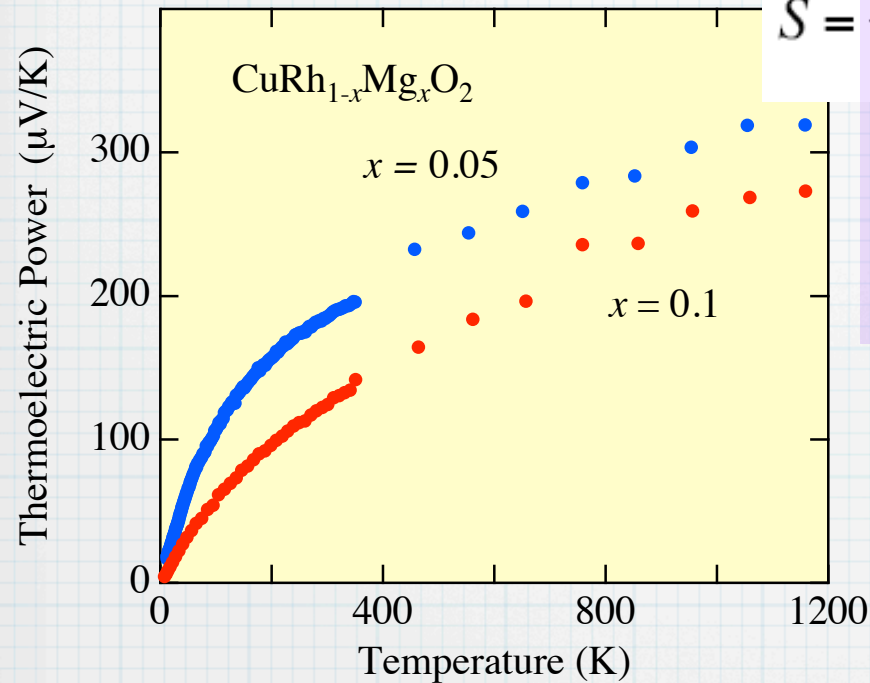


Kuroki & Arita



# Spin & Orbital Scenario predicts High-T value of S

(Heikes)



$$S = \frac{k_B}{e} (\ln g_4 - \ln g_3) - \frac{k_B}{e} \ln \frac{x}{1-x}$$

**Spin & Orbital entropy**

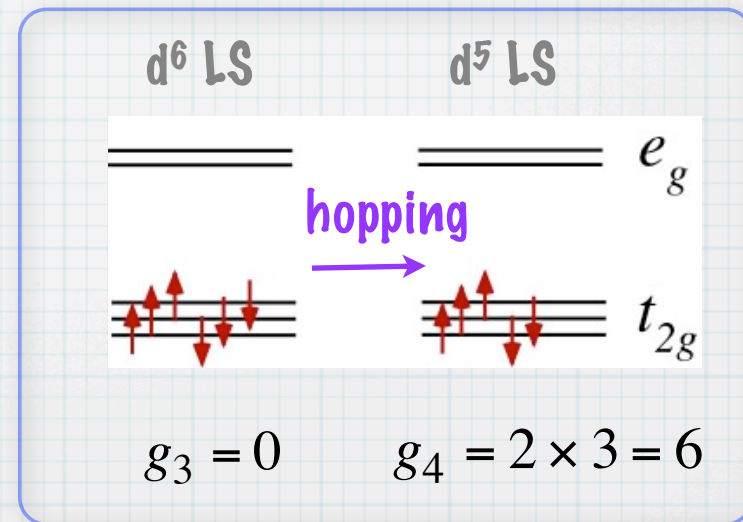
+154  $\mu\text{V/K}$

**Charge configuration entropy**

+190  $\mu\text{V/K}$  for  $x = 0.1$

**High T limit**

$$S \rightarrow 344 \mu\text{V/K}$$



Koshibae et al. Phys. Rev. Lett. 87 (2001) 236603.

# “In-between-state” is ubiquitous theme in strongly correlated systems

$$S = \frac{1}{eT} \frac{K_0}{K_1} + \frac{\mu}{eT}$$

kinetic term

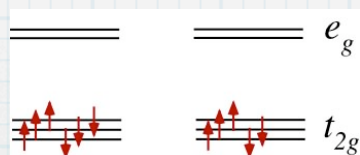
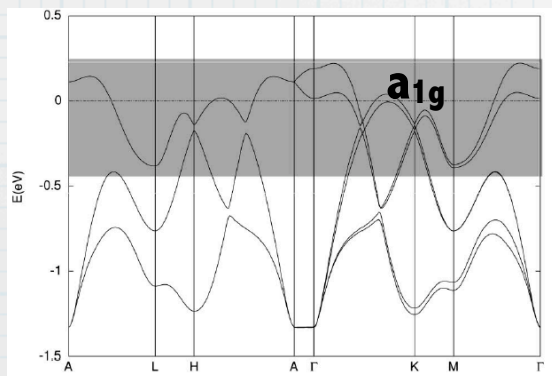
entropy term

Band limit

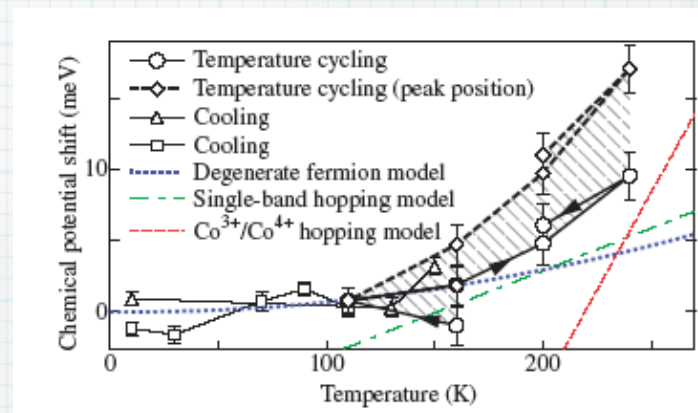
Atomic limit

QP band  
better described  
in k space

Hubbard band  
better described  
in real space



$\text{Na}_x\text{CoO}_2$

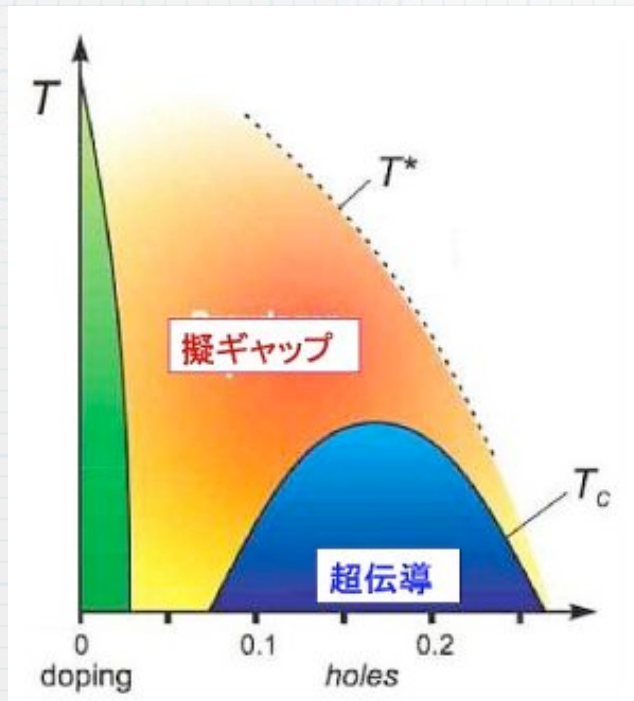


Crossover between band limit  
& Atomic limit by PES

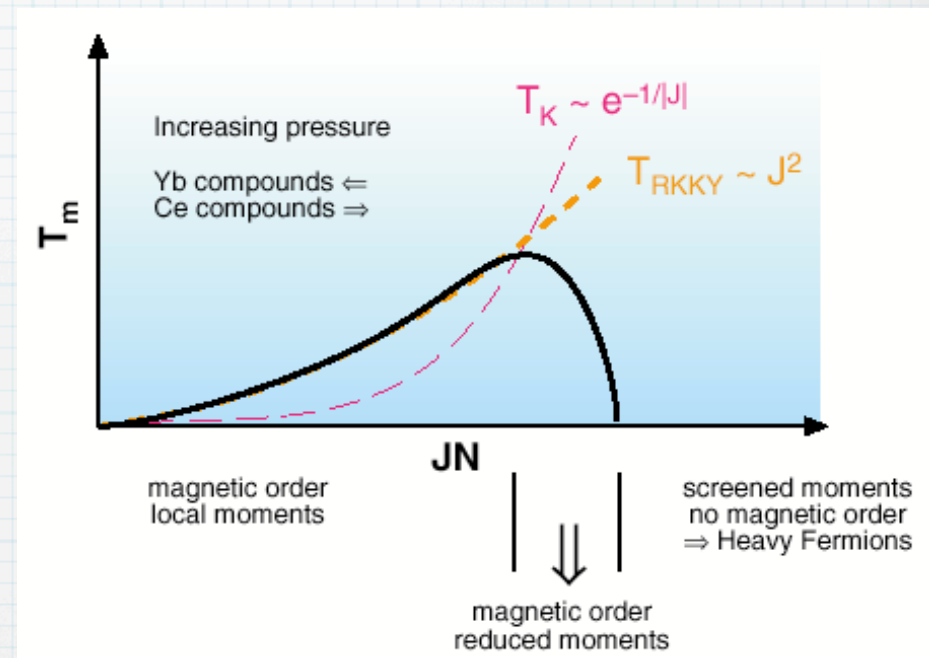
Isida & Fujimori, JPSJ 76, 103709  
(2007).

# “In-between-state” is ubiquitous theme in strongly correlated systems

d-electron system: high- $T_c$



f-electron systems: heavy fermion



Atomic limit

Band limit

Atomic limit

Band limit

Mott Physics

Fermi Liq. & SCR

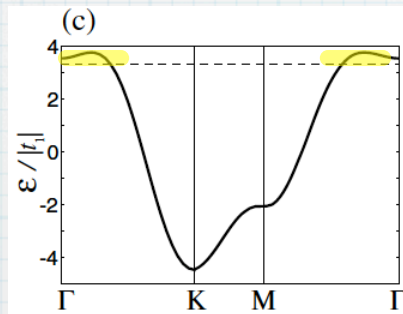
localized f

delocalized f

# Conclusion

Geometrical Frustration

Band limit



“pudding-mold band”

single band tight binding model

Kuroki & Arita, JPSJ 76, 083707 (2007).

Atomic limit



spin/orbital  
degeneracy

\* physics of “in-between-state”

\* material design from  
geometrical frustration

High-entropy metal (thermoelectric materials)