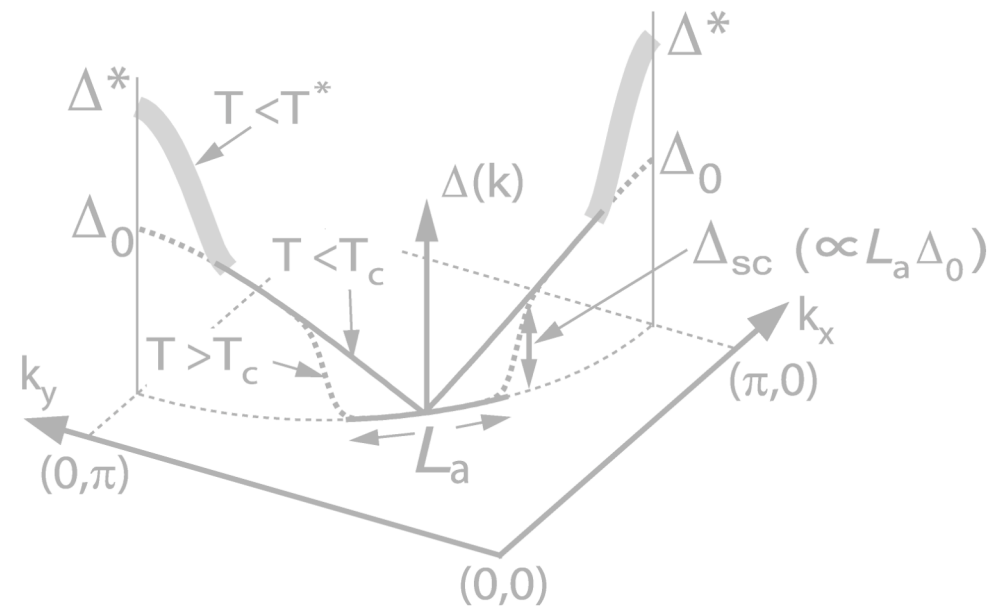
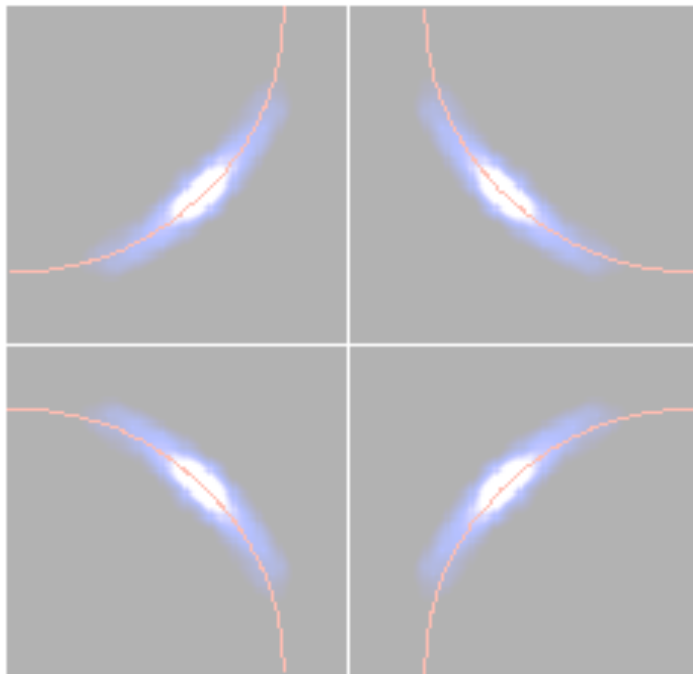


# Angle-resolved photoemission spectroscopy of high-temperature superconductors: Present status and outlook

Atsushi Fujimori  
University of Tokyo



# Collaborators

T. Yoshida, S. Ideta, M. Hashimoto, M. Ikeda, W. Malaeb (Univ. of Tokyo)

K. Tanaka, X.-J. Zhou, D.H. Lu, Z.-X. Shen (Stanford Univ.)

Z. Hussain, W.L. Yang (Advanced Light Source)

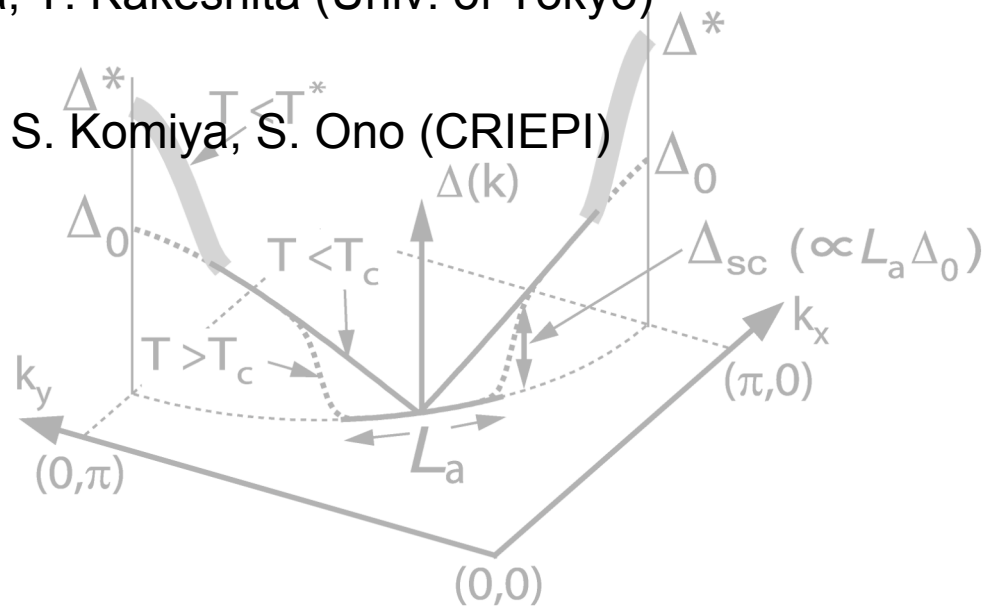
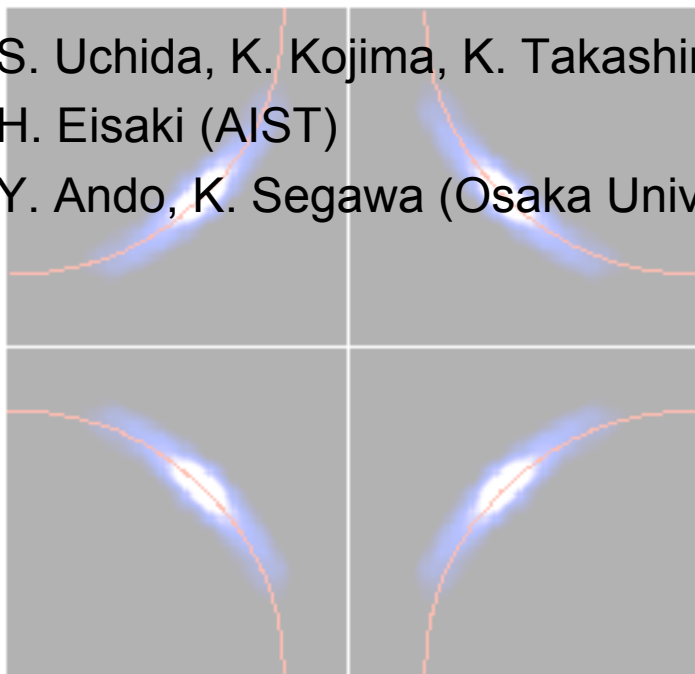
K. Ono, M. Kubota (KEK-PF)

A. Ino, M. Arita, H. Namatame, M. Taniguchi (HiSOR, Hiroshima Univ.)

S. Uchida, K. Kojima, K. Takashima, T. Kakeshita (Univ. of Tokyo)

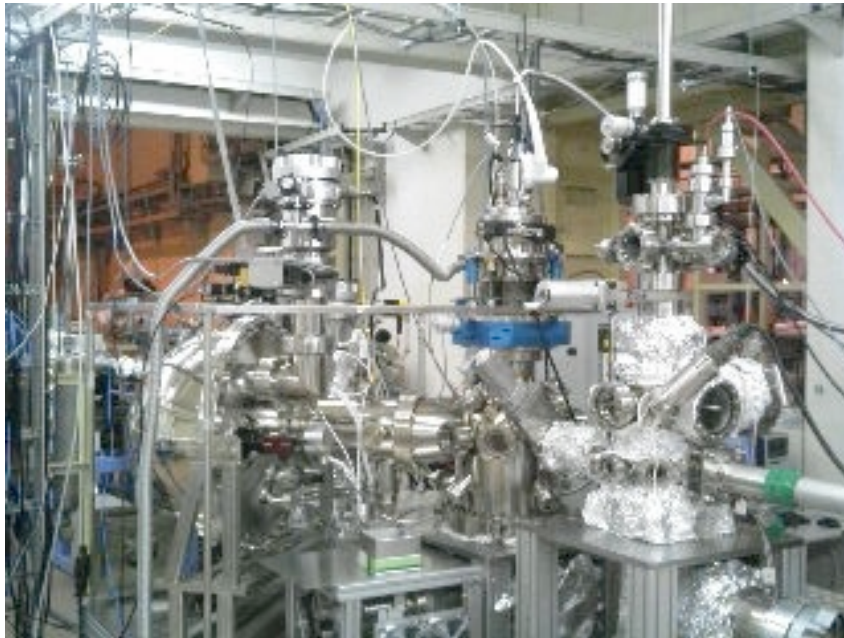
H. Eisaki (AIST)

Y. Ando, K. Segawa (Osaka Univ.), S. Komiya, S. Ono (CRIEPI)



# High-resolution ARPES station BL-28A at Photon Factory

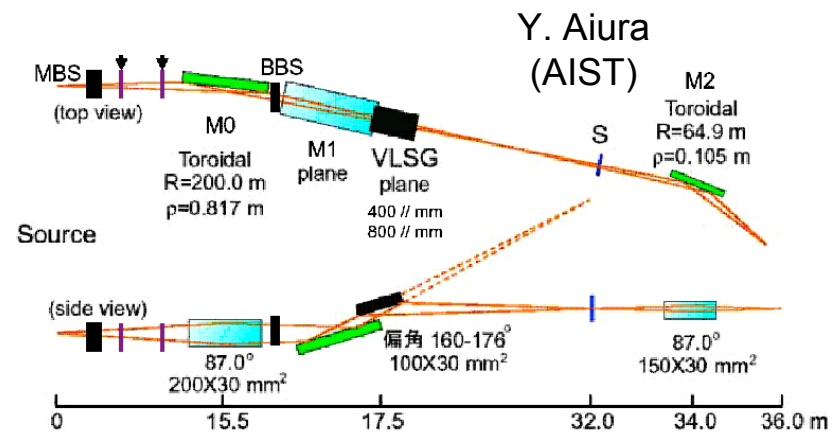
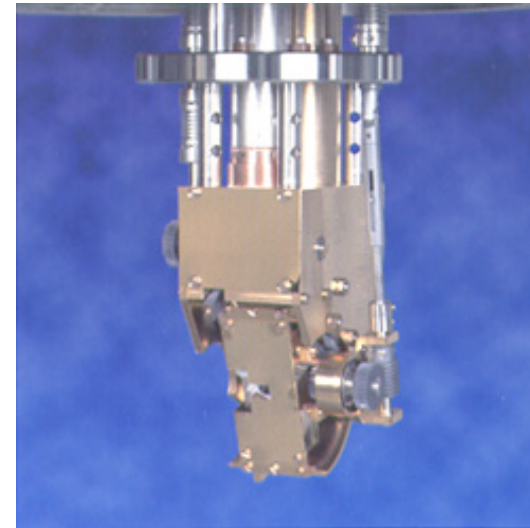
ARPES endstation



Staff: K. Ono, M. Kubota, N. Kamakura (KEK-PF)  
User group: A. Fujimori, T. Takahashi, Y. Aiura,  
T. Saitoh, K. Ozawa, ....

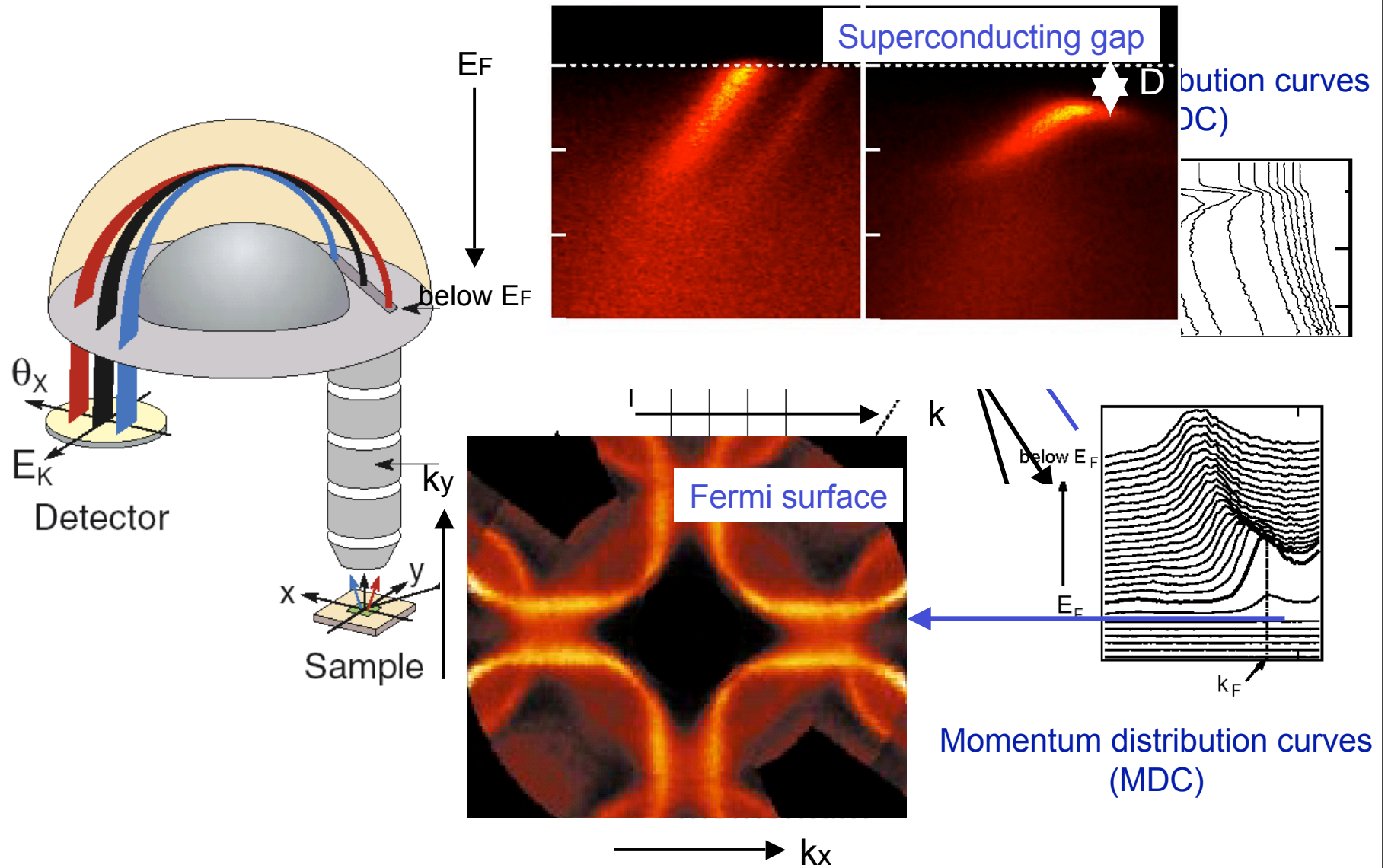
$hn = 35\text{-}200\text{ eV}$

Sample manipulator with two-axis rotation



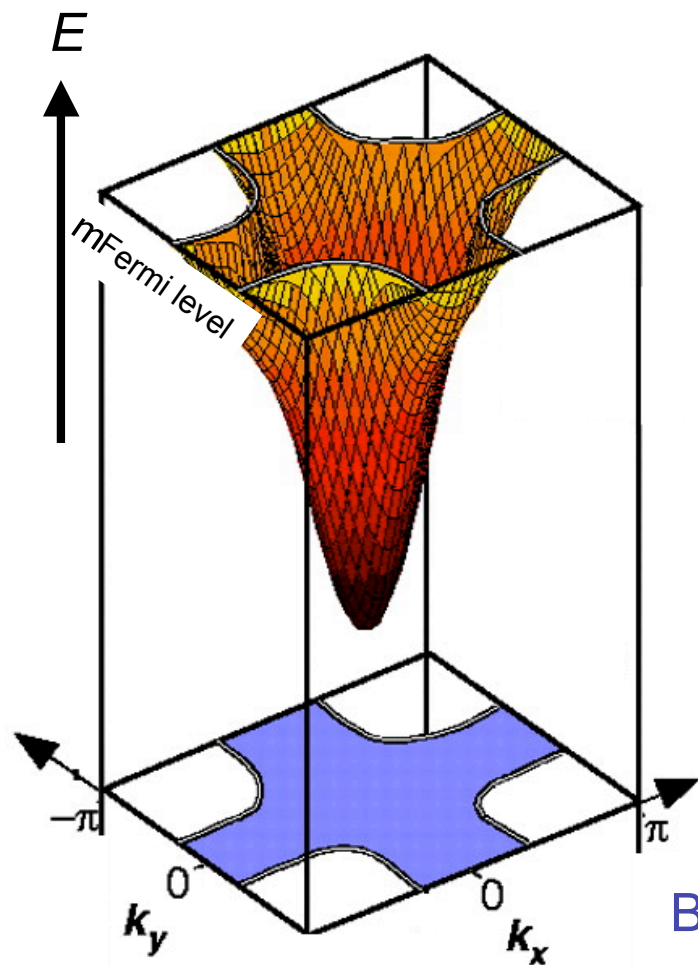
K. Amemiya (KEK-PF)

# Angle-Resolved Photoemission Spectroscopy (ARPES)

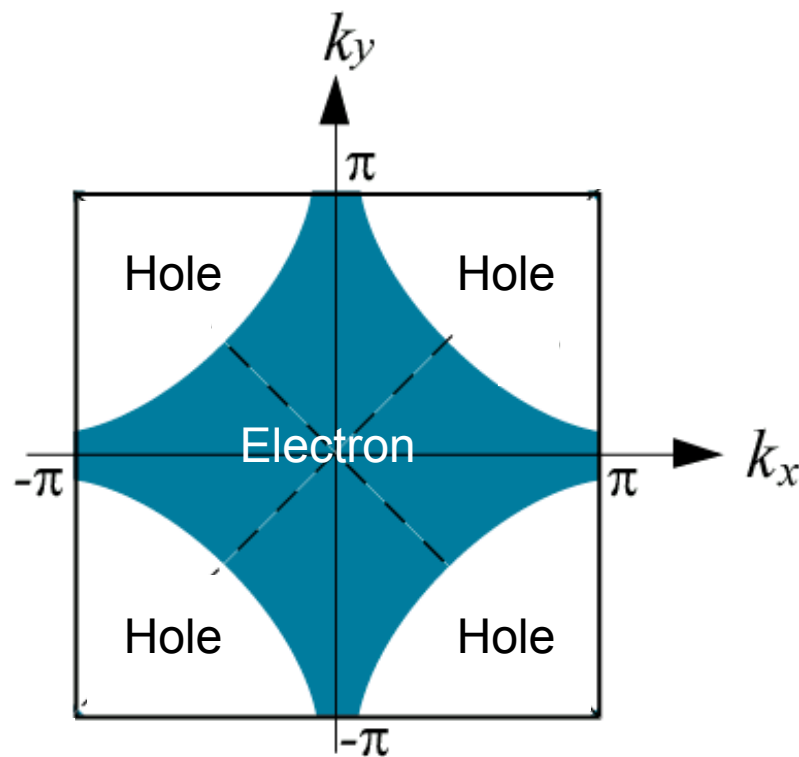


# Band structure and Fermi surface in high- $T_C$ cuprates

Band dispersion



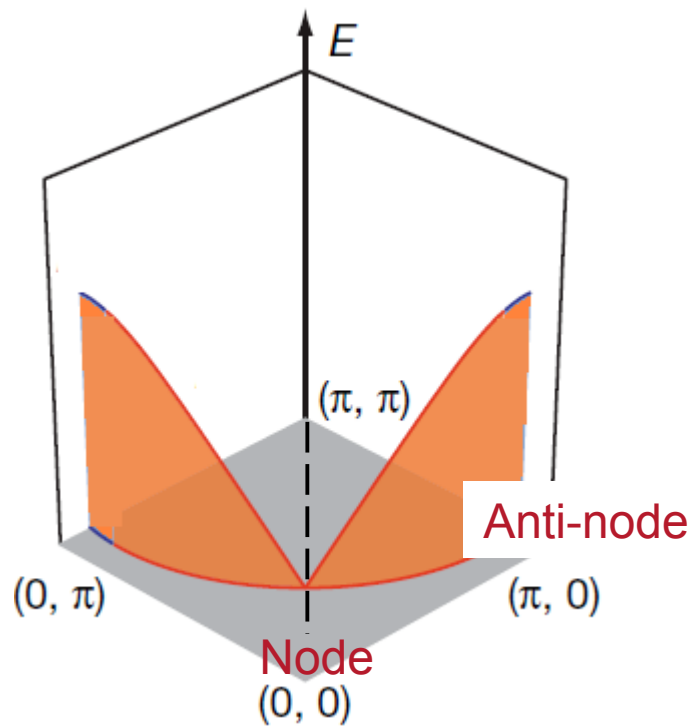
Fermi surface



$$\text{Band structure: } E(\mathbf{k}) = -2t(\cos k_x a + \cos k_y a) - 4t' \cos k_x a \cos k_y a - 2t''(\cos 2k_x a + \cos 2k_y a)$$

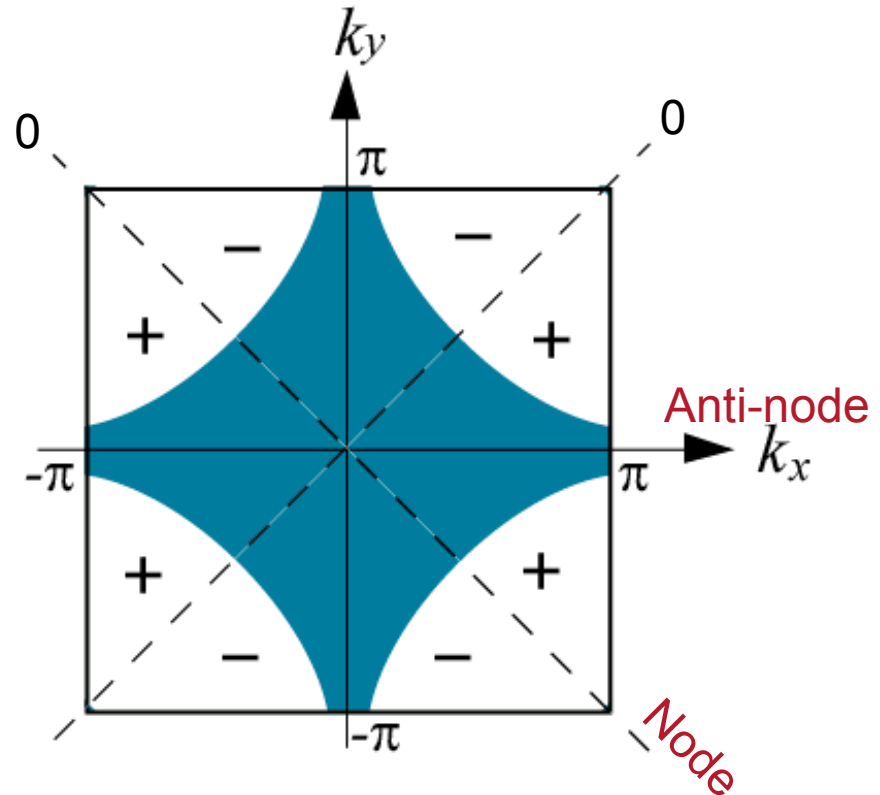
# **d-wave superconducting gap in high- $T_C$ cuprates**

d-wave superconducting gap



$d_{x^2-y^2}$  symmetry

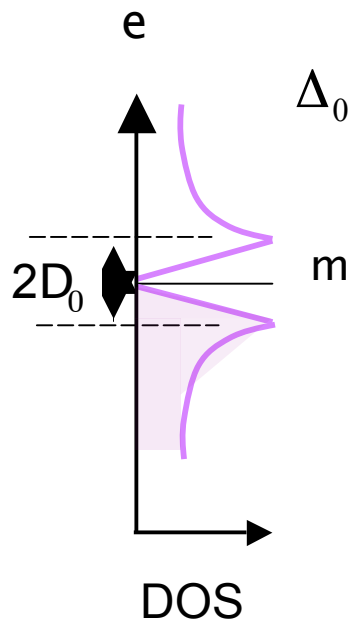
d-wave order parameter



Order parameter  
 $D(\mathbf{k}) = D_0(\cos k_x a - \cos k_y a)$

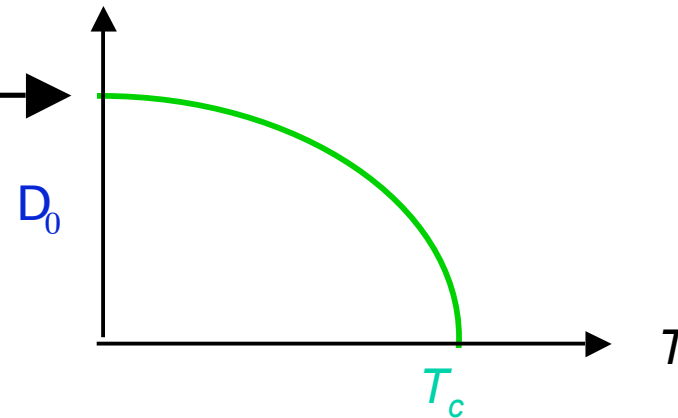
# BCS theory of *d*-wave superconductor

Density of states

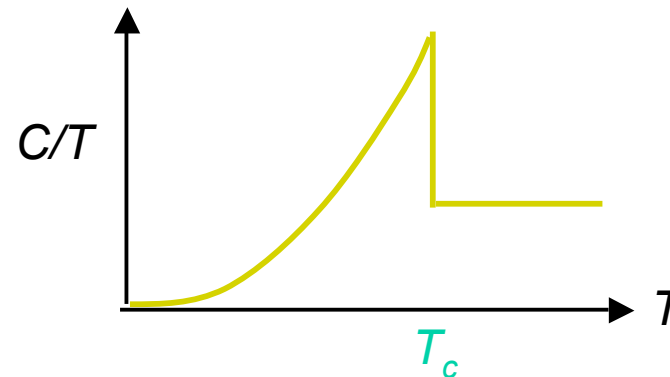


$$\Delta_0(0) = \frac{4.3k_B T_c}{2}$$

Superconducting gap  $D_0(T)$



Electronic specific heat

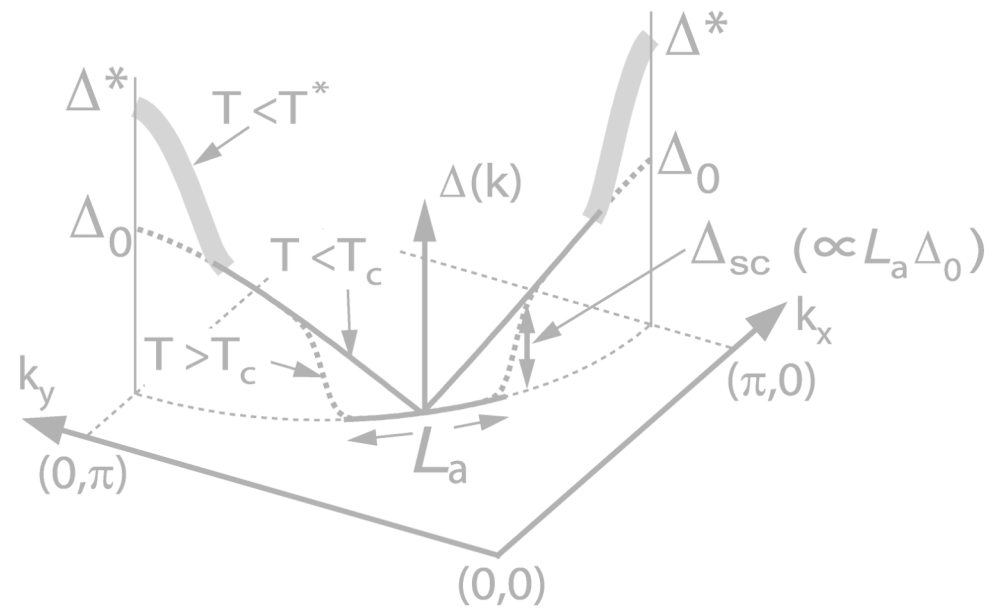
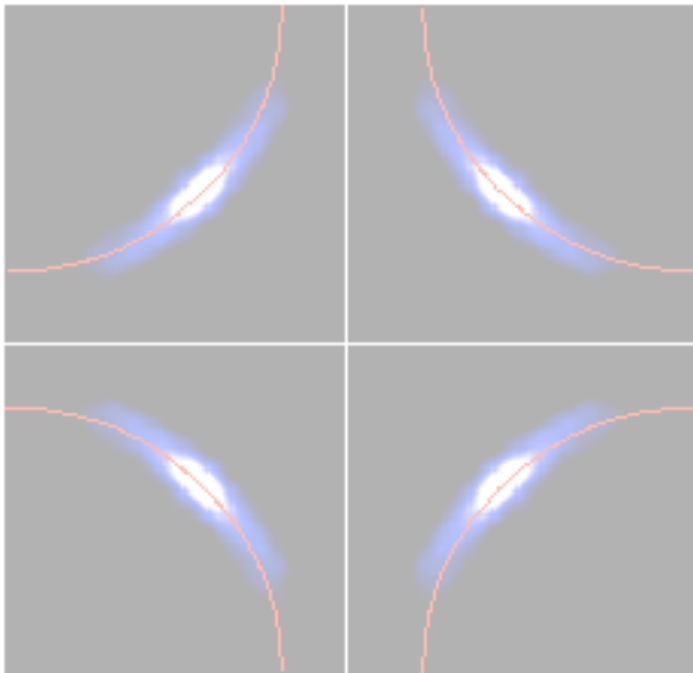


$$D(\mathbf{k}) = D_0(\cos k_x a - \cos k_y a)$$

Superfluid density  
= Fermi surface volume/ $m^*$

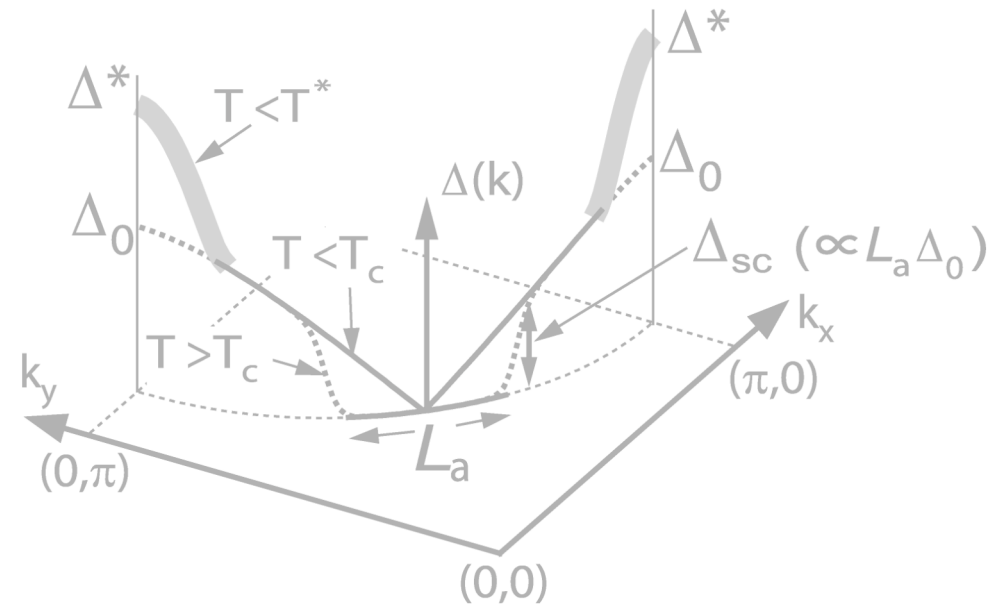
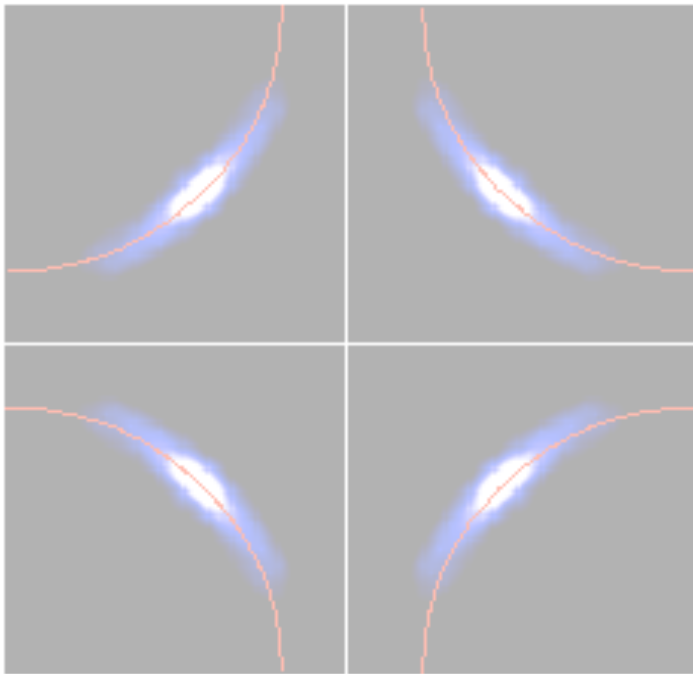
# Outline

- Pseudogap, Fermi arc and superconducting gap
- Coupling of electron to Boson excitations



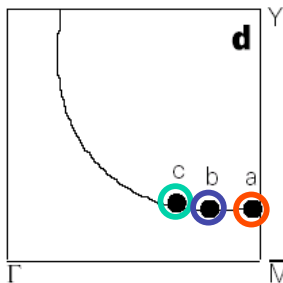
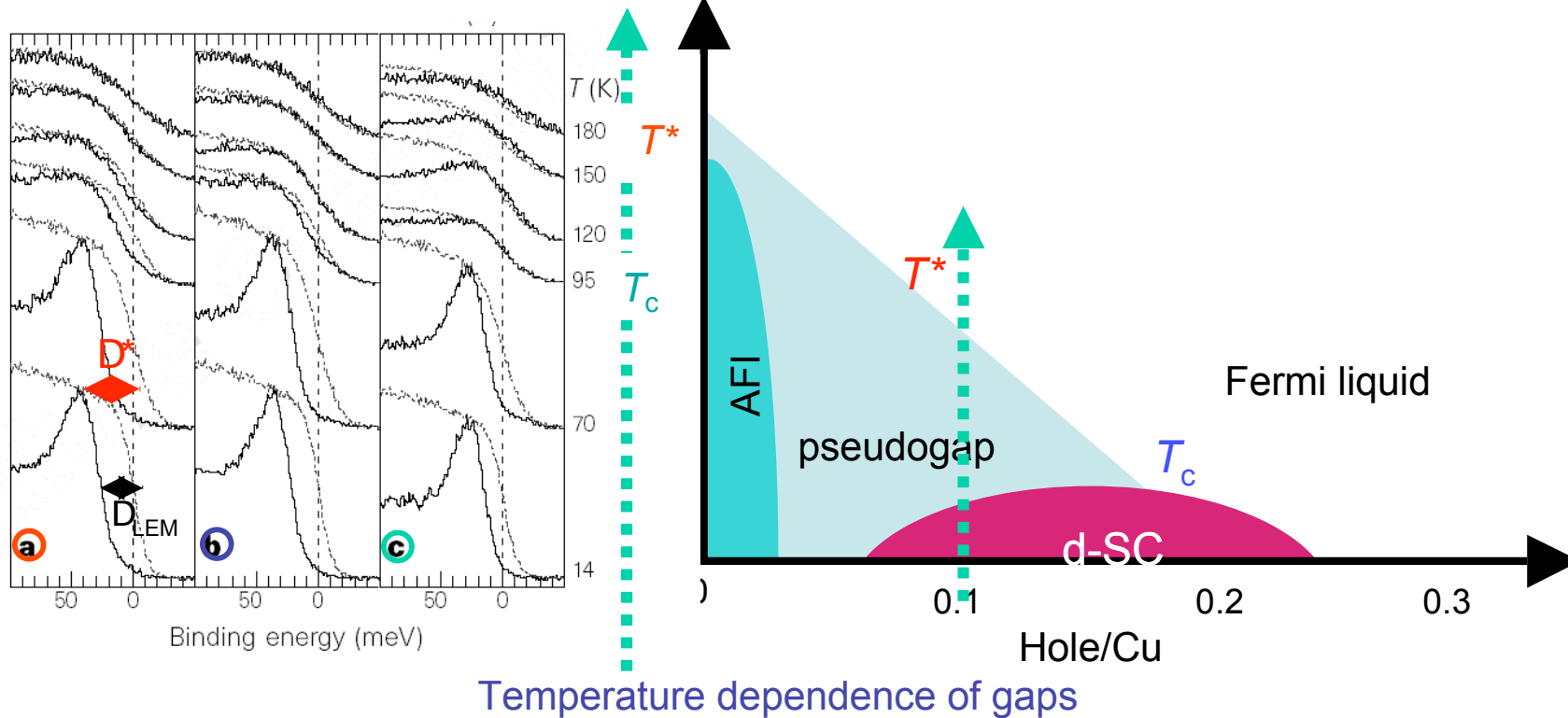


# Pseudogap, Fermi arc and superconducting gap



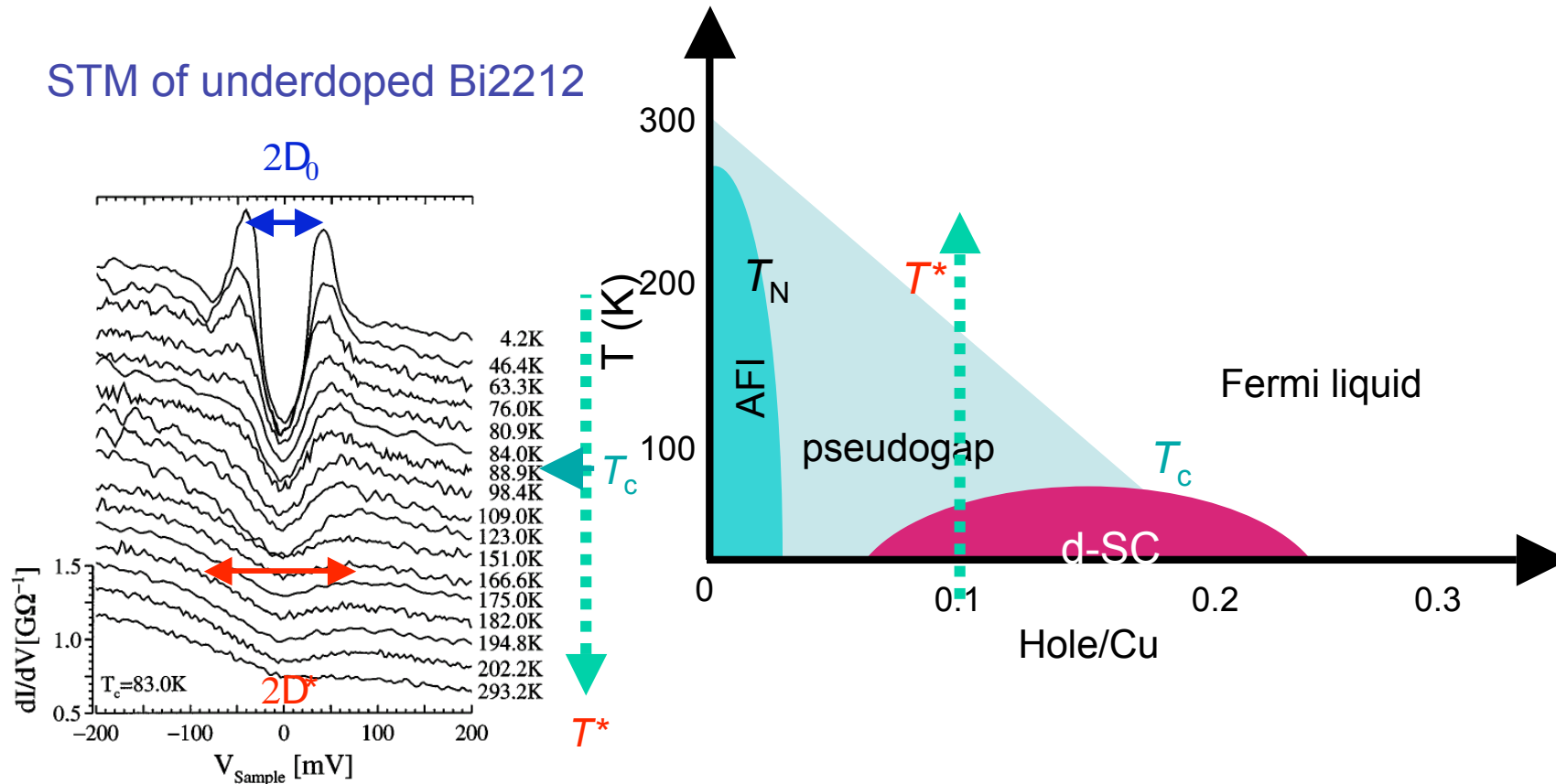
# Temperature-dependent pseudogap opening

ARPES of underdoped Bi2212



M. R. Norman et al. Nature '98

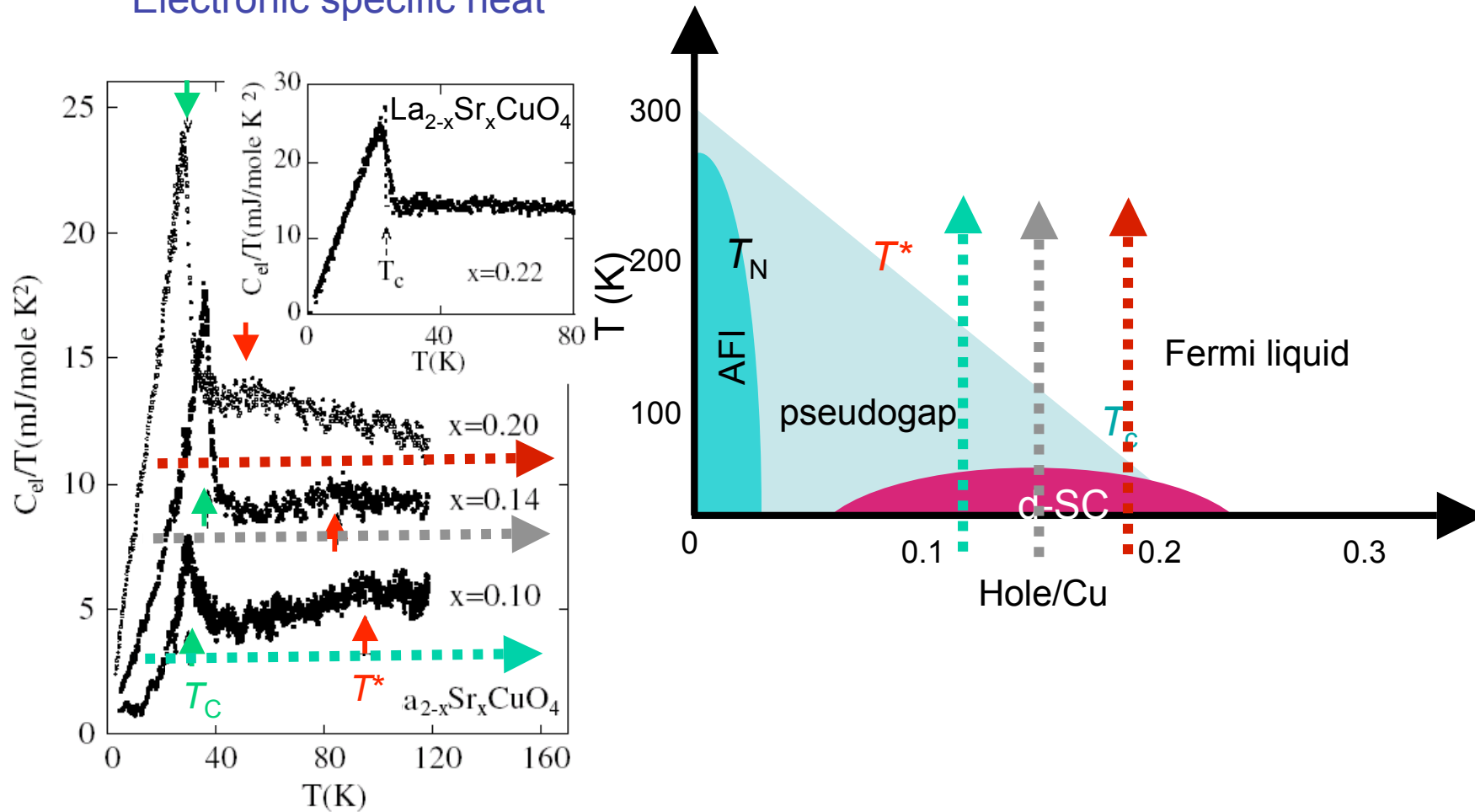
# Temperature-dependent pseudogap opening



Ch. Renner et al., PRL, '98

# Temperature-dependent pseudogap opening

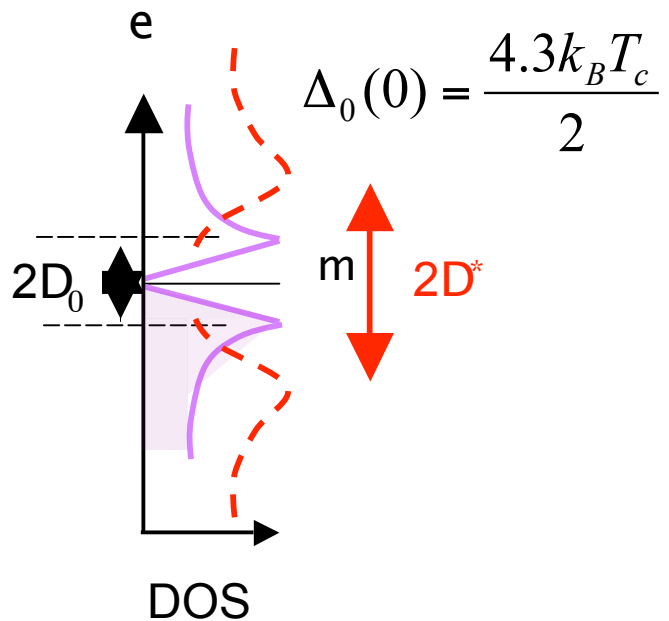
Electronic specific heat



N. Momono et al., JPSJ '02  
 J. Loram et al., Physica C

# Pseudogap phenomena in high- $T_c$ cuprates

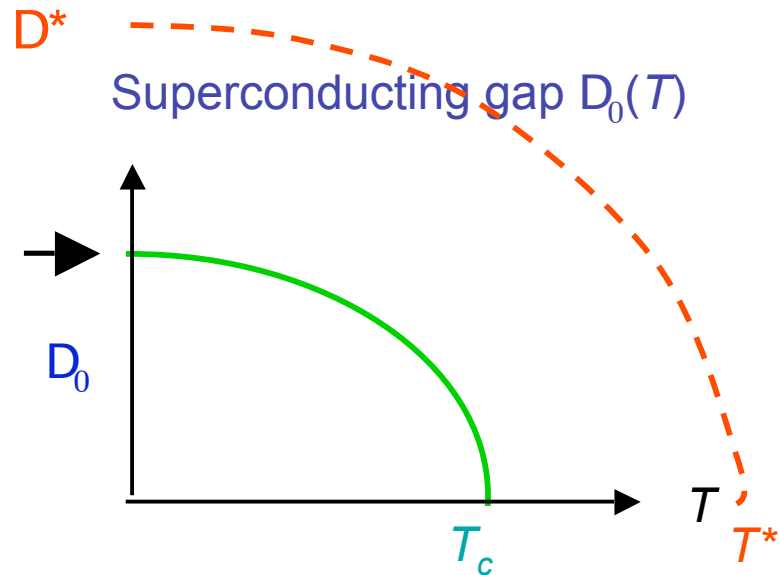
Density of states



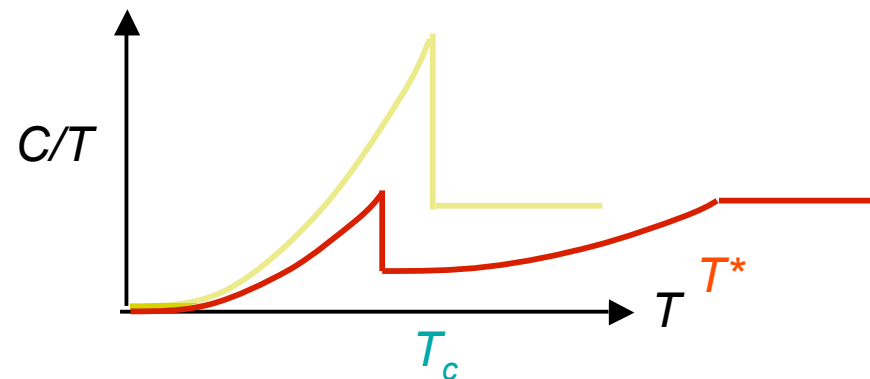
$$D(\mathbf{k}) = D_0(\cos k_x a - \cos k_y a)$$

Superfluid density  
 $\ll$  Fermi surface volume/ $m^*$

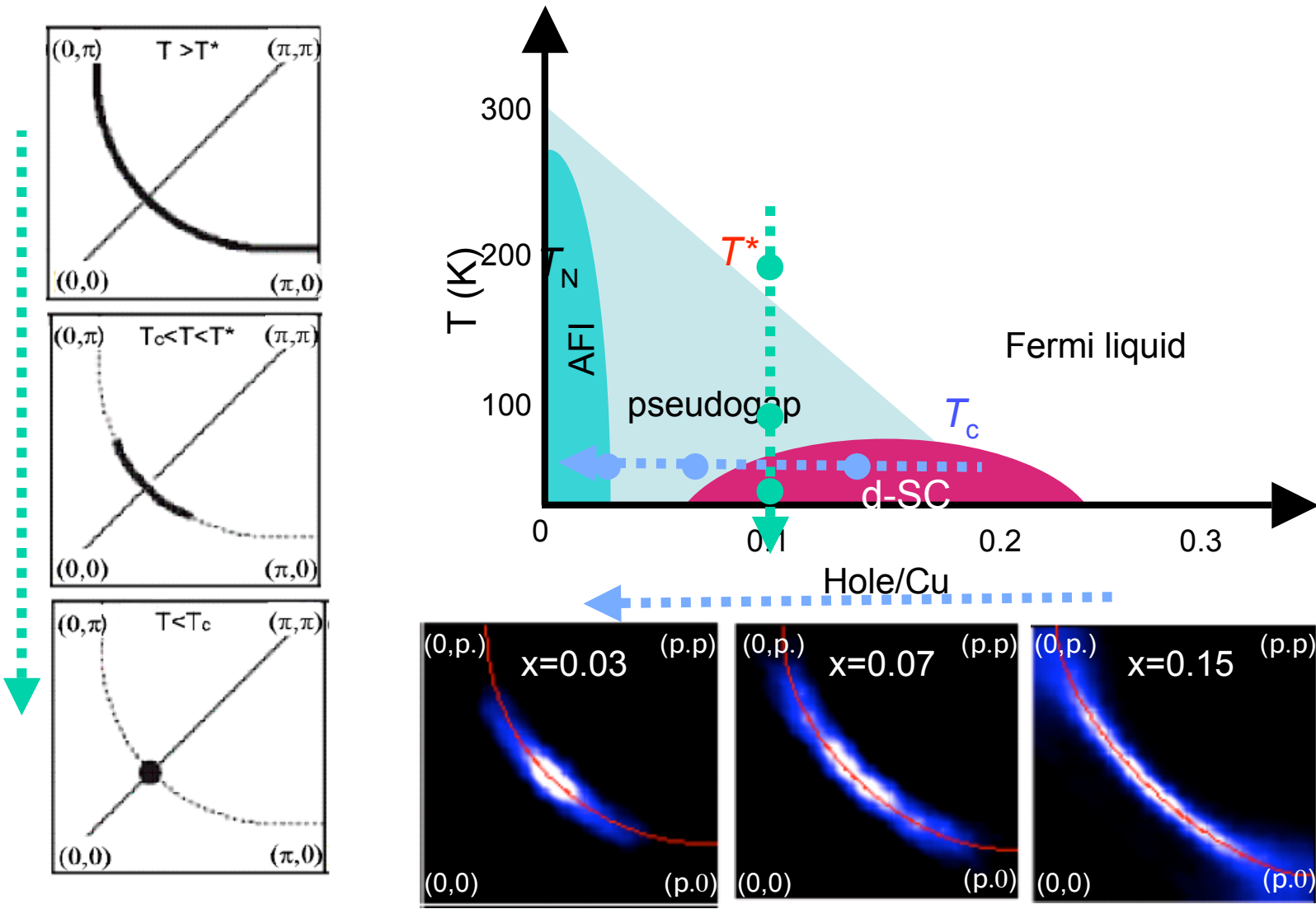
$\propto T_c$ : Uemura relation



Electronic specific heat



# Pseudogap opening and Fermi "arc" formation

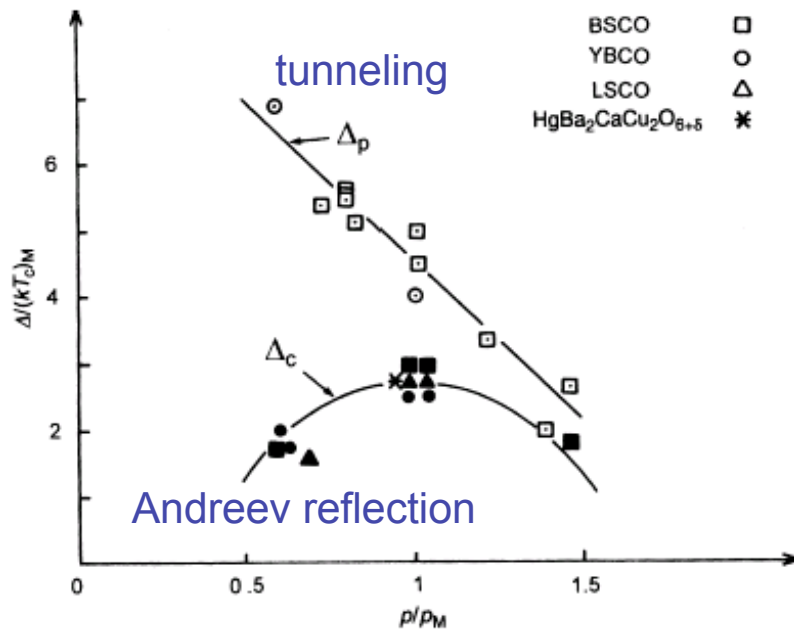


M. R. Norman et al. Nature '98

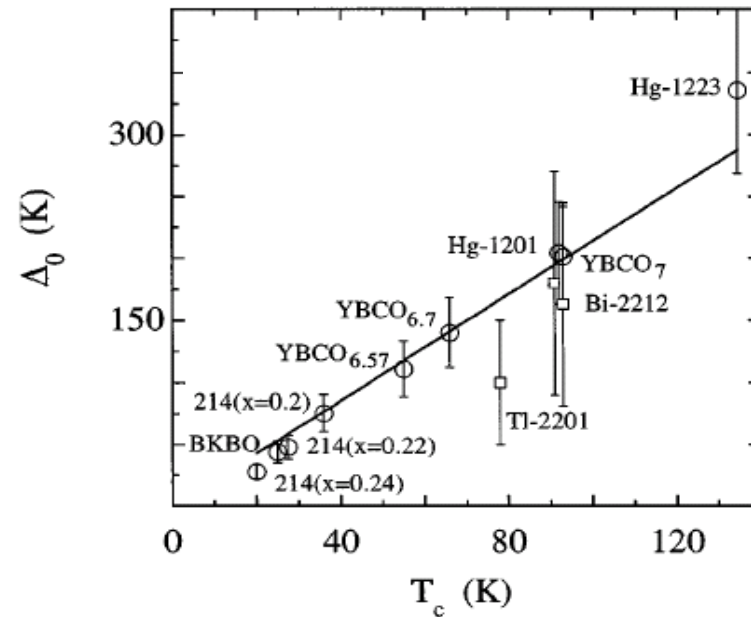
T. Yoshida et al., PRB'06

# Distinct superconducting gap and pseudogap?

Andreev reflection



Common measurements of penetration depth



$$\frac{\lambda_{ab}^2(0)}{\lambda_{ab}^2(T)} \approx 1 - \frac{(2 \ln 2)T}{\Delta_0}$$

$$D(\mathbf{k}) \equiv D_0(\cos k_x a - \cos k_y a)$$

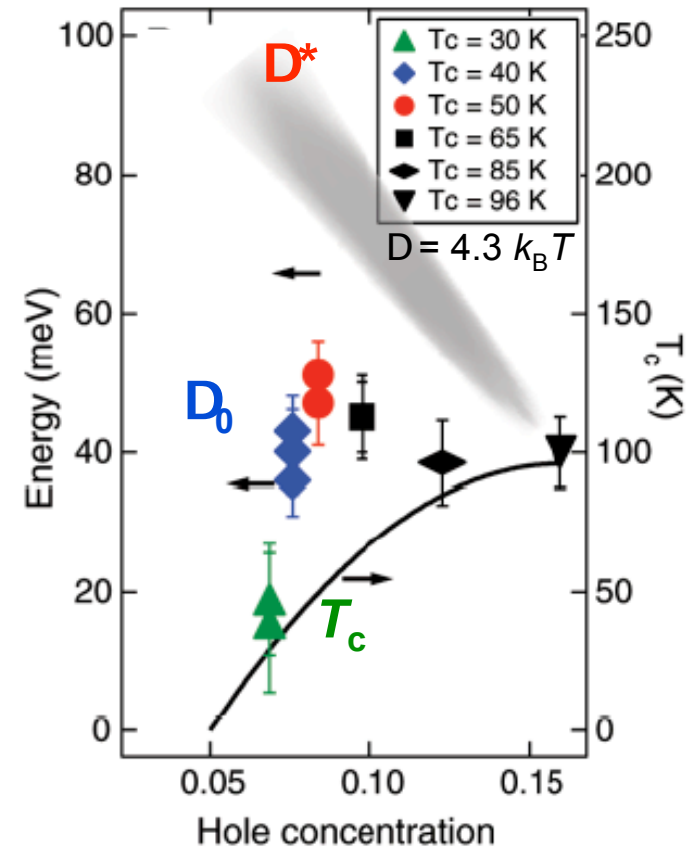
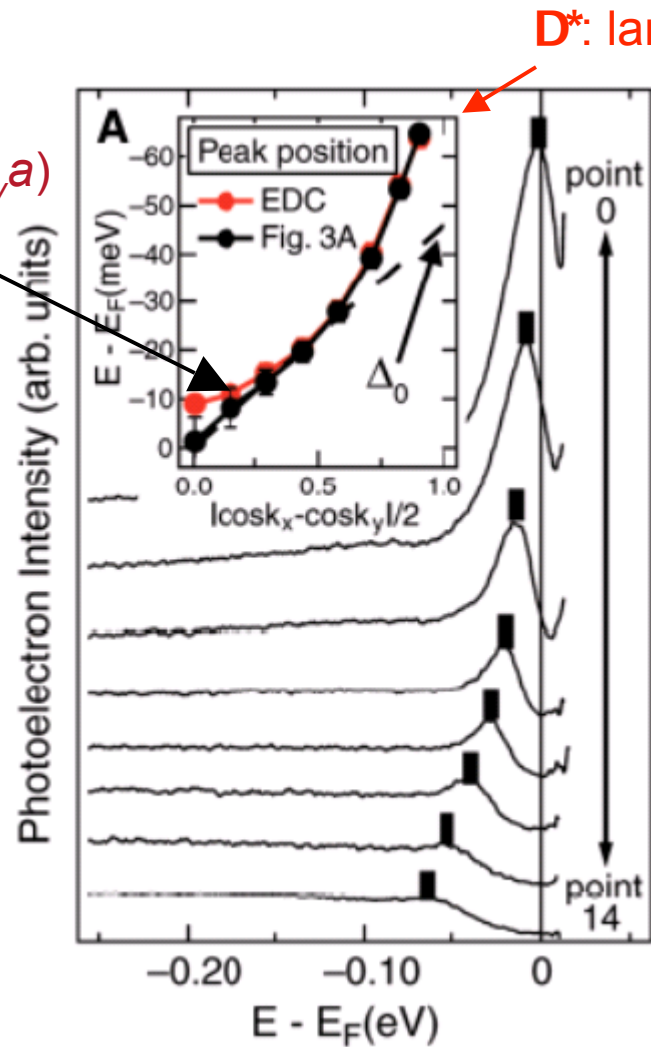
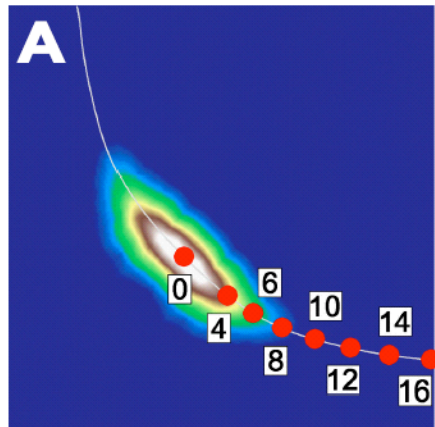
G. Deutcher, Nature '99

C. Panagopoulos, PRL '98

# Two gap energy scales $D^*$ and $D_0$ in underdoped Bi2212

$D(\mathbf{k}) = D_0(\cos k_x a - \cos k_y a)$   
near node

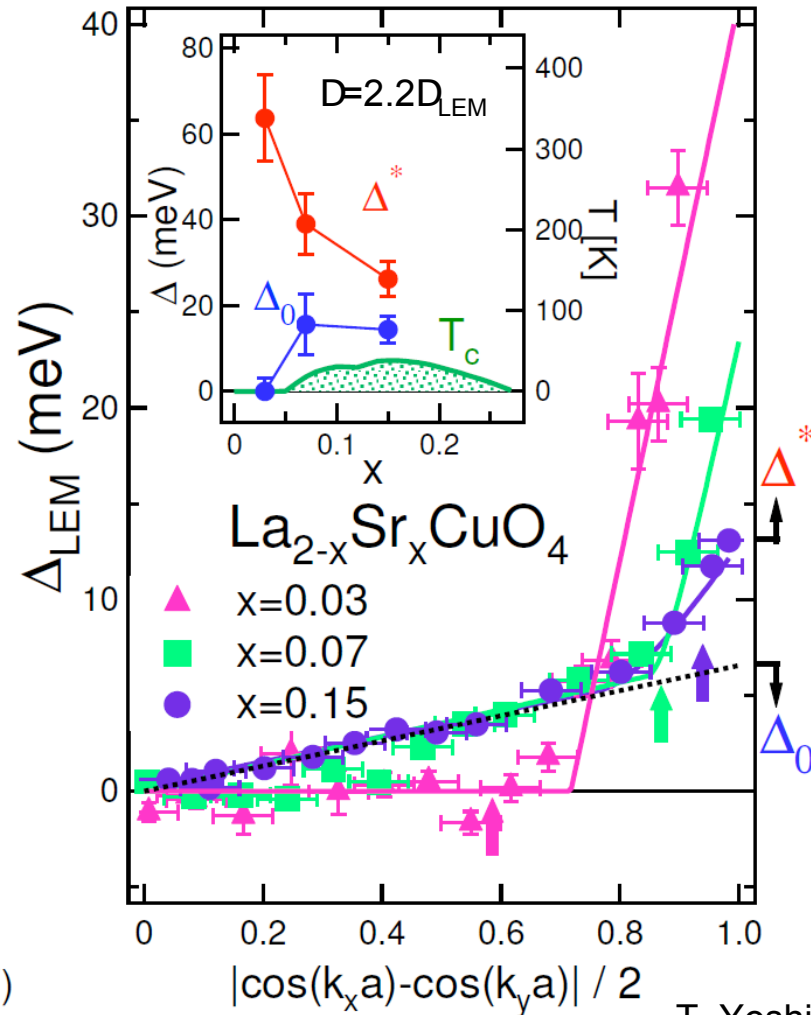
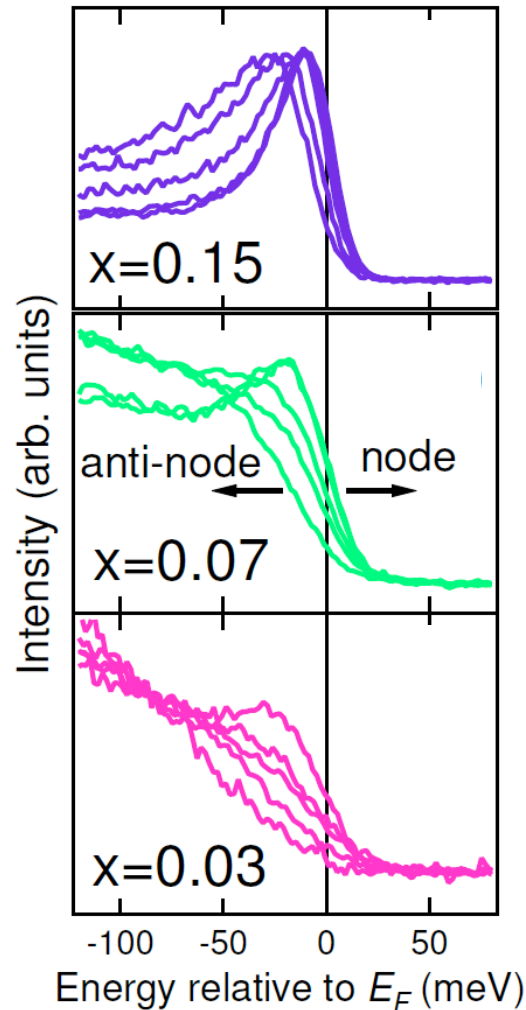
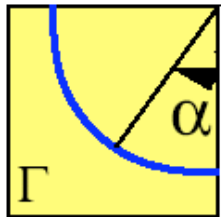
$D^*$ : larger gap near (p,0)





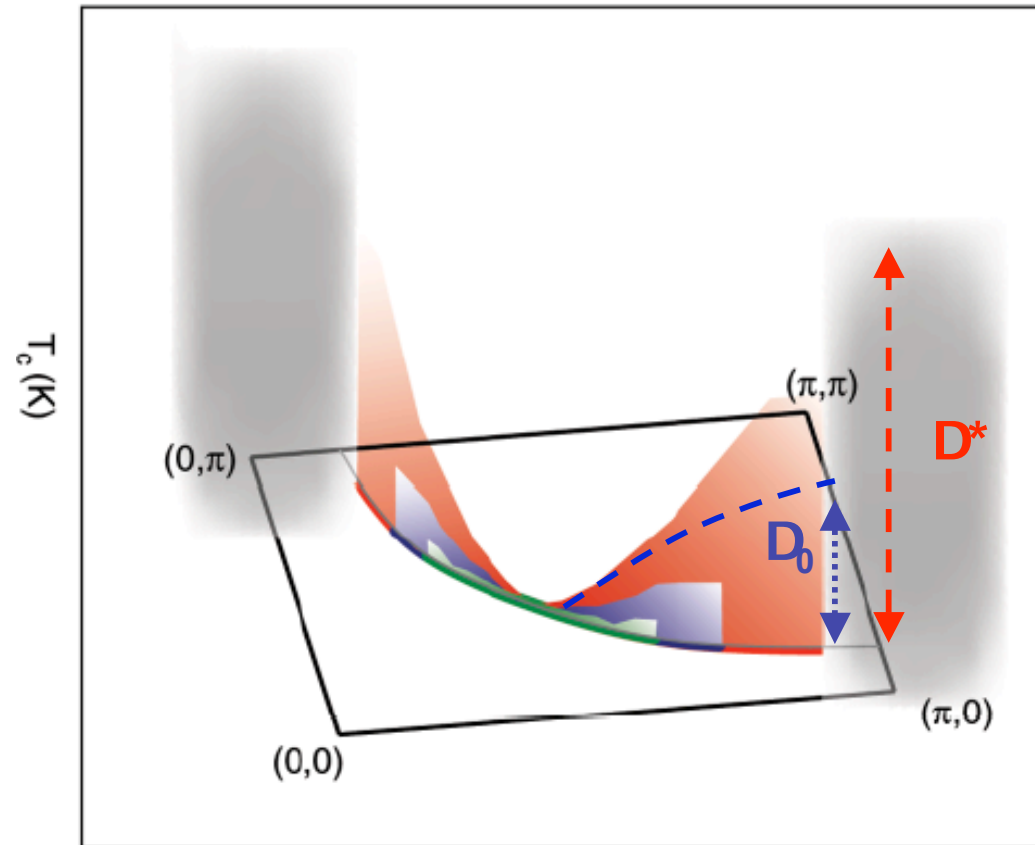
# Two gap energy scales $D^*$ and $D_0$ in underdoped $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$

ARPES spectra on Fermi surface



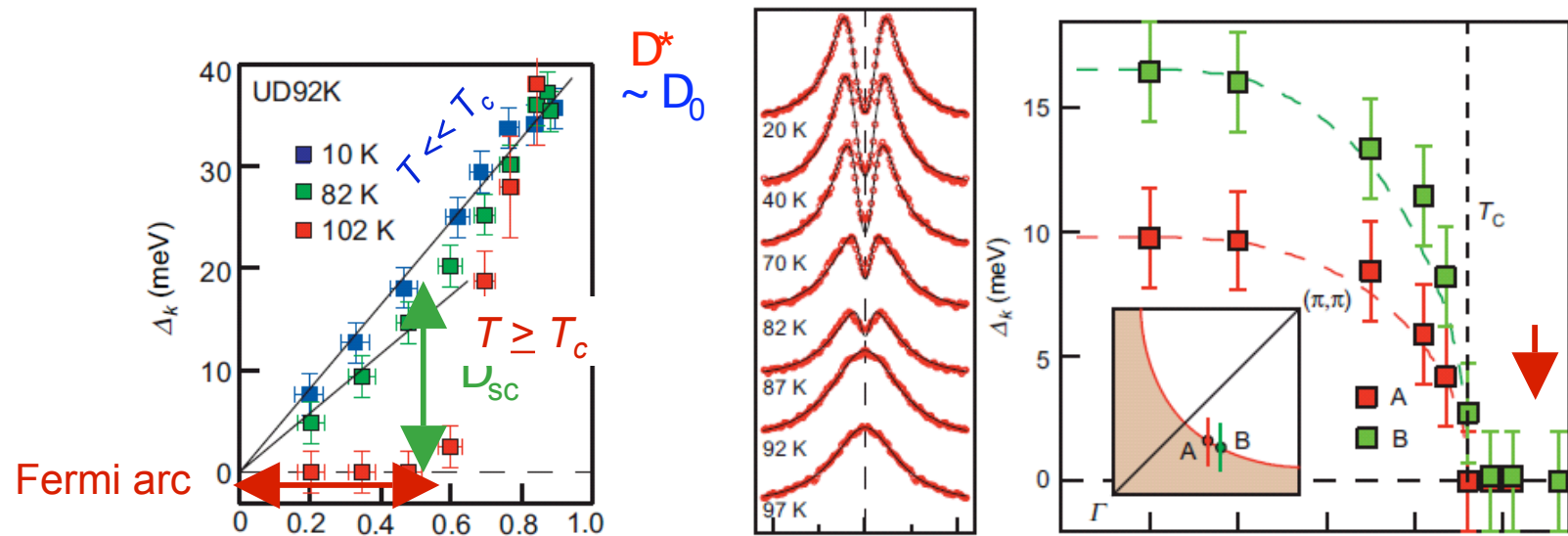
T. Yoshida et al.

# Two gap energy scales $D^*$ and $D_0$ in underdoped cuprates

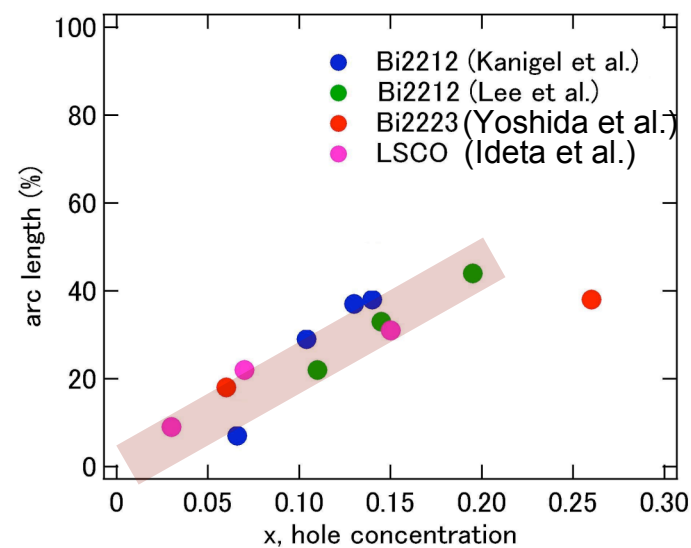


$$D(\mathbf{k}) = D_0(\cos k_x a - \cos k_y a) \text{ near node}$$

# Temperature dependence of superconducting gap/pseudogap in underdoped Bi2212

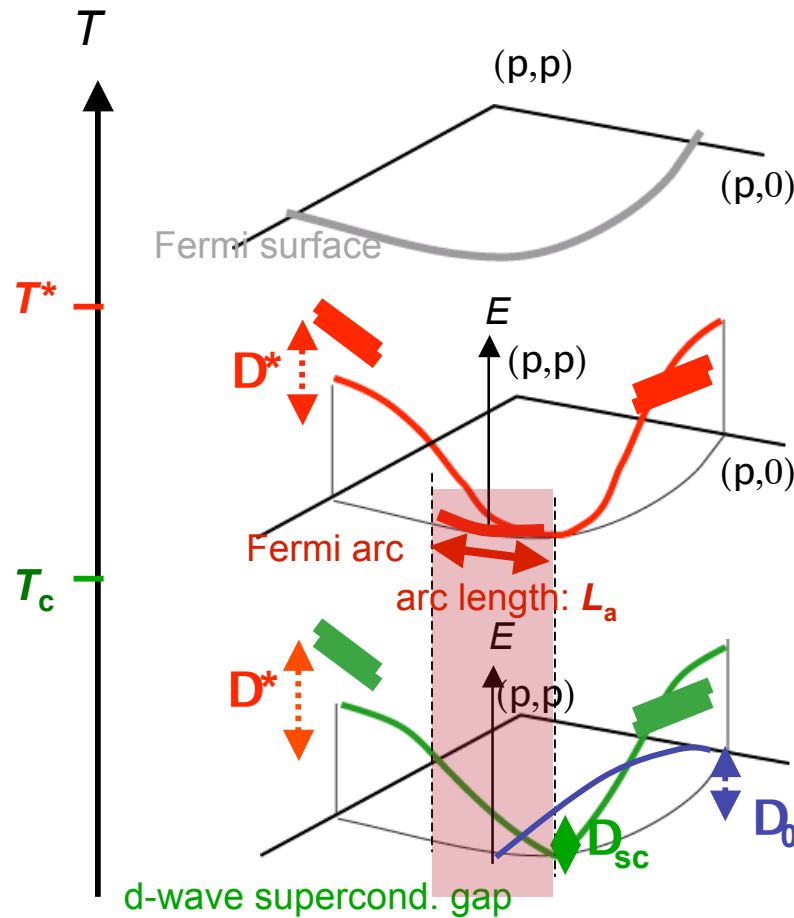


W.S. Lee et al., Nature '07

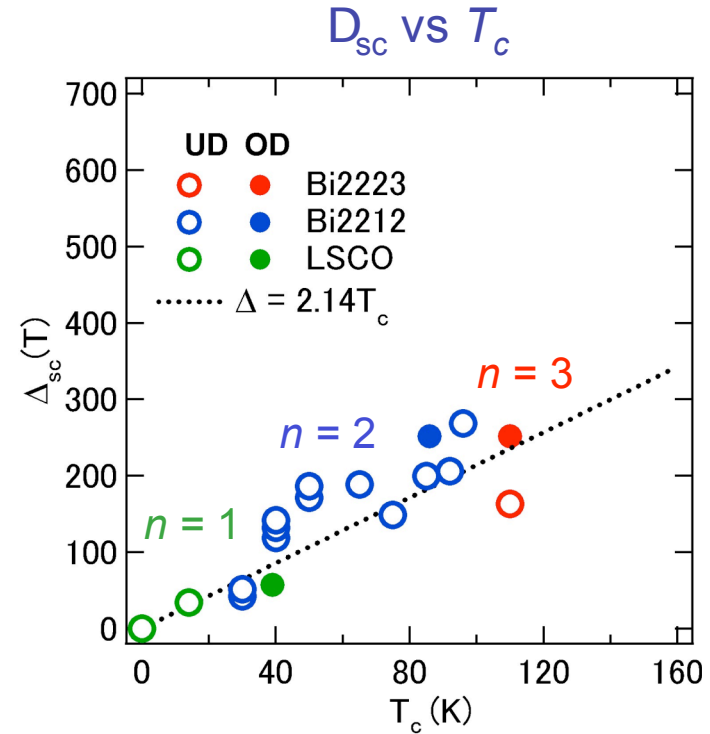


Ideta et al

# Superconducting gap $D_{sc}$ vs $T_c$



M. Oda et al, JPSJ '00  
P.A. Lee and X.G. Wen, PRL '97

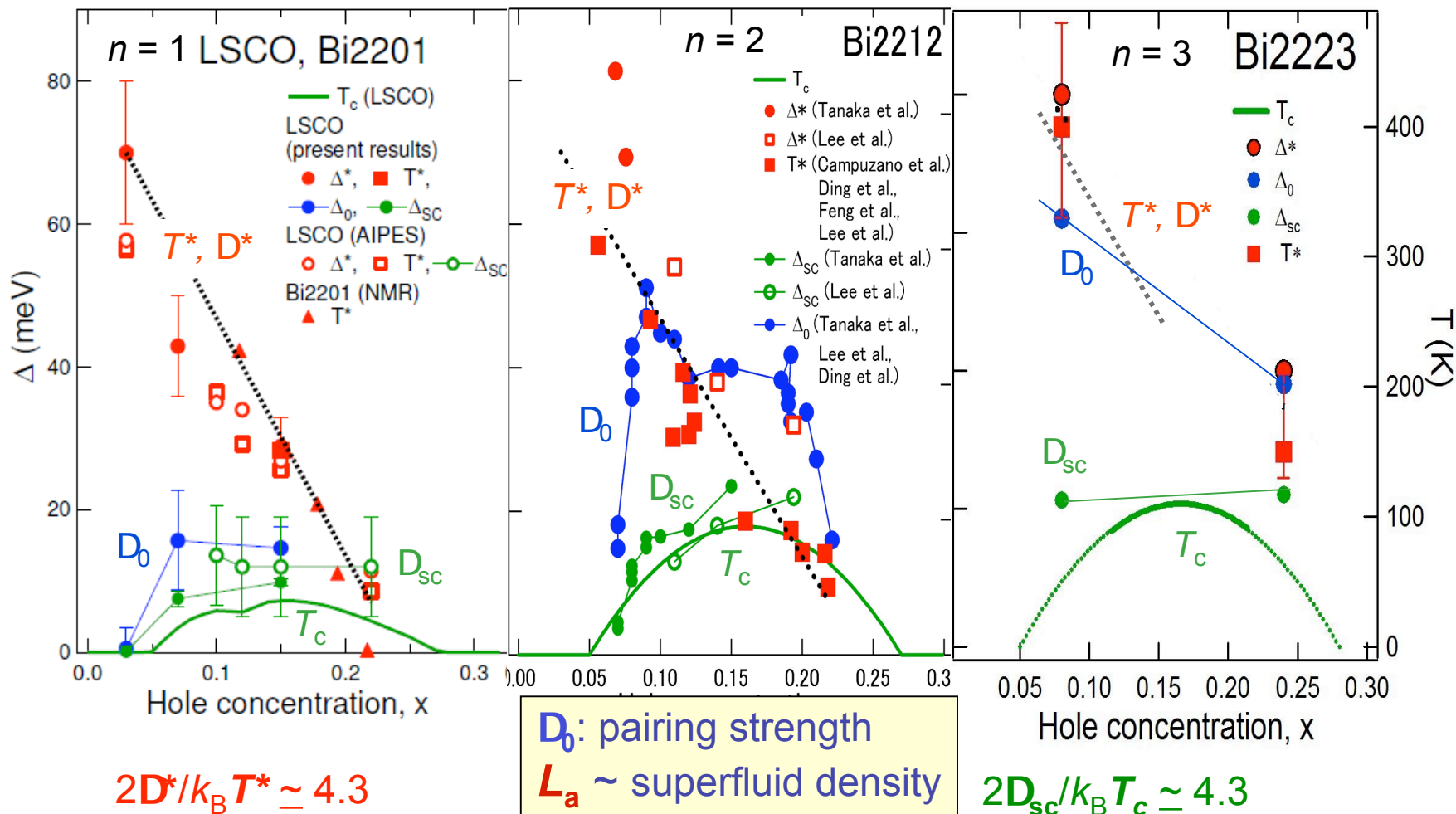


$$2D_{sc}/k_B T_c \approx 4.3$$

$$D_{sc} \sim D_0 (a/2\sqrt{2}) L_a$$

S. Ideta et al

# Superconducting gap/pseudogap in single, double and triple layer cuprates



T. Yoshida et al.  
S. Ideta et al.

# Dependence of $D_0$ and $T_{c,max}$ on the $\text{CuO}_2$ -layer number

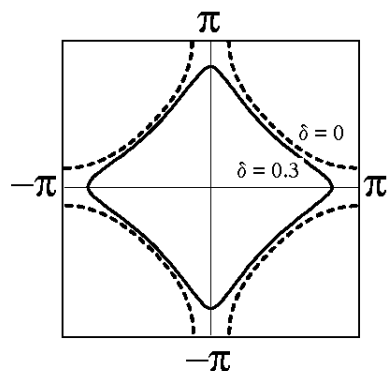
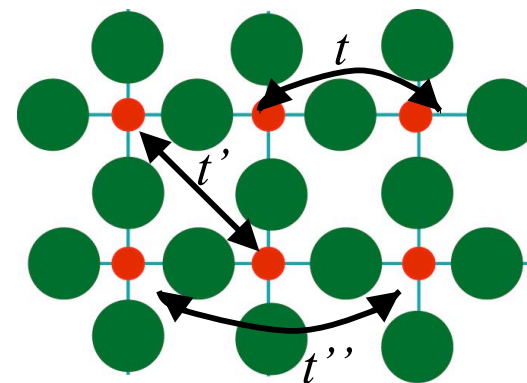
$D^*$ ,  $T^*$ : independent of  $\text{CuO}_2$ -layer #  
Property of a single  $\text{CuO}_2$  layer ( $U, J, t, \dots$ )

$D_0$ ,  $D_{sc}$ ,  $T_c$ : dependent on  $\text{CuO}_2$ -layer #

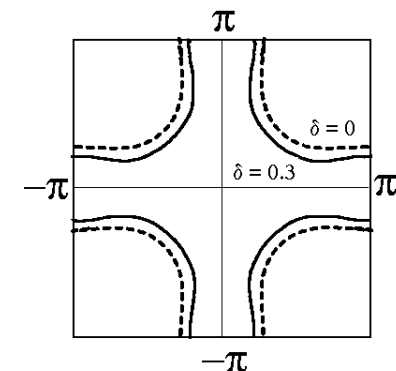
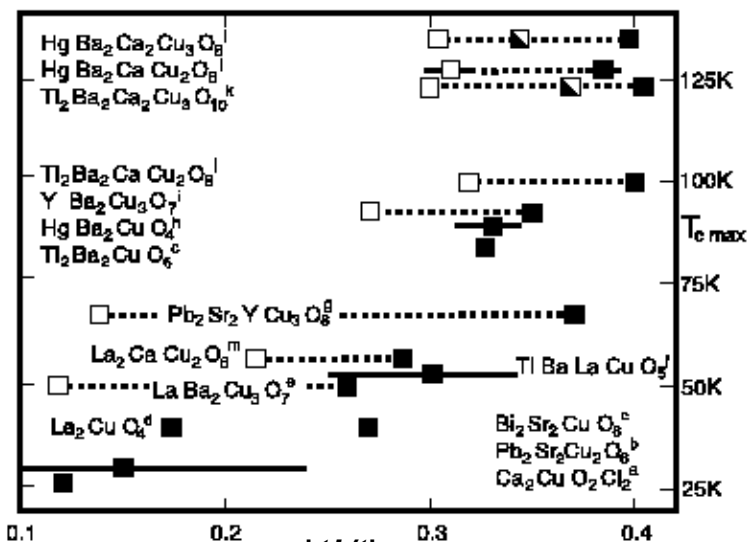
Apical oxygen ( $t', t'', \dots$ )

Out-of-plane disorder (Eisaki, Uchida)

Interlayer coupling – Copper pair tunneling

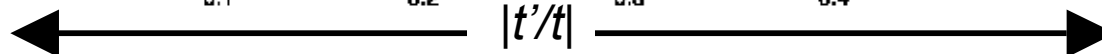


LSCO  $t'/t = -0.12, t''/t = 0.08$



BSCCO  $t'/t = -0.34, t''/t = 0.23$

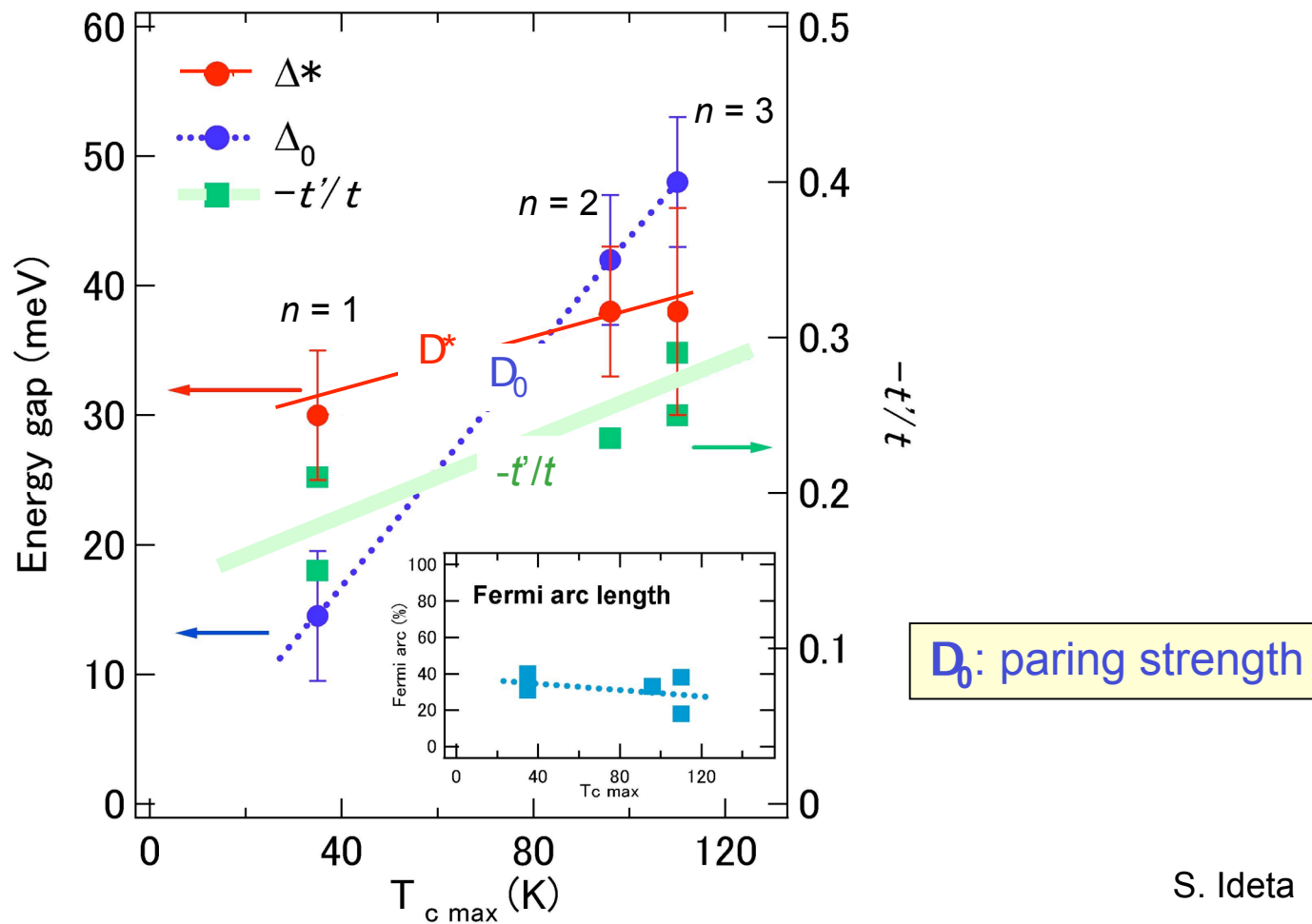
small



large

# Dependence of $T_{c,max}$ on material parameters

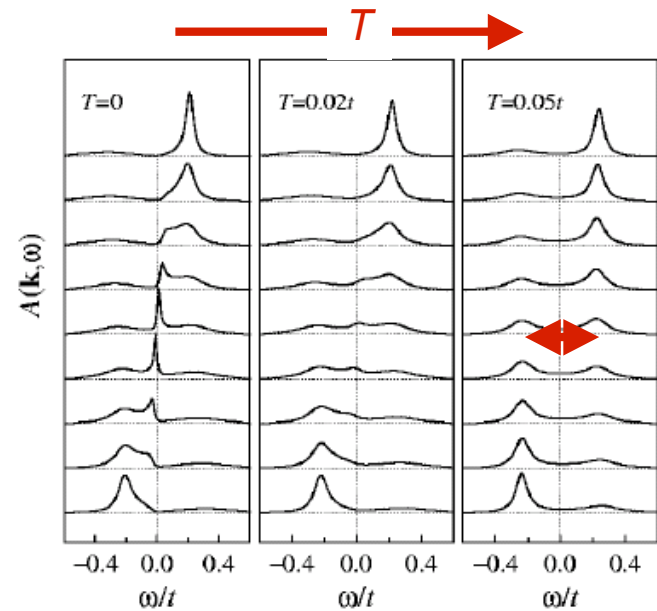
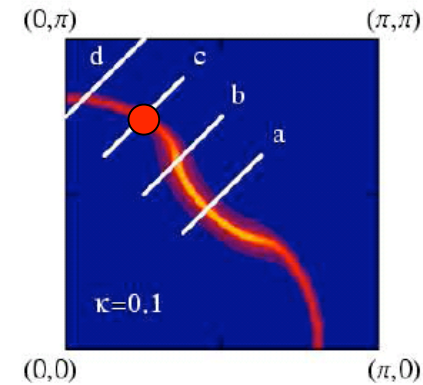
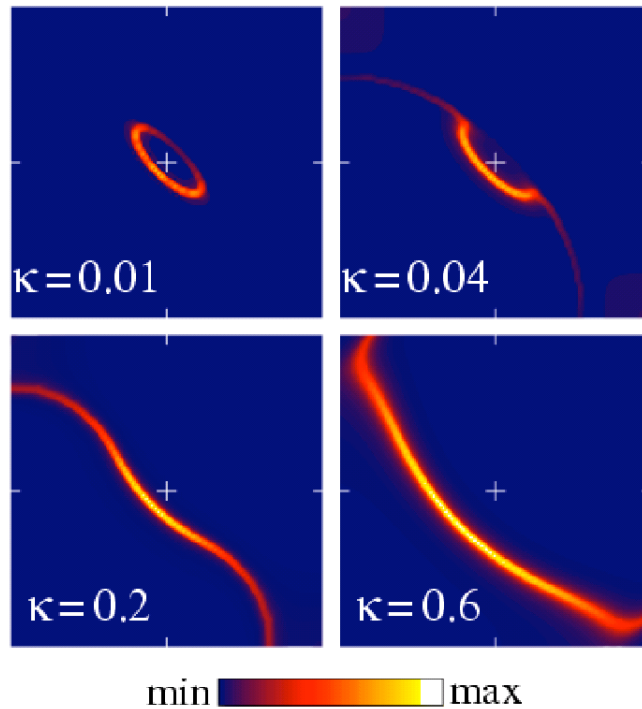
Relationship for optimally-doped LSCO, Bi2212, Bi2223



S. Ideta

# Possible origin of pseudogap? (1) Antiferromagnetic fluctuations

Generalized  $t$ - $J$  model calc



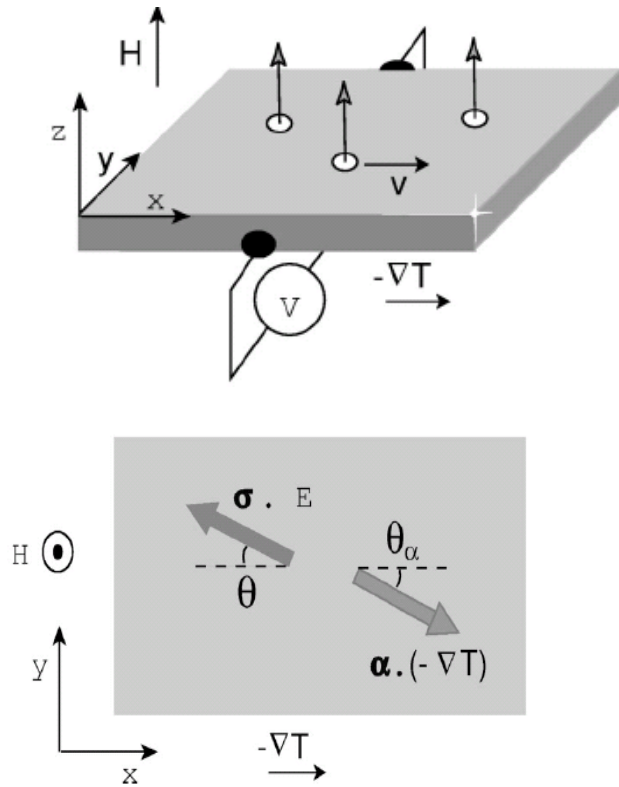
Pseudogap

P. Prelovsek and A. Ramsak, PRB '02

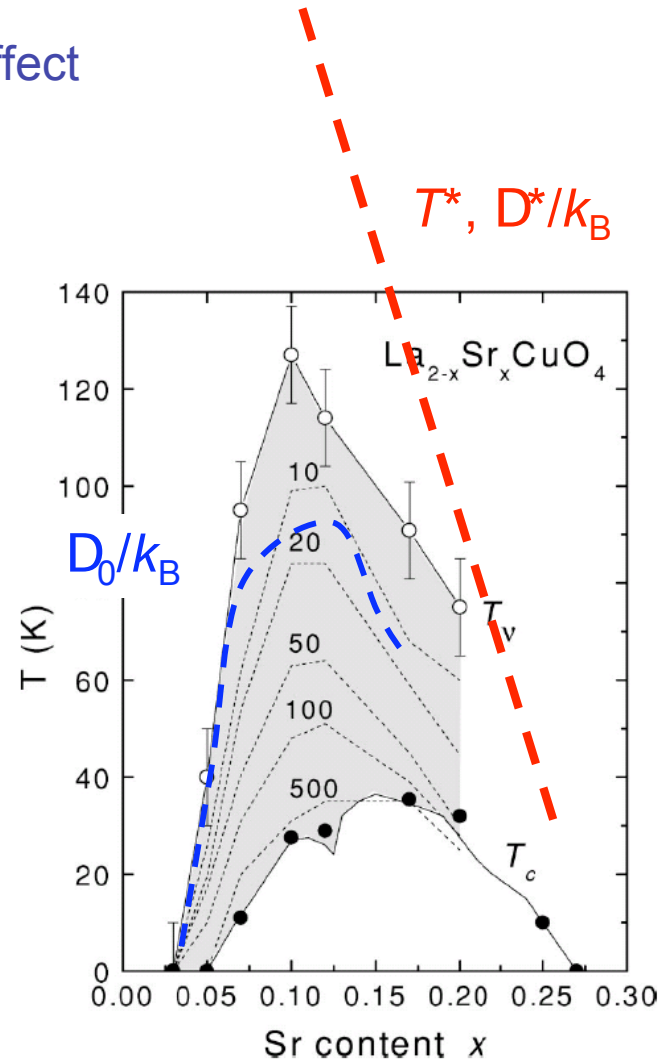


# Possible origin of pseudogap? (2) *d*-wave pairing fluctuations

Nernst effect

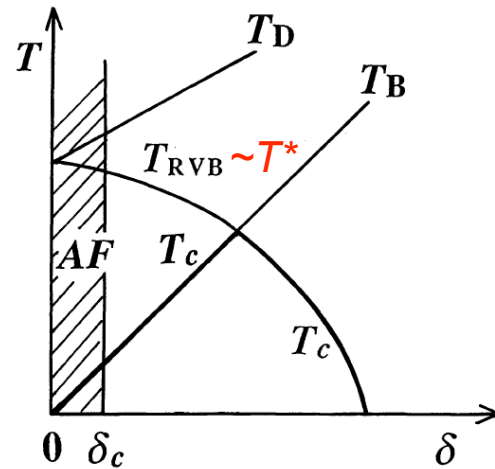


Signals too weak  
Drops toward  $x \rightarrow 0$  unlike  $T^*$



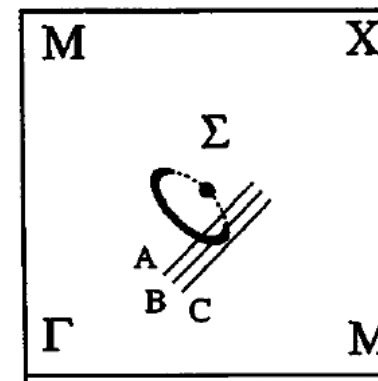
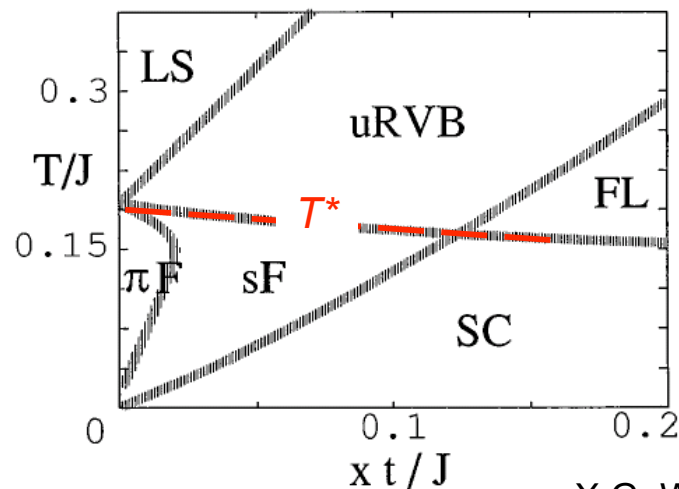
# Possible origin of pseudogap? (3) RVB - Resonating Valence Bonds

Slave-boson mean-field theories



H. Fukuyama  
N. Nagaosa and P.A. Lee  
G. Baskaran  
G. Kotliar

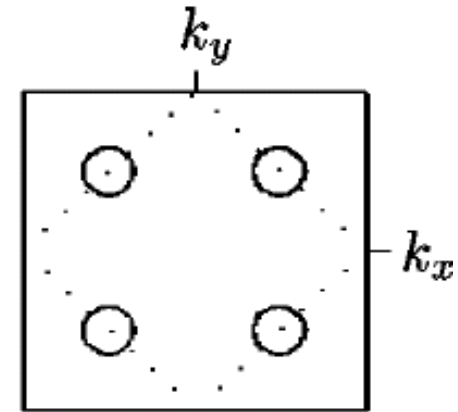
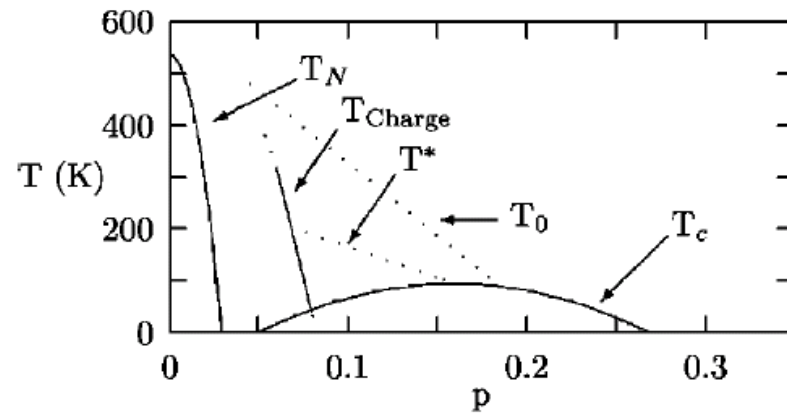
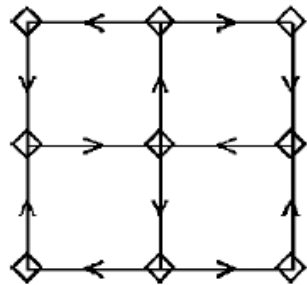
SU(2)



X.G. Wen and P.A. Lee, PRL '98

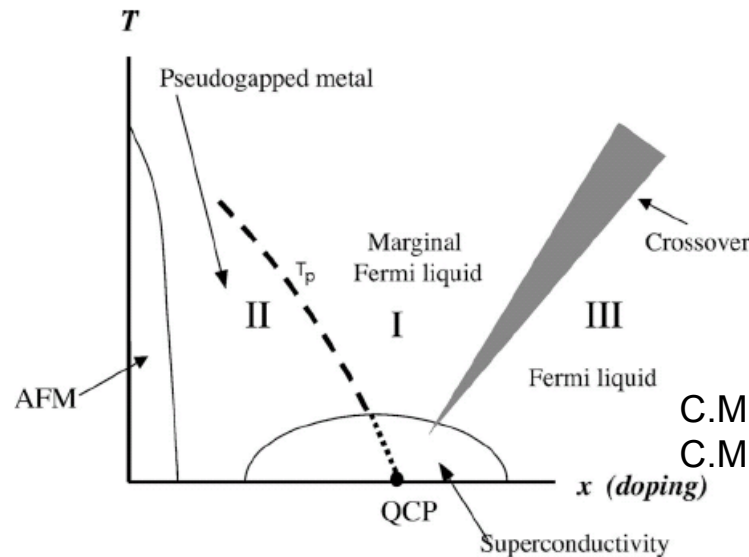
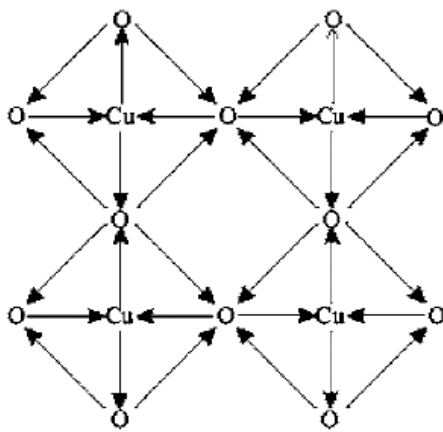
# Possible origin of pseudogap? (4) Time-reversal symmetry breaking

*d*-DW



S. Chakraverty et al., PRB '01

Circulating current in *p*-*d* model



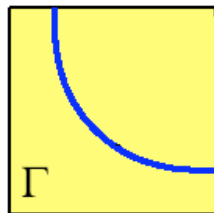
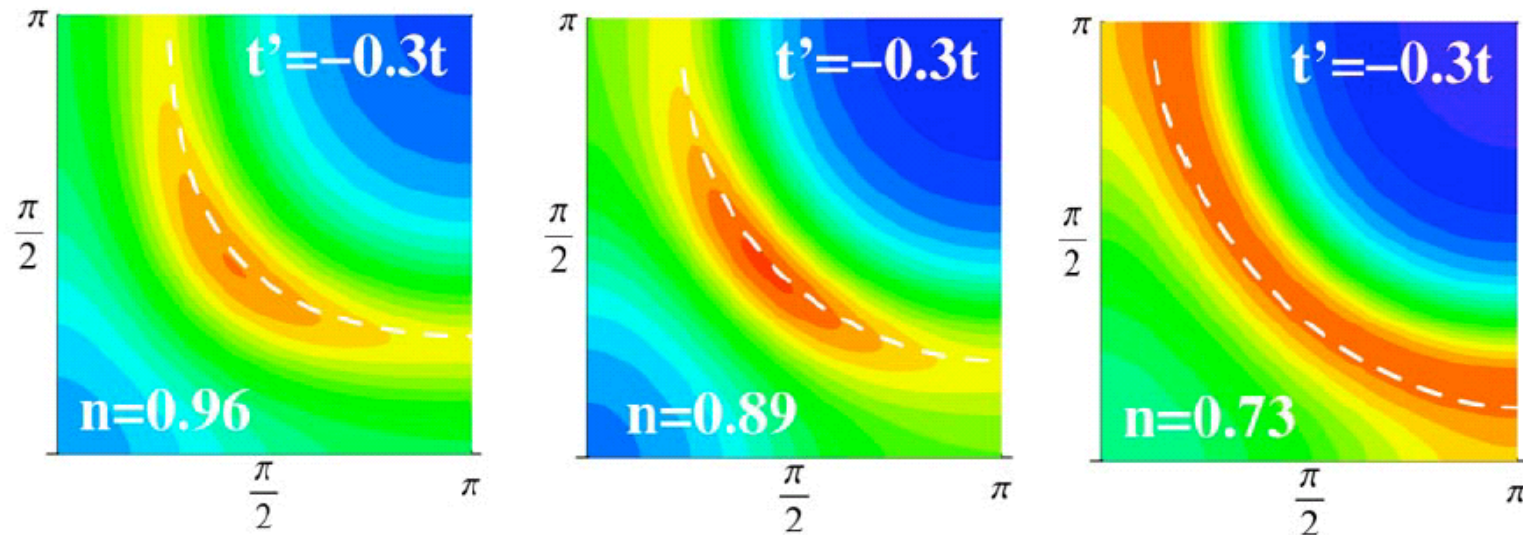
→ Fermi arc

C.M. Varma PRB '06

C.M. Varma and L. Zhu, RL '07

# Possible origin of pseudogap? (5) $k$ -dependent Mott transition

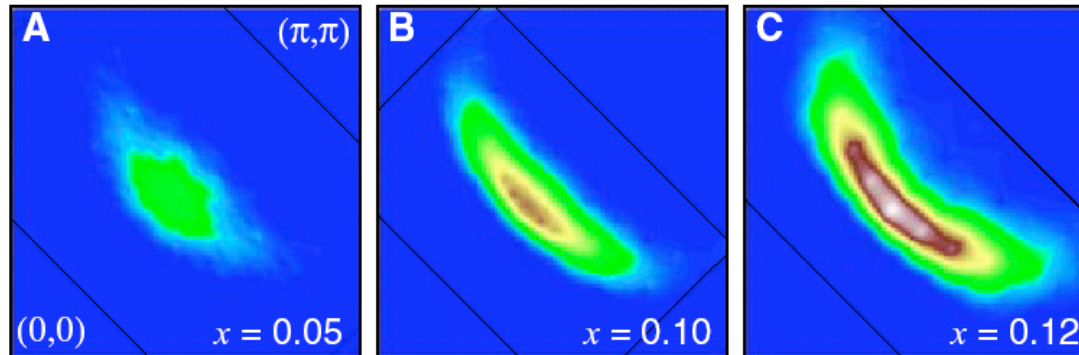
CDMFT calc



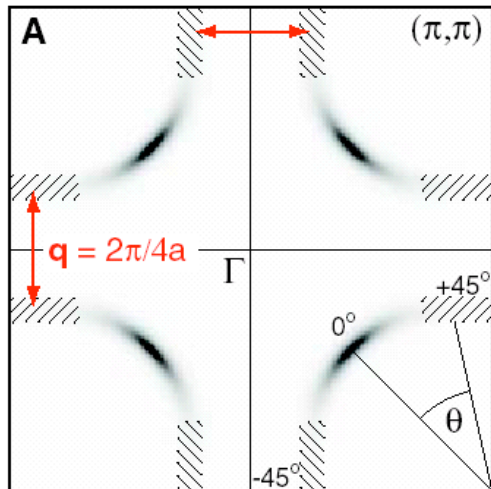
M. Civelli et al., PRL '05  
Y.Z. Zhang and M. Imada, PRB '07

# Possible origin of pseudogap? (6) CDW, polaron effects

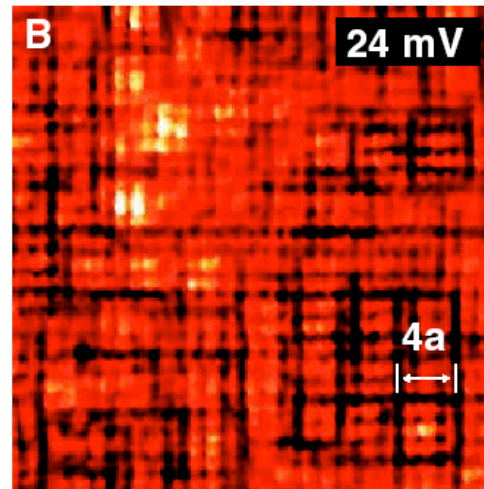
Fermi arc in  $\text{Na}_x\text{Ca}_{2-x}\text{CuCl}_2\text{O}_2$



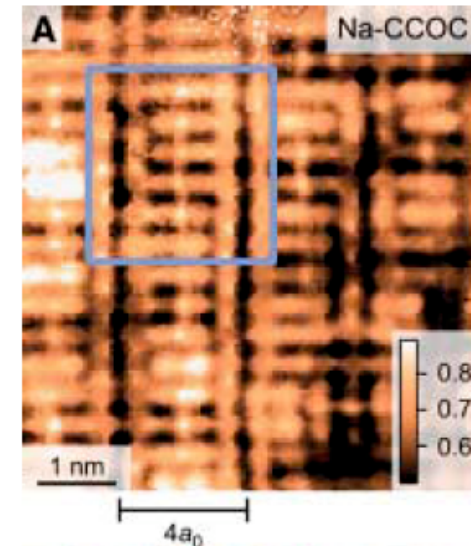
Fermi surface nesting?



Checkerboard pattern?



Cluster glass in STM?



K.M. Shen et al., Science '05

Y. Kohsaka et al., Science '07

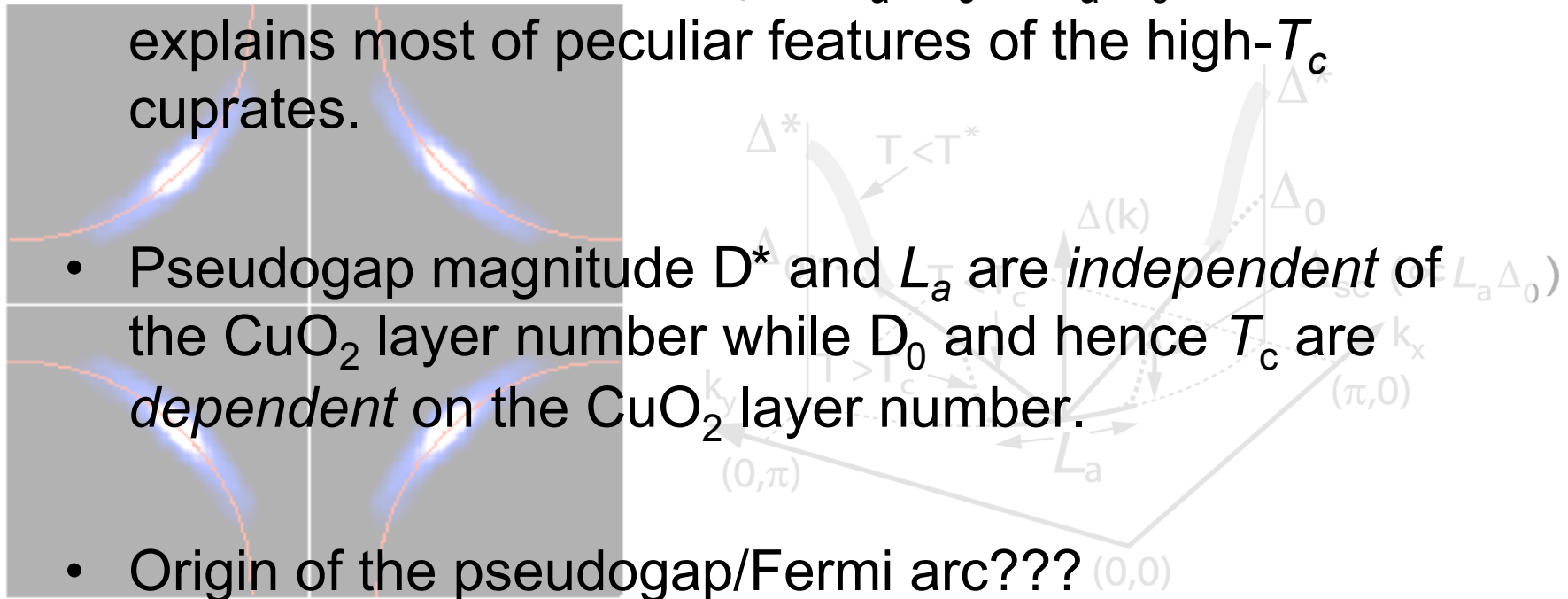
# Short summary 1

- Superconductivity in high- $T_c$  cuprates occurs on the Fermi arc of length  $L_a$ .

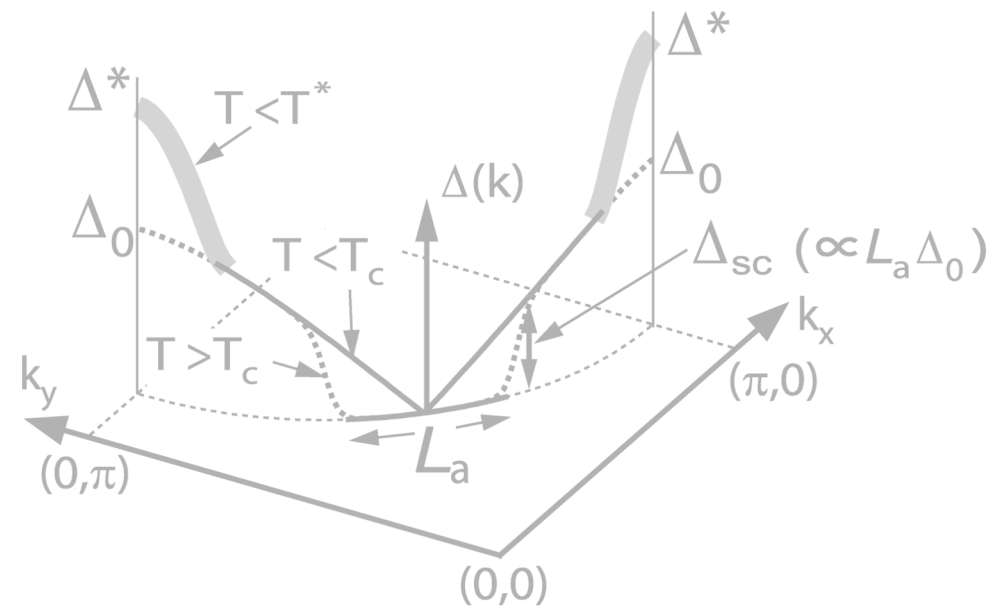
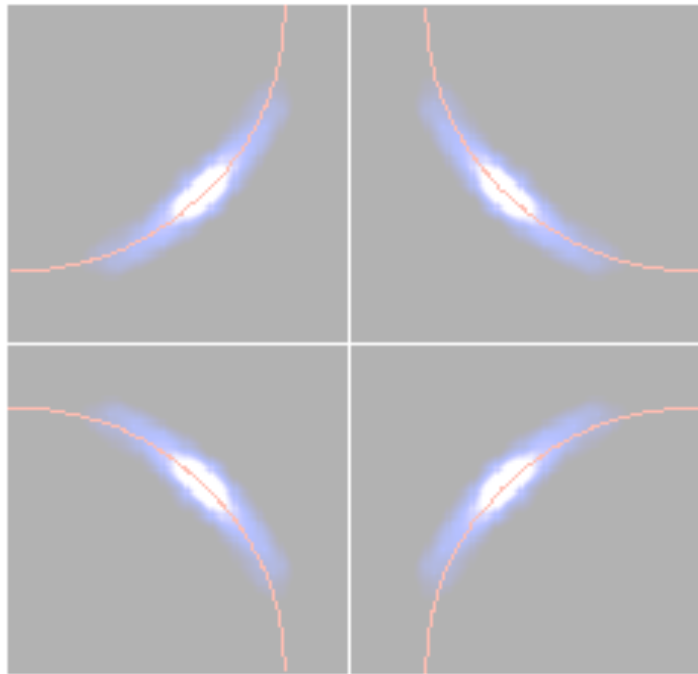
$T_c$  is determined by the pairing strength  $D_0$  and the available electron density  $\propto L_a$ :  $T_c \propto L_a D_0$ , which explains most of peculiar features of the high- $T_c$  cuprates.

- Pseudogap magnitude  $D^*$  and  $L_a$  are *independent* of the  $\text{CuO}_2$  layer number while  $D_0$  and hence  $T_c$  are *dependent* on the  $\text{CuO}_2$  layer number.

- Origin of the pseudogap/Fermi arc???

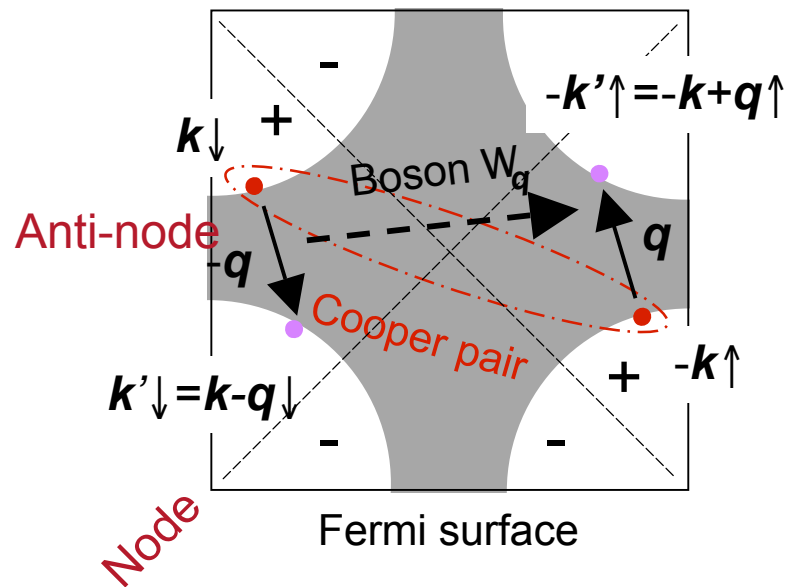


# Coupling of electron to Boson excitations

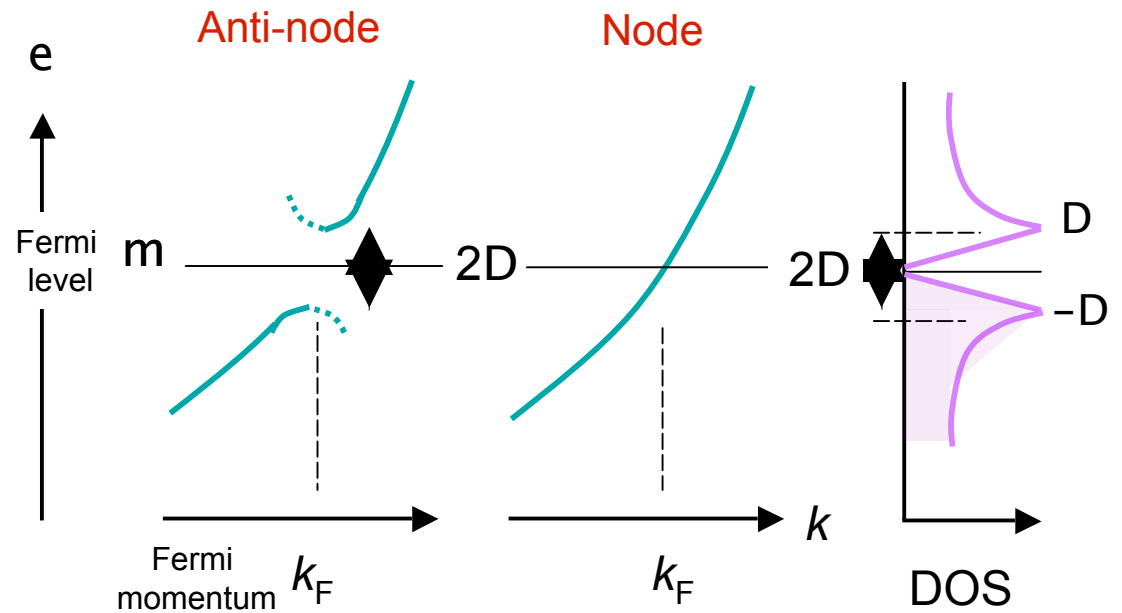


# Boson-mediated d-wave superconductivity

Cooper pair formation



Superconducting gap + boson structure



$$\Psi_{\text{BCS}} = \prod_{\mathbf{k}} (u_{\mathbf{k}} + v_{\mathbf{k}} a_{\mathbf{k},\uparrow}^+ a_{-\mathbf{k},\downarrow}^+) |0\rangle$$

$$\Delta_{\mathbf{k}} = \frac{1}{2} \sum_{\mathbf{k}' > 0} \frac{\Delta_{\mathbf{k}'}}{\sqrt{\epsilon_{\mathbf{k}'}^2 + \Delta_{\mathbf{k}'}^2}} V_{\mathbf{k}\mathbf{k}'} \quad \text{Gap equation}$$

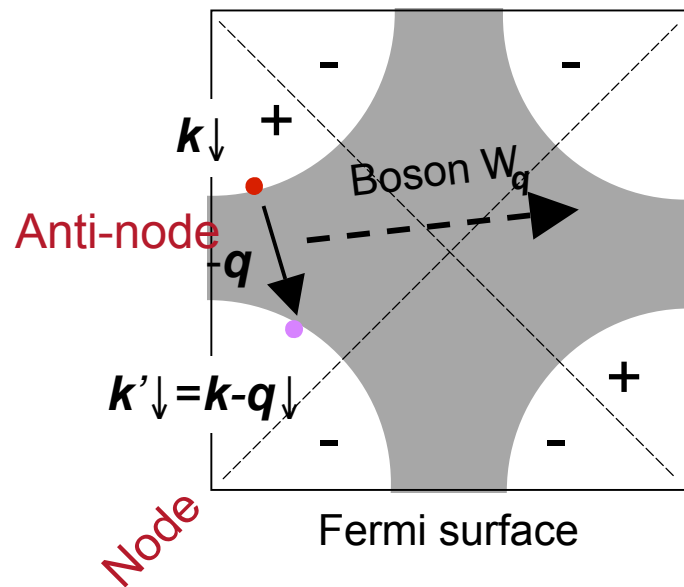
$$\epsilon = \pm \sqrt{\epsilon(\mathbf{k})^2 + \Delta(\mathbf{k})^2}$$

$$D(\mathbf{k}) = D_0(\cos k_x a - \cos k_y a)$$

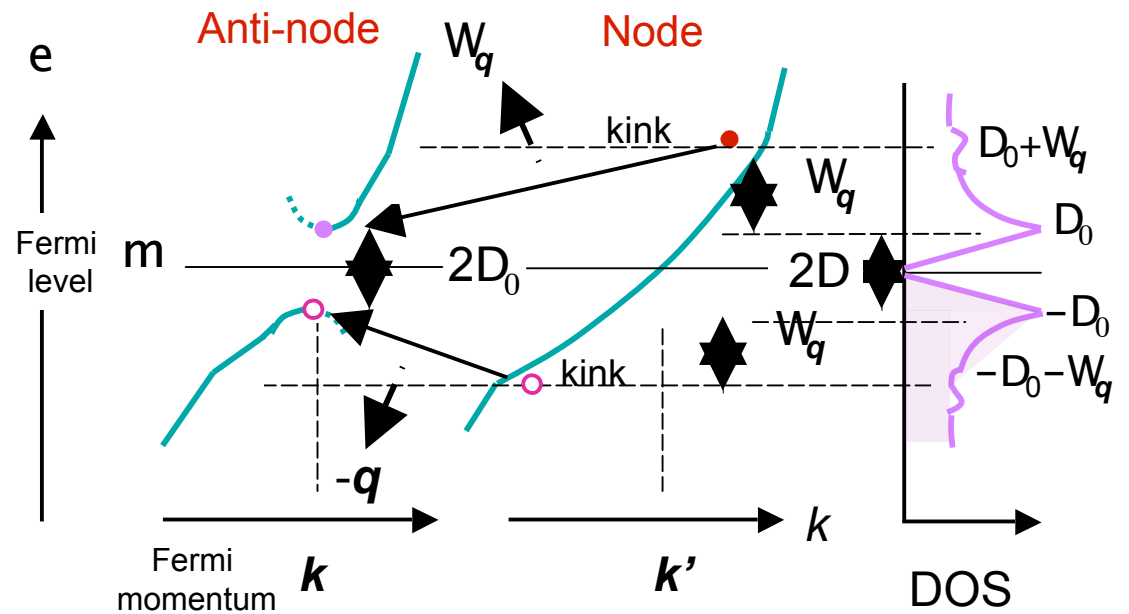


# Scattering of quasi-particle by Boson excitation

Electron-Boson coupling



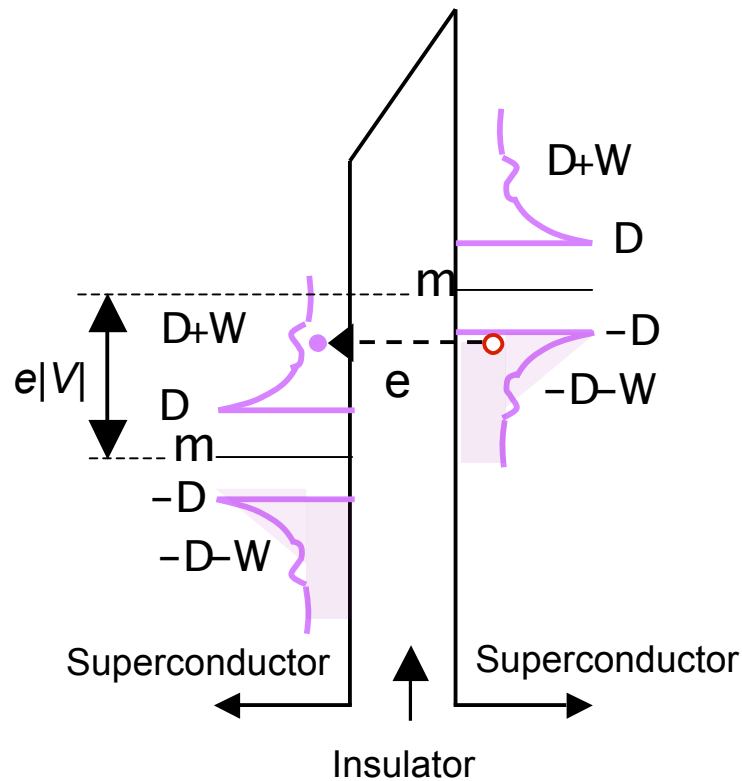
Superconducting gap + boson structure



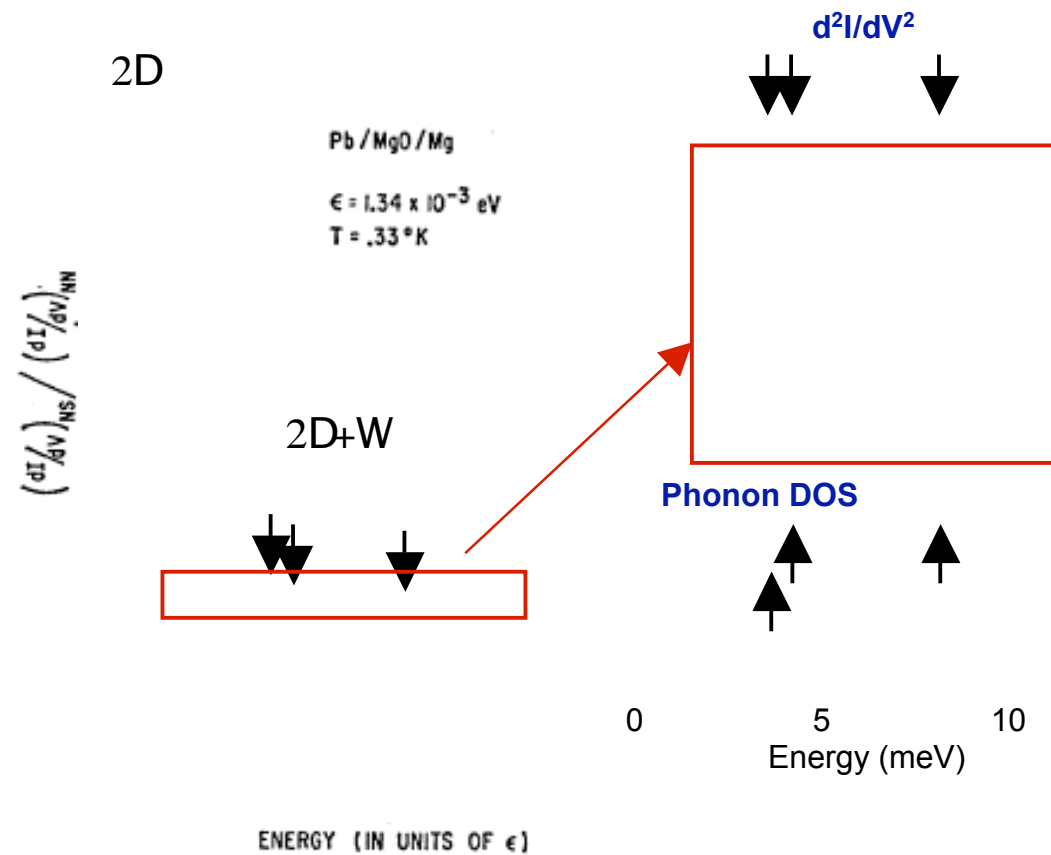
$W_q$ : Boson energy

# Evidence for electron-phonon coupling from tunneling spectroscopy

S/I/S tunneling barrier

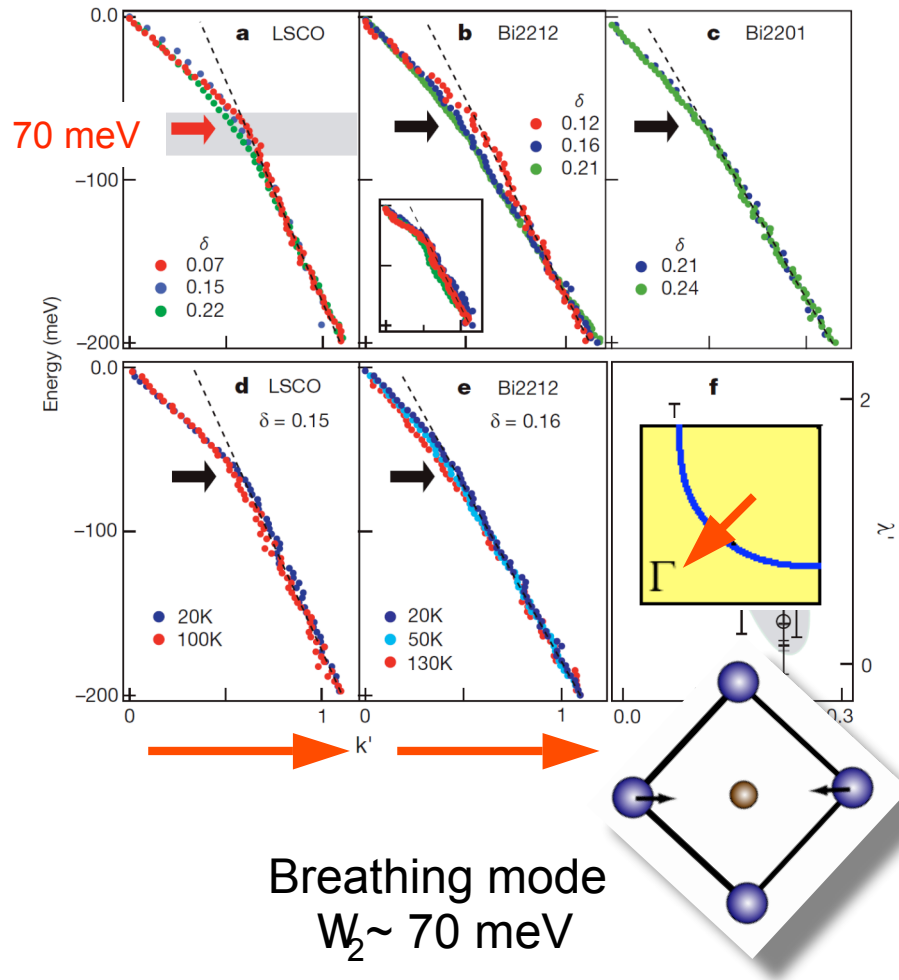


Tunneling spectrum of Pb/MgO/Pb junction



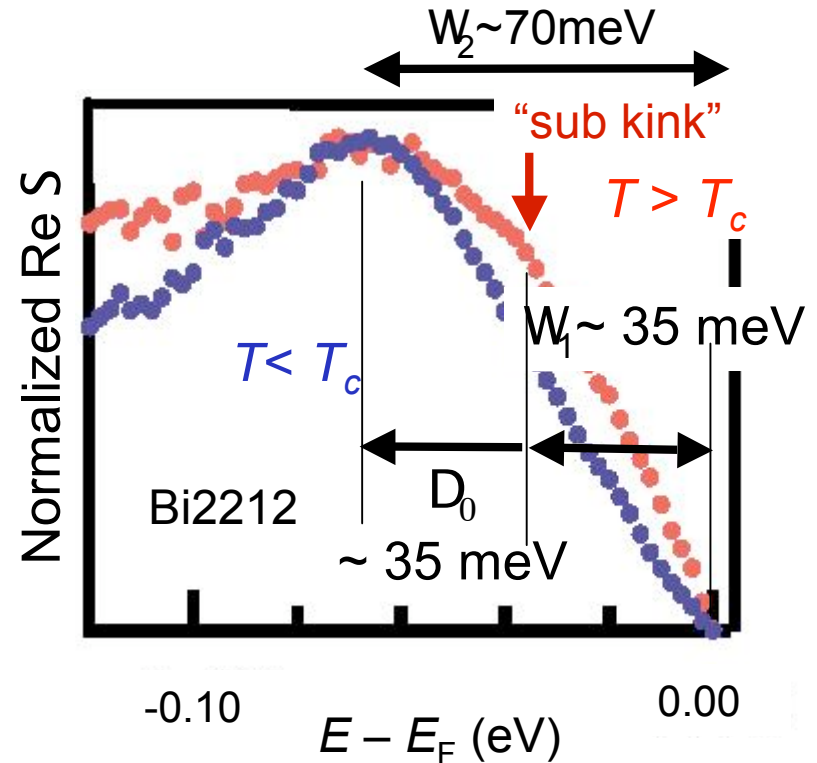
# ~70 meV kink in the nodal direction

## Previous interpretation



A. Lanzara et al., Nature '01

## New interpretation



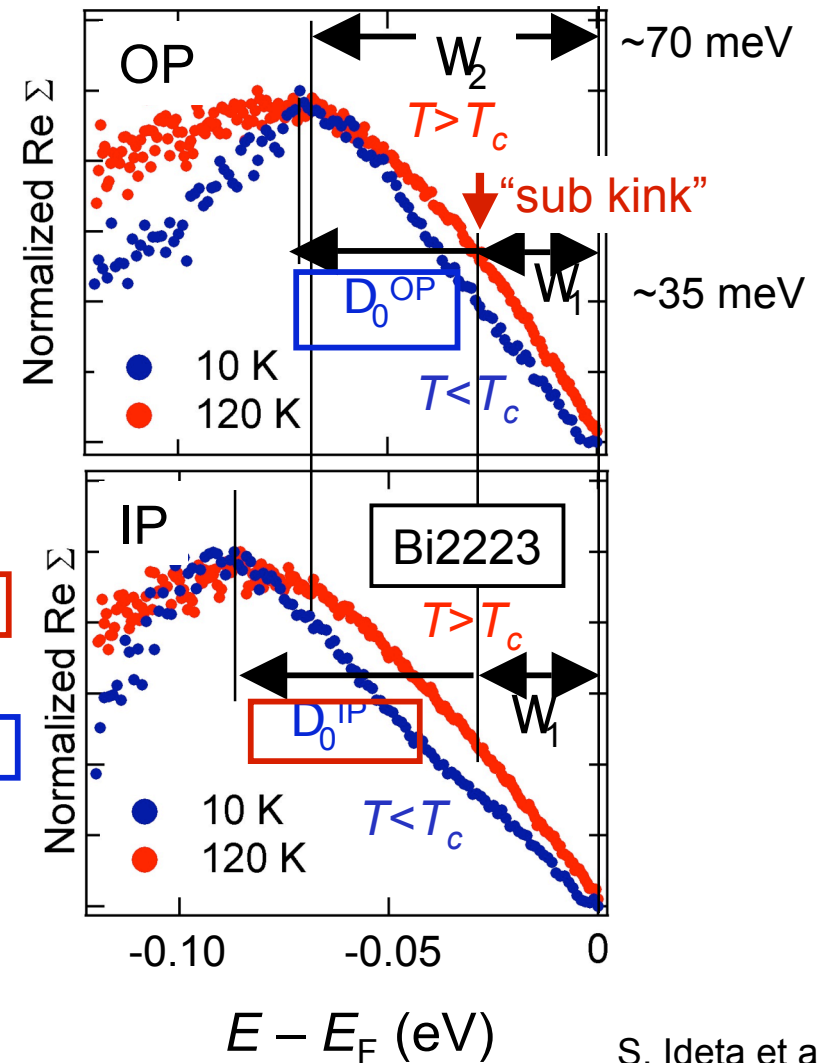
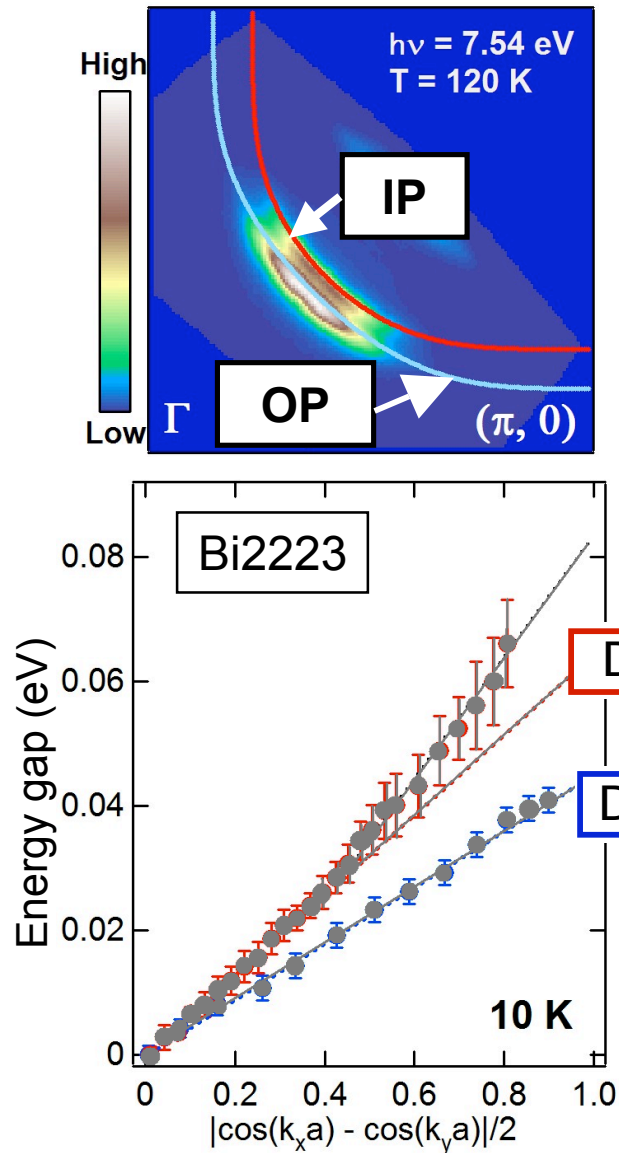
Boson energies

$$\begin{cases} W_1 \sim 35 \text{ meV} \\ W_2 \sim 70 \text{ meV} \end{cases}$$

W. S. Lee et al., PRB '08

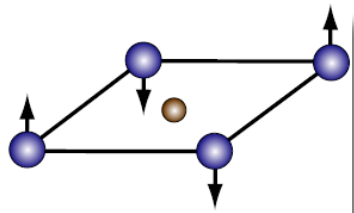
Theory: A. W. Sandvik et al., PRB '04

# ~95(!) meV kink in the trilayer cuprate Bi2223

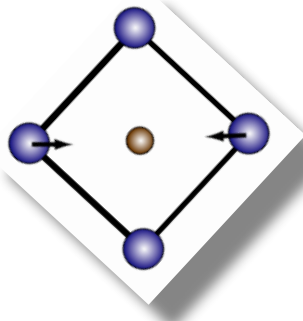


# Phonon scenario of ARPES kinks

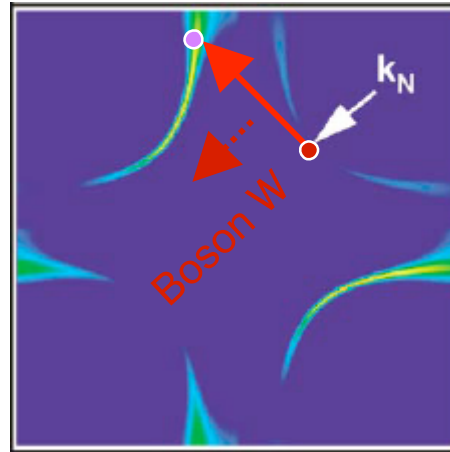
Buckling mode  
 $W_1 \sim 35$  meV



Breathing mode  
 $W_2 \sim 70$  meV

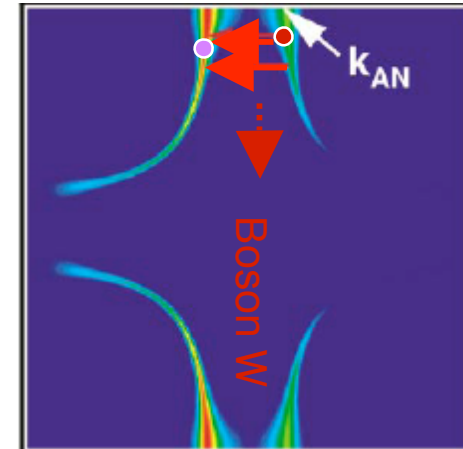


Nodal quasi-particle

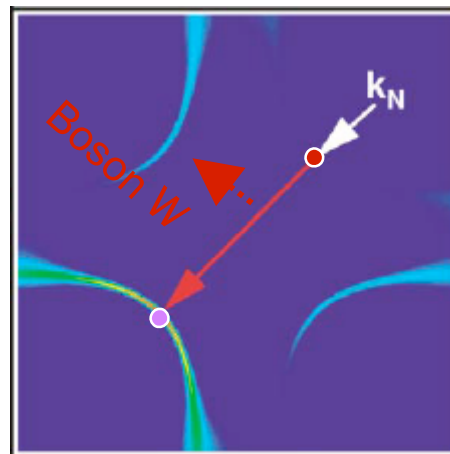


Kink at  $\sim W_1 + D_0$

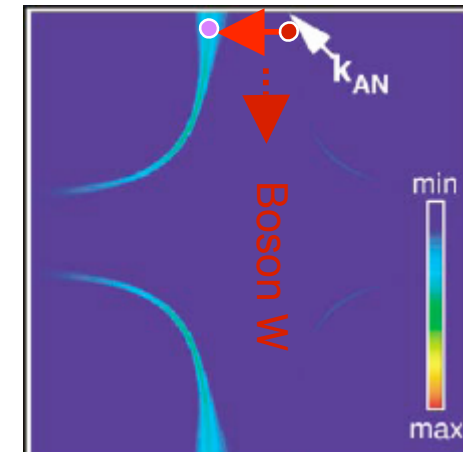
Antinodal quasi-particle



$W_1 + D_0$

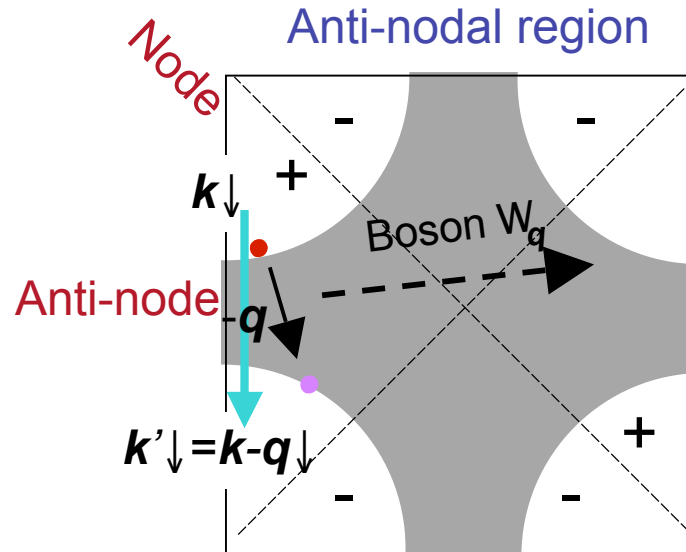
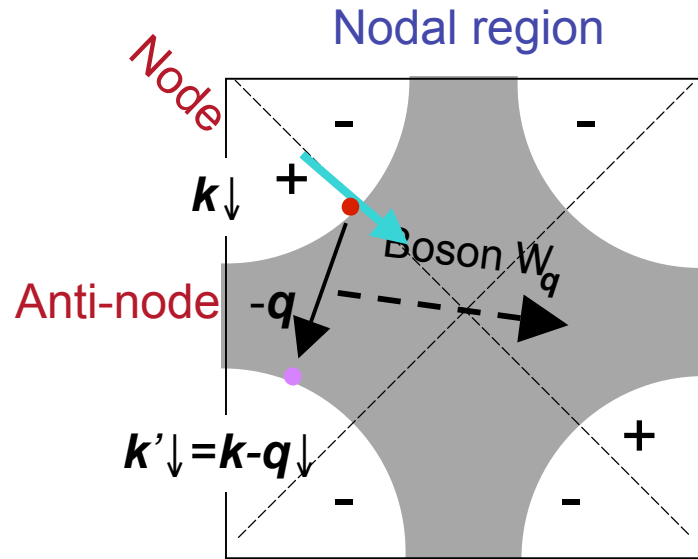


$W_2$

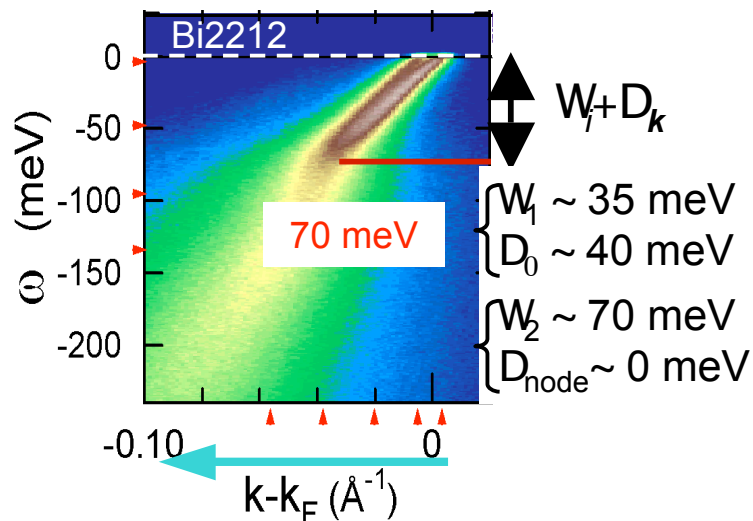


$W_2 + D_0$  but weak

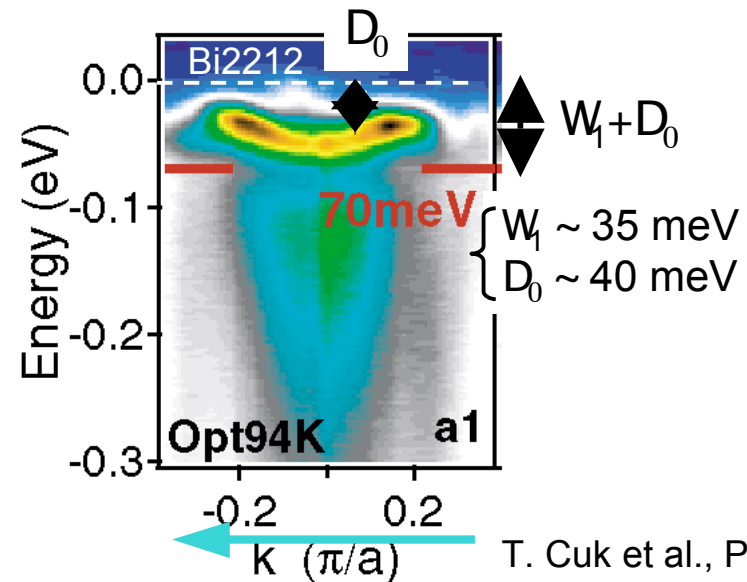
# Kink in ARPES spectra



Boson energies

$$\begin{cases} W_1 \sim 35 \text{ meV} \\ W_2 \sim 70 \text{ meV} \end{cases}$$


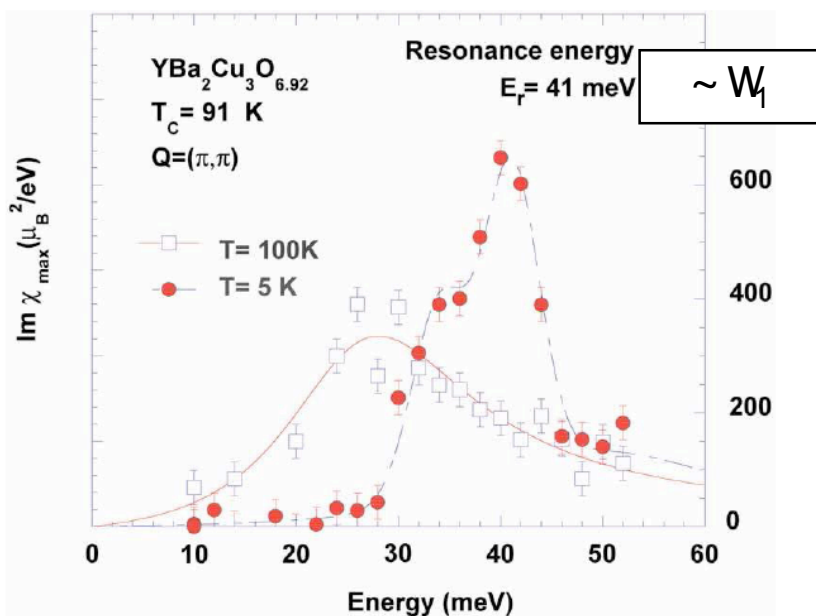
T. Yamasaki et al., PRB '07



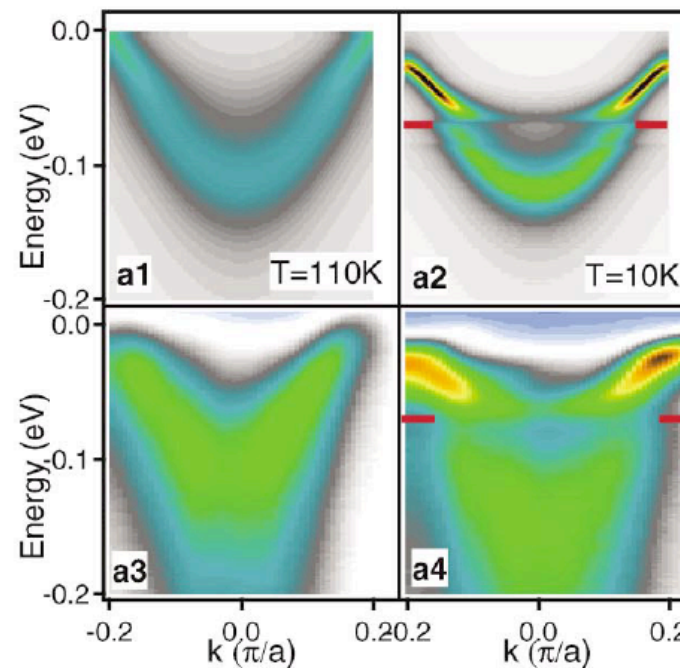
T. Cuk et al., PRL '04

# Coupling to magnetic resonance at $W_1 \sim 40$ meV

Inelastic neutron scattering spectra



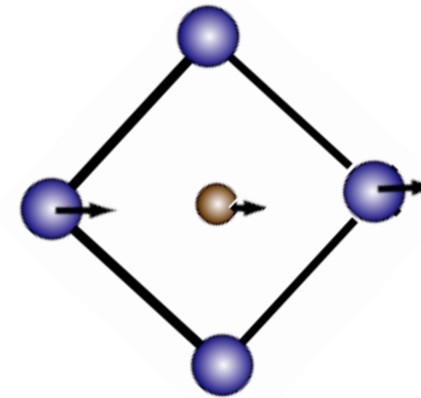
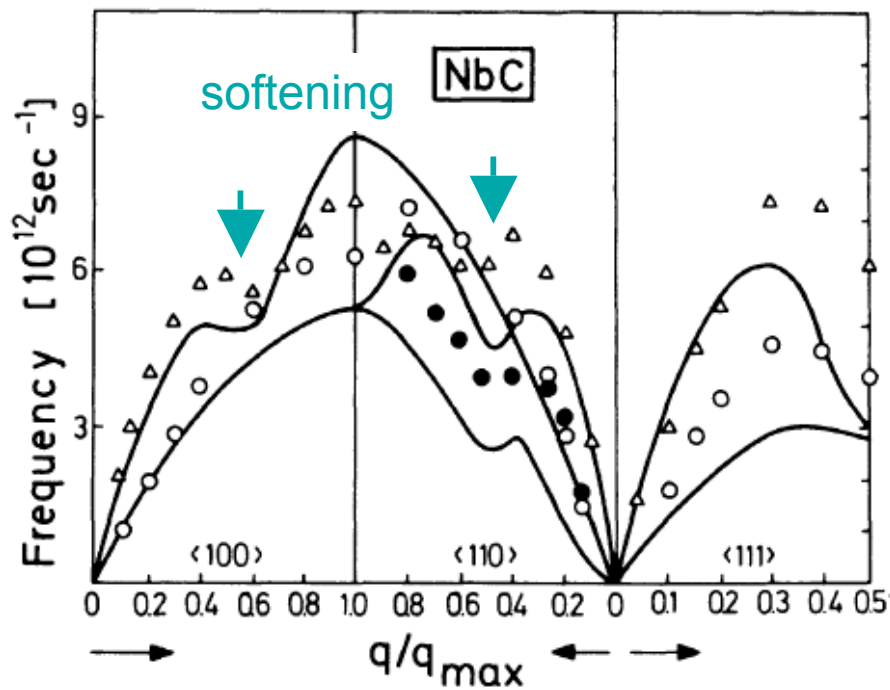
cf) Phonon scenario



Broadening of Boson spectrum above  $T_c$   $\rightarrow$  Smearing of ARPES kink around the anti-node  $\leftarrow$  Broadening of electronic spectrum above  $T_c$

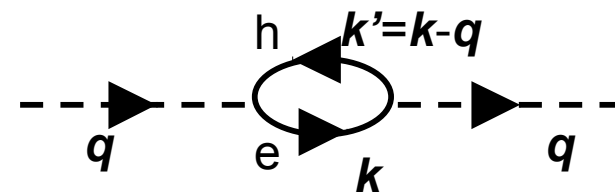
# Phonon anomalies in conventional BCS superconductors

Phonon dispersions in NbC by neutron scattering



Breathing LA phonons:  
 $q \sim (\pm p/2a, 0, 0)$

$\omega \sim 15 \text{ meV}$

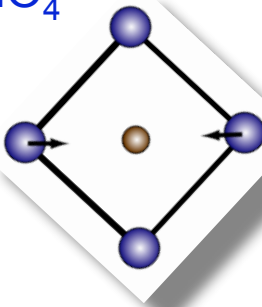
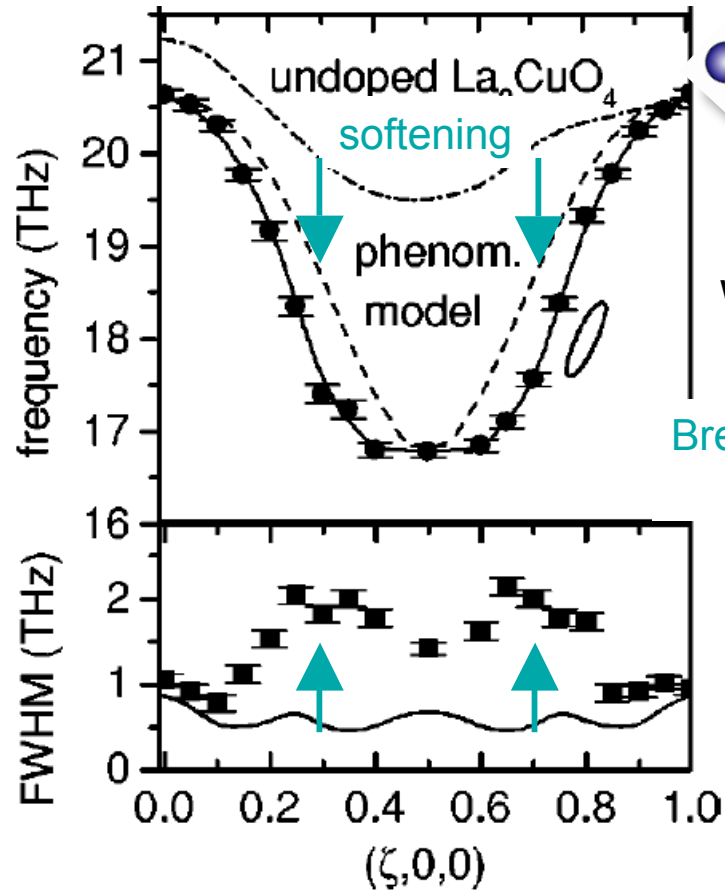


W. Hanke et al., PRL '76



# Corresponding $W_2 \sim 70$ meV phonon anomalies in high- $T_c$ cuprates

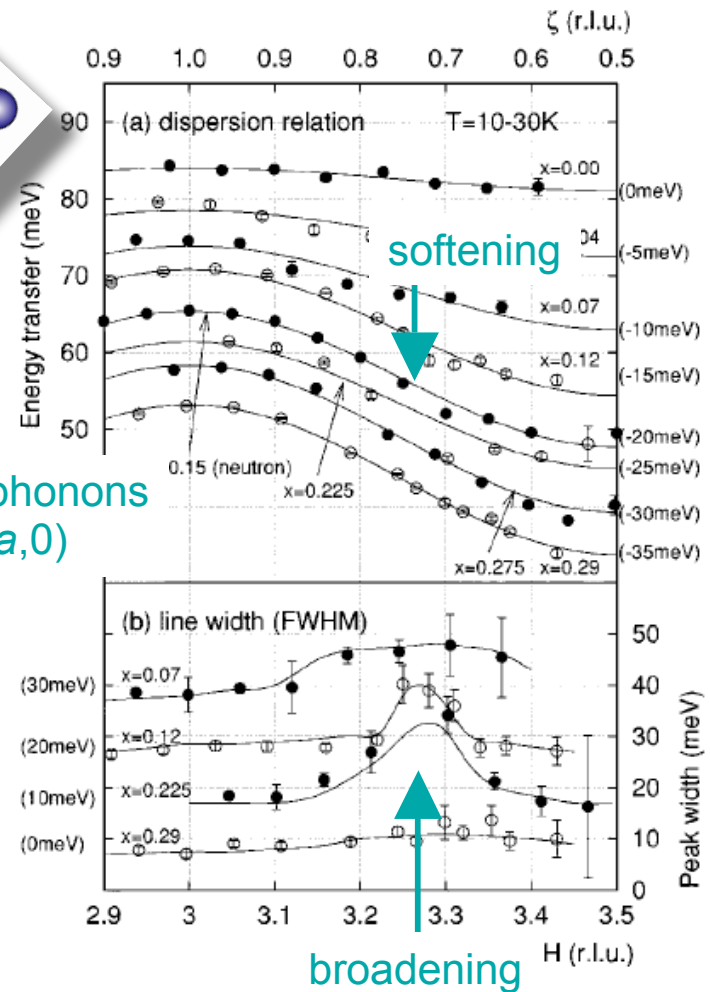
Neutron scattering of  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$



$W_2 \sim 70$  meV

Breathing LO phonons  
 $q \sim (\pm p/2a, 0)$

X-ray scattering of  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$

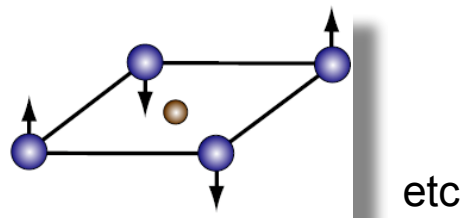
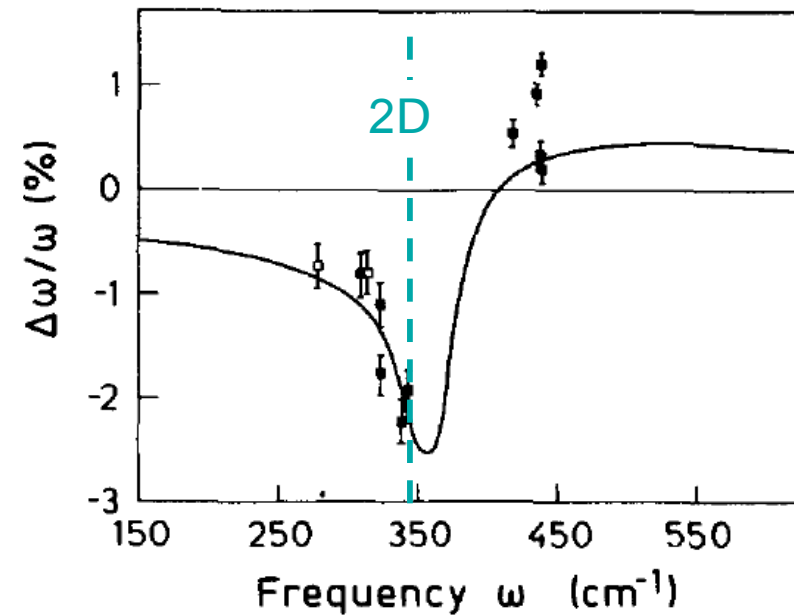
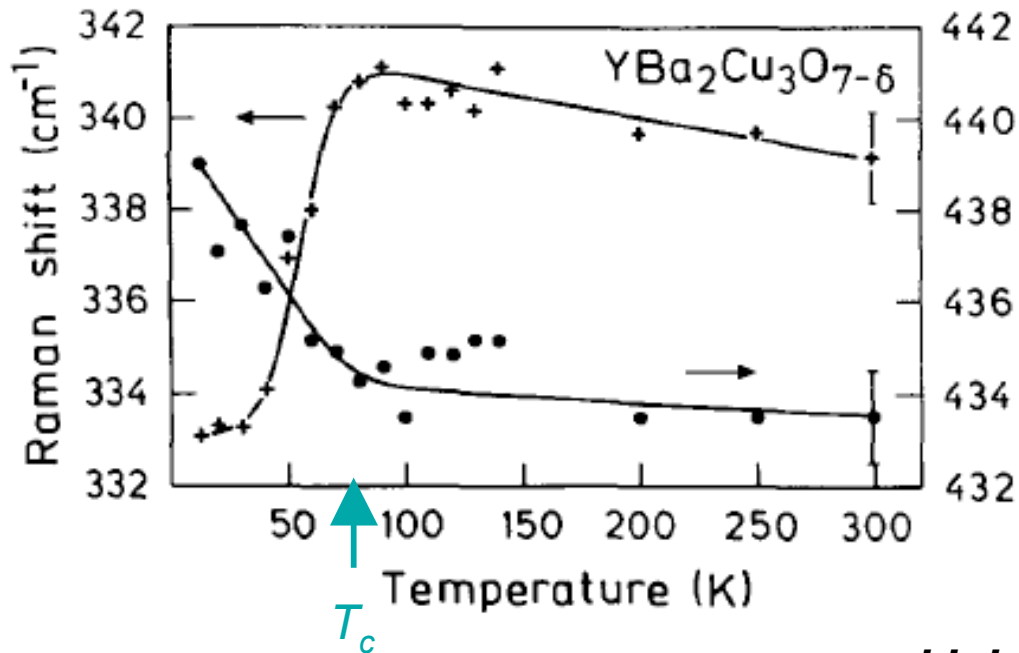


L. Pinchovius and M. Braden, PRB '99

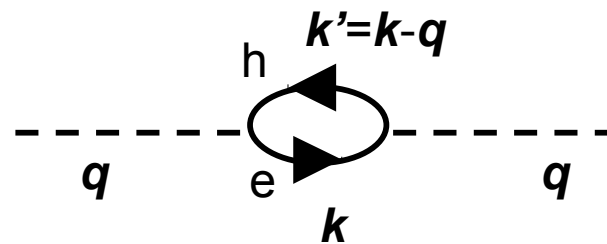
T. Fukuda et al., PRB '05

# Corresponding $\omega_1 \sim 35$ meV phonon anomalies in high- $T_c$ cuprates

Raman shifts in  $\text{YBa}_2\text{Cu}_3\text{O}_{7-d}$



$\omega_1 \sim 35$  meV

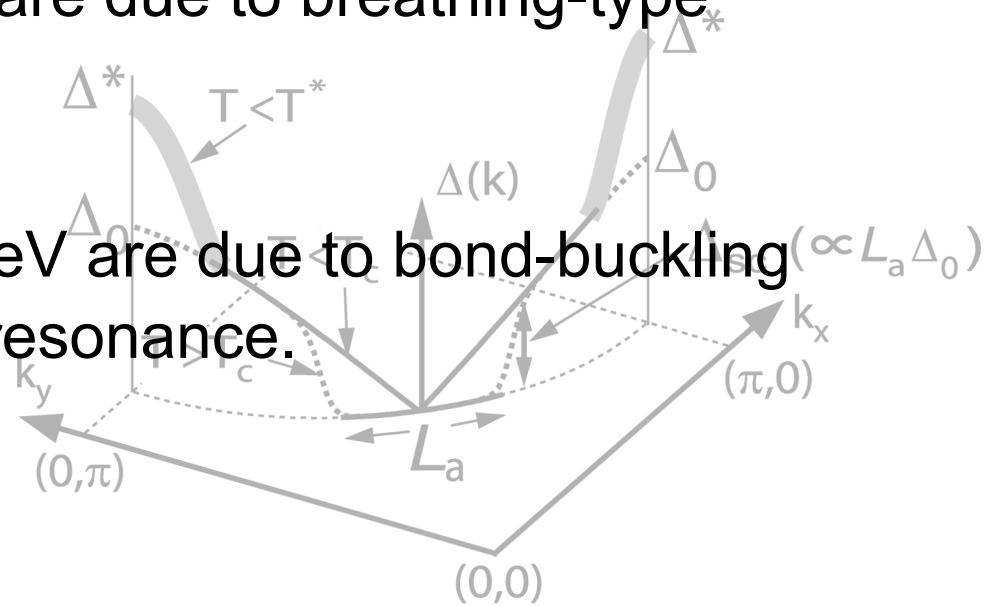
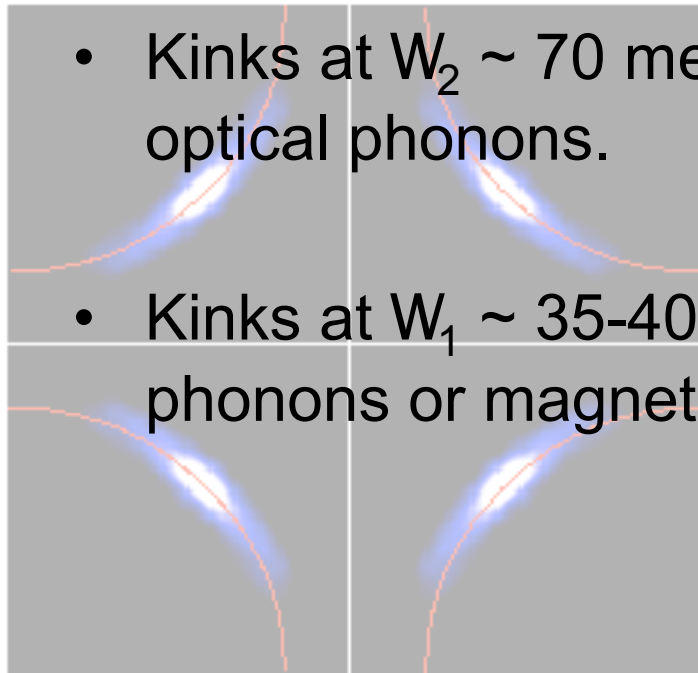


## Short summary 2

- Electrons are coupled to Boson excitations, which yield kinks in ARPES spectra and may provide glue for Cooper pairing.

- Kinks at  $W_2 \sim 70$  meV are due to breathing-type optical phonons.

- Kinks at  $W_1 \sim 35-40$  meV are due to bond-buckling phonons or magnetic resonance.



# Outlook

- Understanding the origin of the pseudogap/Fermiarc and the  $\text{CuO}_2$  layer number dependences of the pairing strength  $D_0$  and hence of  $T_{c,\text{max}}$  will provide a key to elucidate the mechanism of high- $T_c$  superconductivity.

- Understanding the momentum, temperature, doping, and  $\text{CuO}_2$  layer number dependences of kinks in ARPES spectra will also provide a key to understand the mechanism of high- $T_c$  superconductivity. *Close collaboration between ARPES, neutron and x-ray studies are indispensable.*

